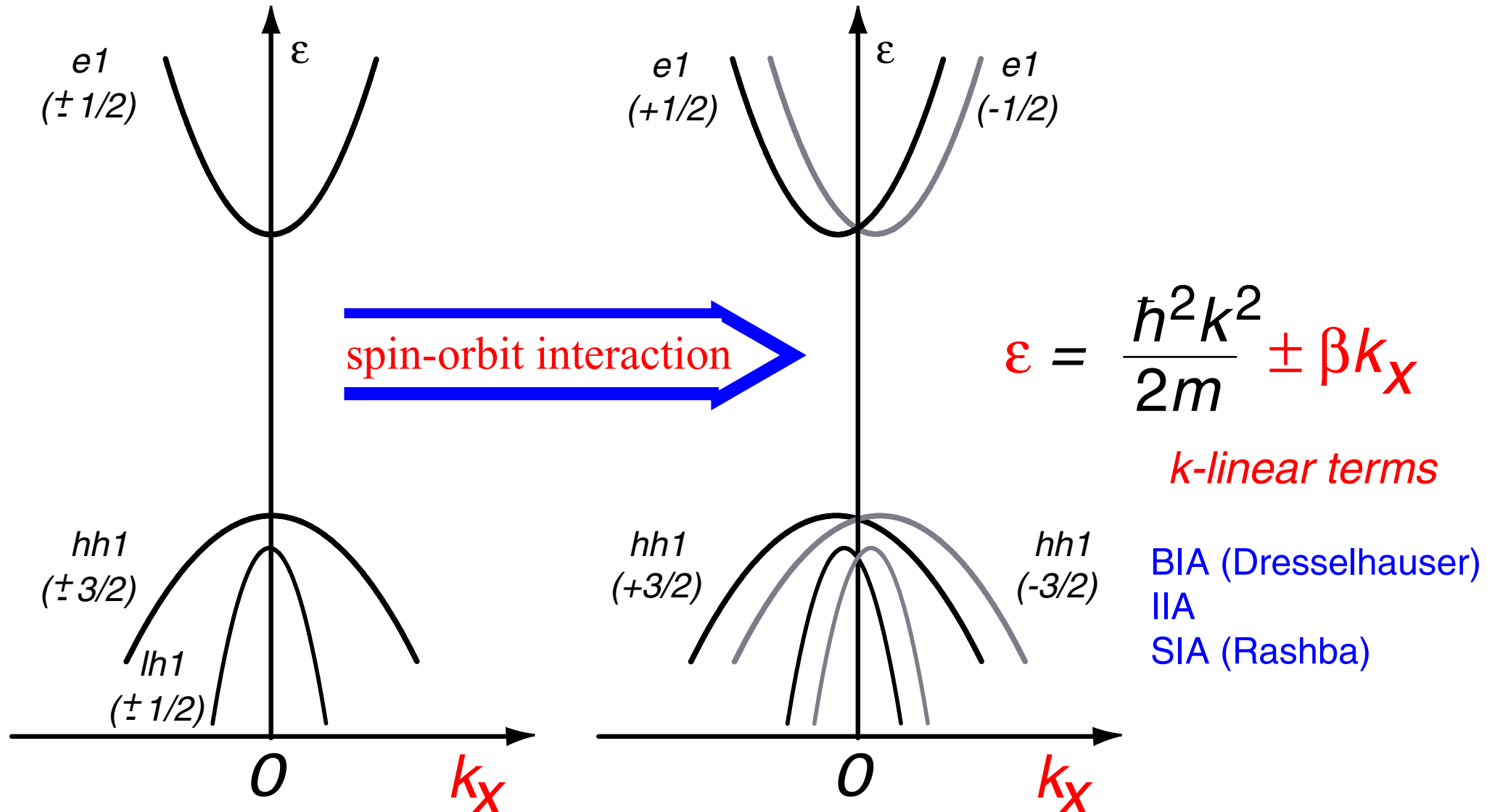


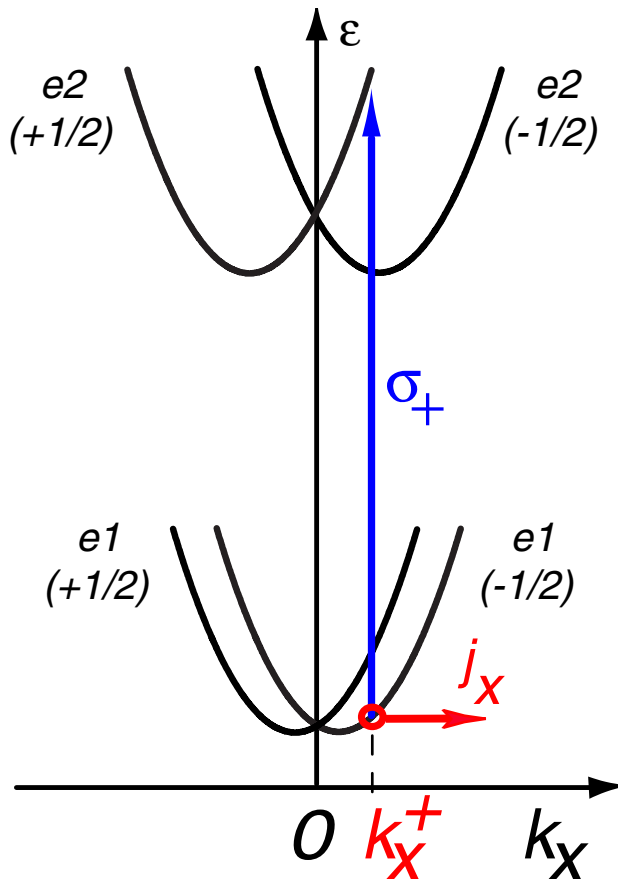
# Microscopic model: *k*-linear terms in the Hamiltonian



# Microscopic model: direct transitions

$$j \propto W(\varepsilon) v(k_x^-) (\tau_{pi} - \tau_{pf})$$

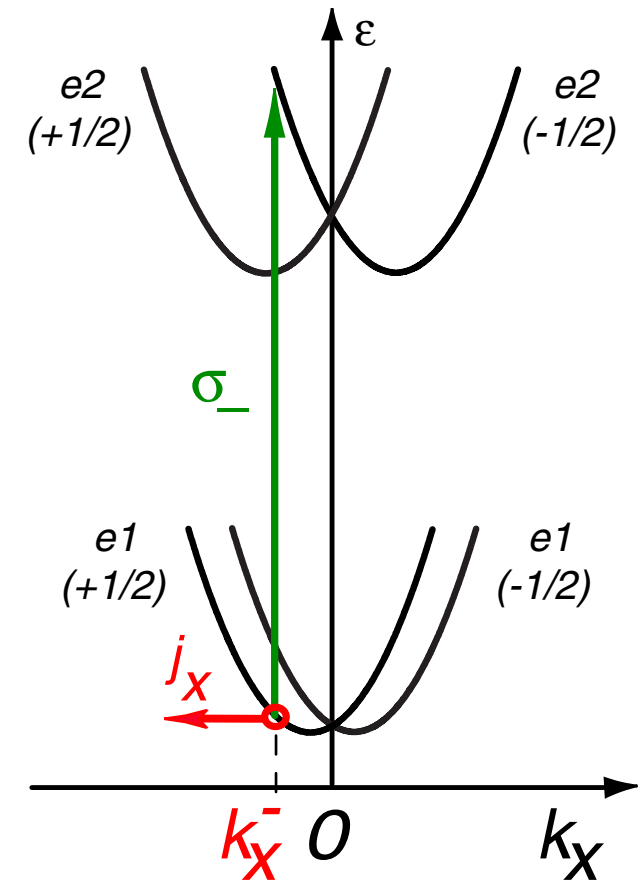
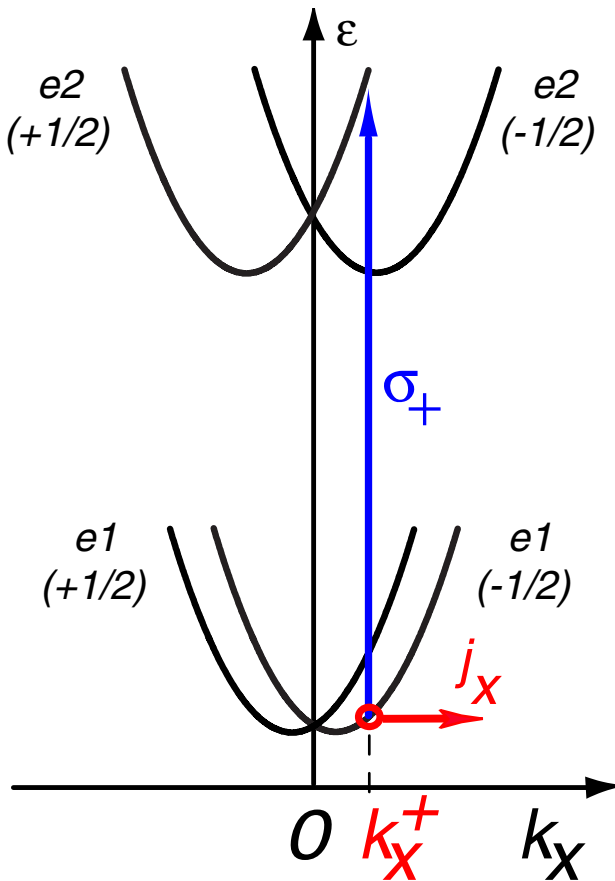
$$\hbar\omega > \hbar\omega_{LO} \rightarrow \tau_{pi} \gg \tau_{pf}$$



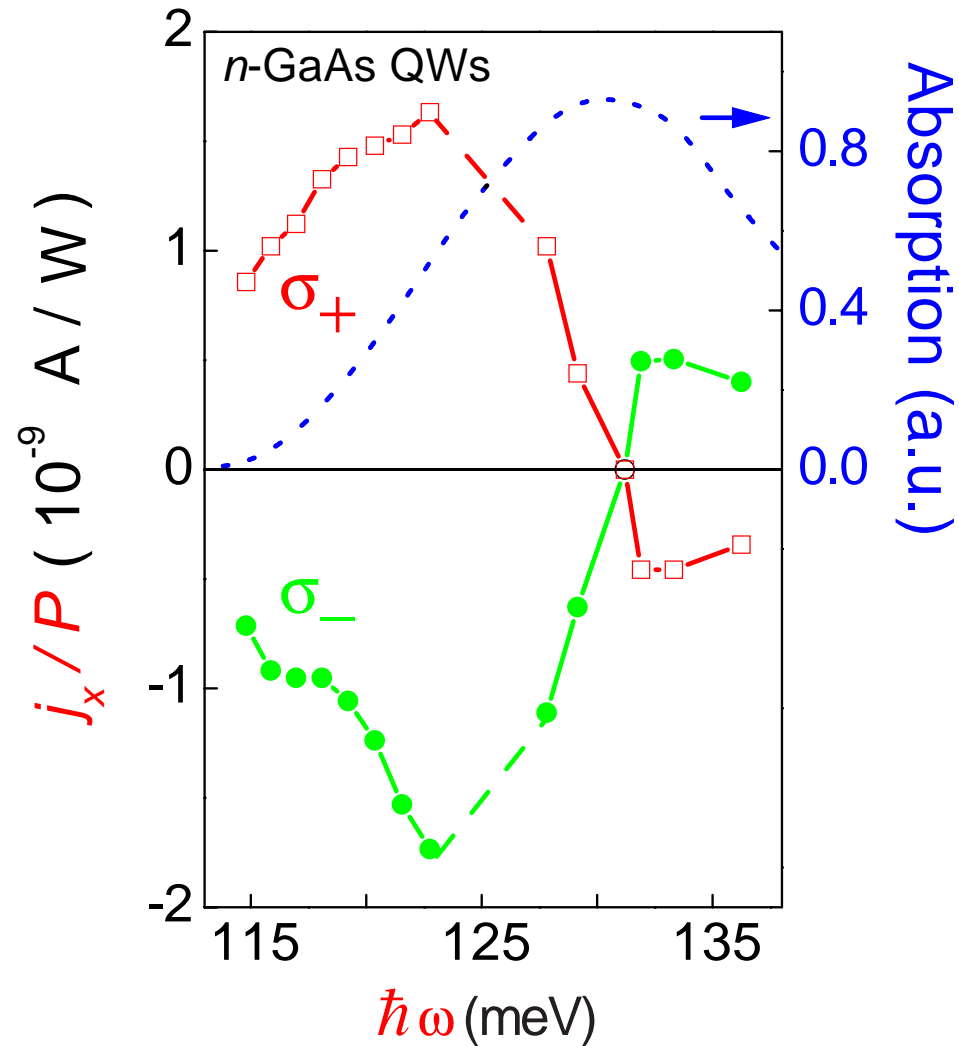
# Microscopic model: direct transitions

$$j \propto W(\epsilon) v(k_x^-) (\tau_{pi} - \tau_{pf})$$

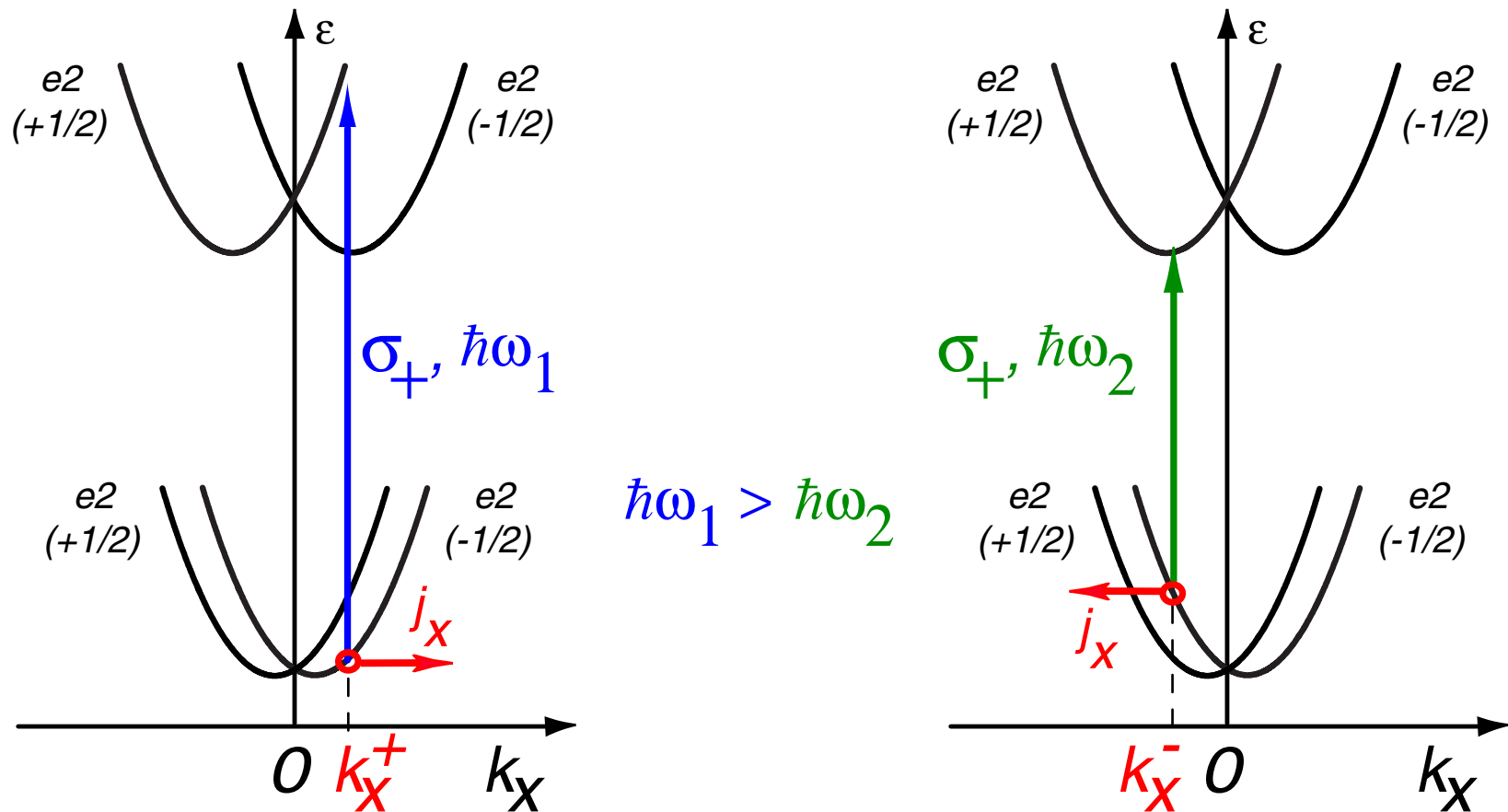
$$\hbar\omega > \hbar\omega_{LO} \rightarrow \tau_{pi} \gg \tau_{pf}$$



# Experiment: $e1-e2$ direct transitions

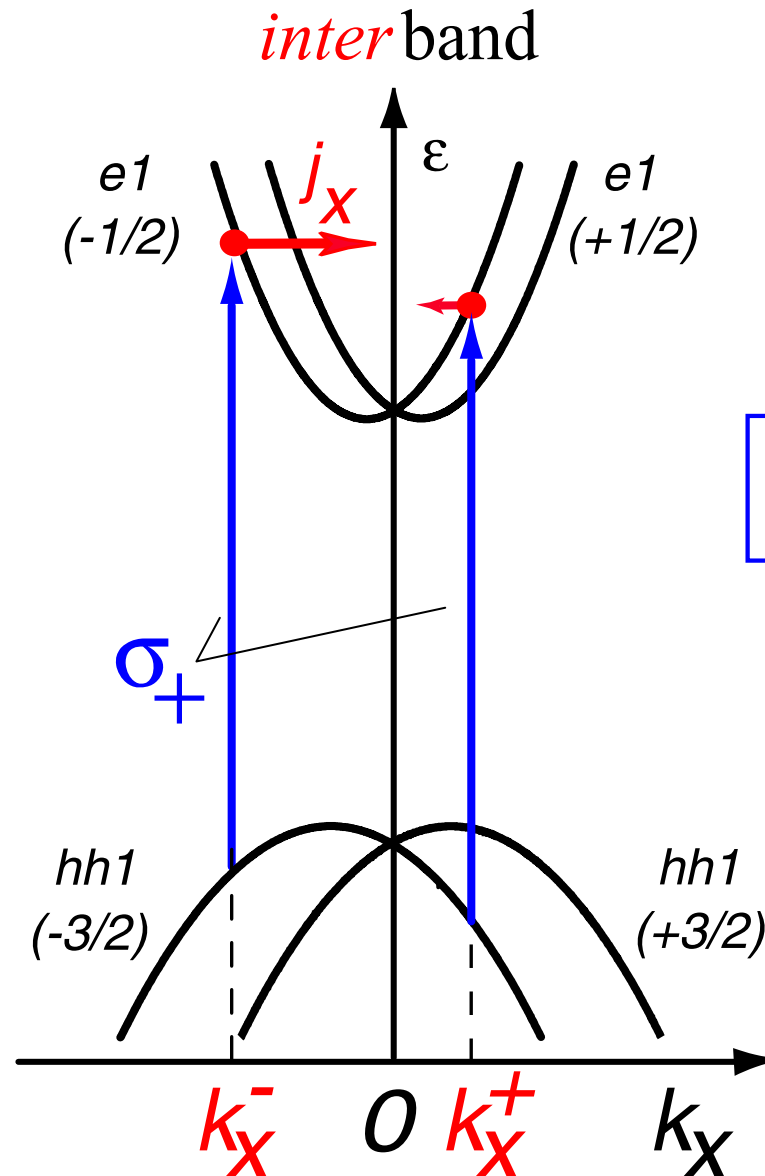


# Resonant inversion of the CPGE



$$j_x(\text{CPGE}) \propto (\tau_{p1} - \tau_{p2}) \frac{d\eta_{21}(\hbar\omega)}{d\hbar\omega} \frac{IP_c}{\hbar\omega}$$

# Microscopic model: direct transitions

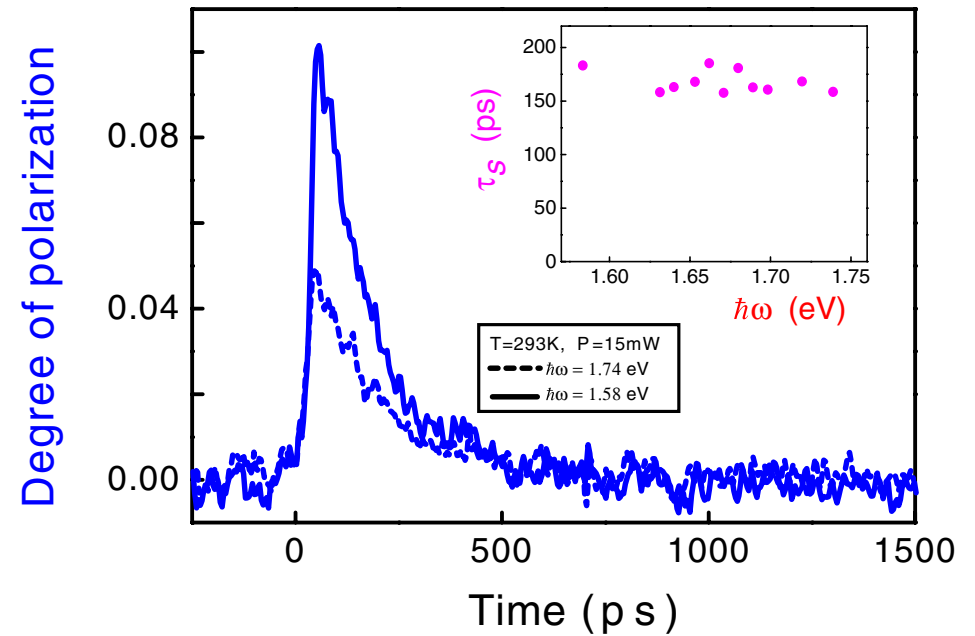
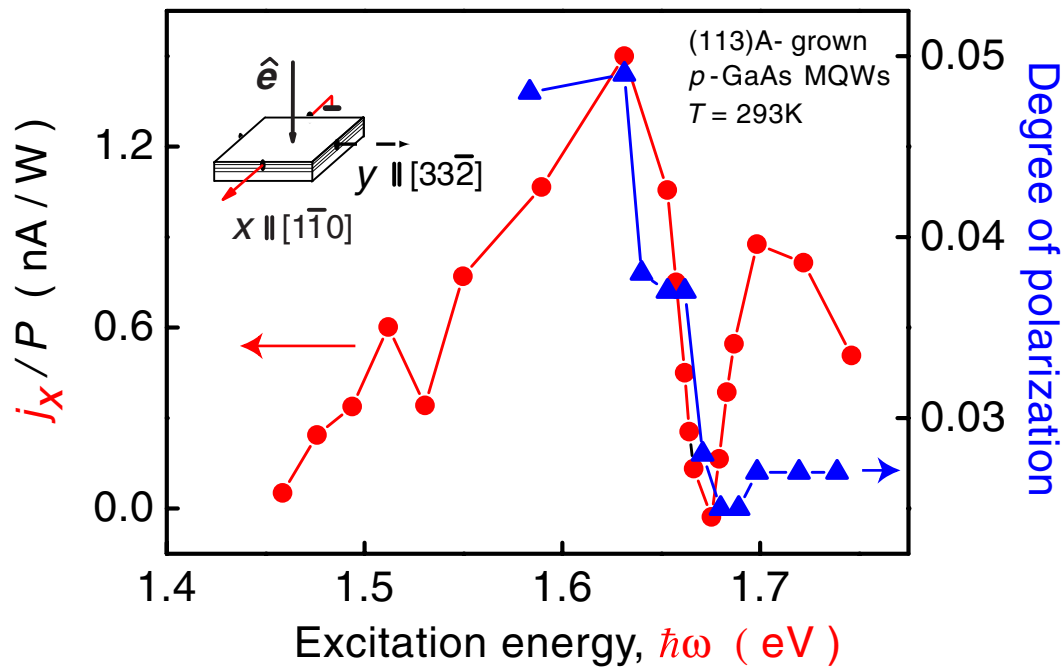


$$j \propto W(\epsilon) v(k) \tau_p(\epsilon)$$

# Direct interband transitions

Regensburg group (S.Ganichev) & Hannover group (M.Oesstreich),  
solid state comm. (2003)

M. Sakaki, Y.Ohno, H.Ohno, ICPC-2004



# Phenomenological description of PGE I

Fourier amplitudes:  $j_i(\omega)$ ,  $E_j(\omega)$

$$\begin{aligned} j(0) &= \sigma_{ij} E_j(0) \quad \text{Ohm's law} \\ &+ \alpha_{ijkl} E_j(0) E_k(\omega) E_l^*(\omega) \quad \text{Photoconductivity} \\ &+ \lambda_{ijk} E_j(\omega) E_k^*(\omega) \quad \text{Photogalvanic effect (PGE)} \end{aligned}$$

$$E_j(0) = 0 \quad \Rightarrow \quad j(0) = \lambda_{ijk} E_j(\omega) E_k^*(\omega)$$

see for review:

E.L. Ivchenko, G.E. Pikus, *Superlattices and Other Heterostructures. Symmetry and Optical Phenomena*, (second edition, Springer, Berlin 1999) □  
B.I. Sturman, V.M. Fridkin, *The Photovoltaic and Photorefractive Effects in Non-Centrosymmetric Materials*, □  
Gordon and Breach Science Publishers, New York, 1992.



# Phenomenological description of PGE II

Photogalvanic effect (PGE):

$$j_i \text{ (PGE)} = \alpha_{ijl} e_j e_l^* = \underbrace{\chi_{ijl} [e_j e_l^* + e_l e_j^*]}_{\substack{\text{Linear PGE} \\ \text{(symmetric part)}}} / 2 + \underbrace{\gamma_{ij} i (\mathbf{e} \times \mathbf{e}^*)_j}_{\substack{\text{Circular PGE} \\ \text{(anti-symmetric part)}}$$

$\chi_{ijl}$  - third rank *piezoelectric* tensor

$\gamma_{ij}$  - second rank *gyration* pseudo-tensor

$$j_i \text{ (CPGE)} = \gamma_{ij} i (\mathbf{e} \times \mathbf{e}^*)_j \propto E_0^2 P_{\text{circ}} = E_0^2 \sin 2\varphi$$

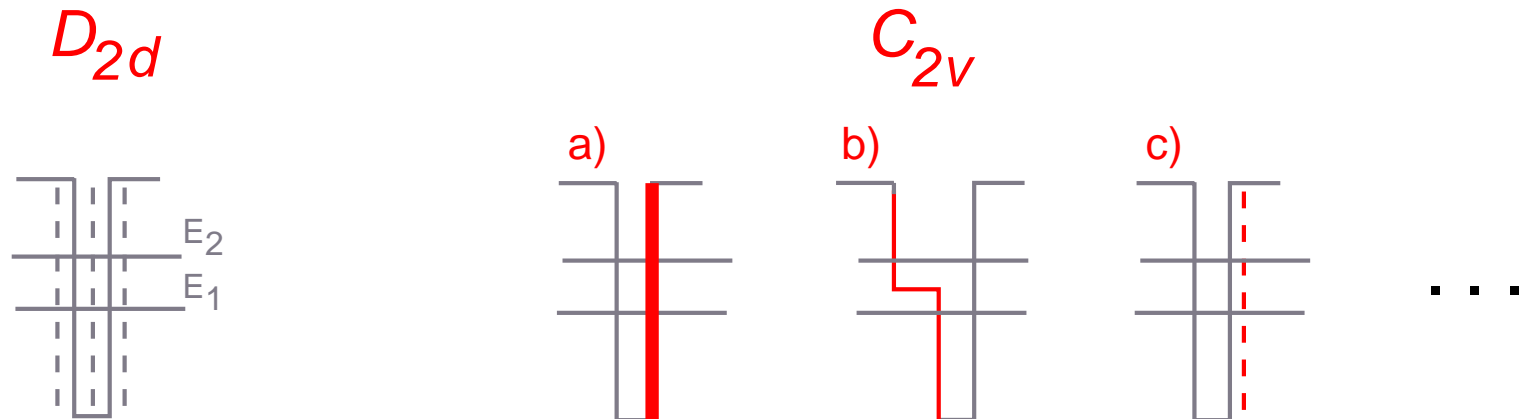
at first theoretically considered by: Ivchenko&Pikus □

and, independently, by Belinicher&Sturman □

observed in a bulk tellurium by V.M. Asnin, A.A. Bakun, A.M. Danishevskii, and A.A. Rogachev,

# Symmetry:

- Bulk GaAs, InAs etc.: point group  $T_d$ 
  - inversion asymmetric, but *non-gyrotropic*
  - no CPGE ( linear photogalvanic effect only )
- (001) - oriented QWs: point group  $D_{2d}$  or  $C_{2v}$ 
  - CPGE -- only at oblique incidence

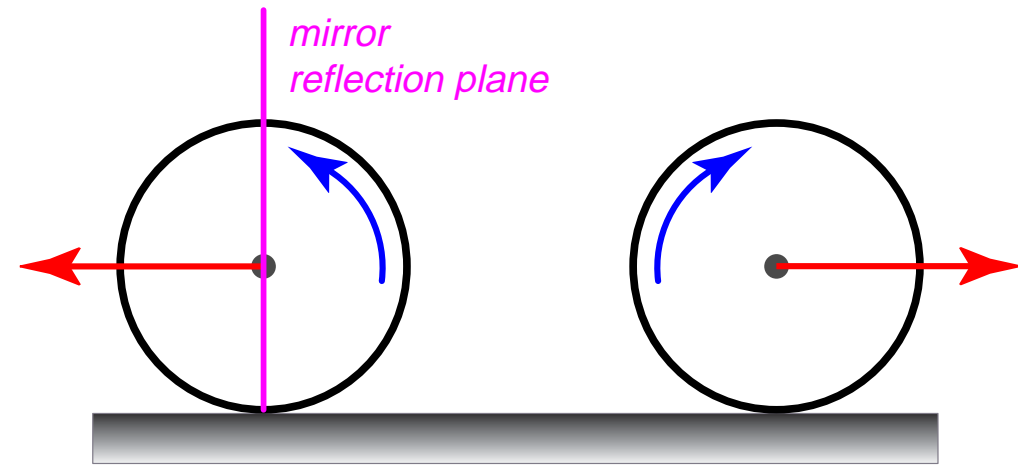


- (113) - oriented QWs: point group  $C_s$ 
  - CPGE at normal and at oblique incidence

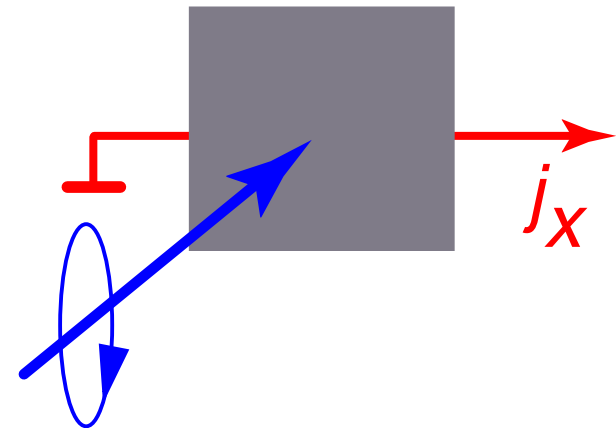
# Mechanical analogues of the CPGE

transversal - wheel

longitudinal - propeller



angular momentum of circ. pol. photons  $\Rightarrow$  directed motion of carriers



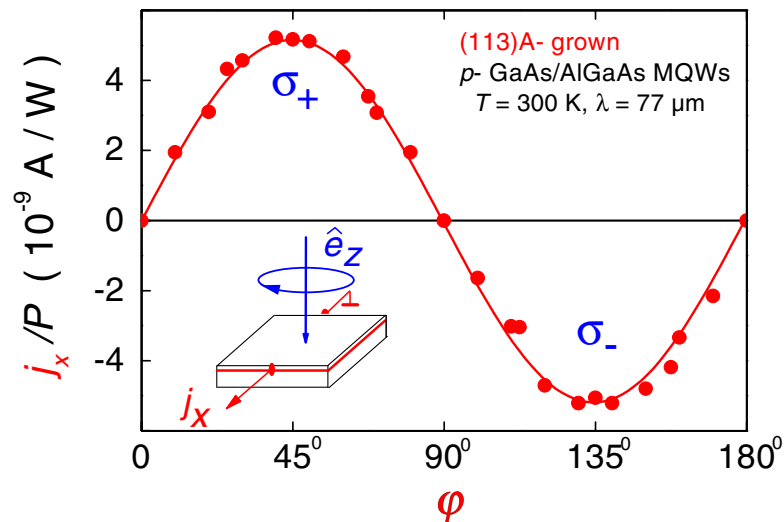
# Helicity dependent current

$C_s$  symmetry

(113)A or miscut - grown QWs

$$j_x = (\gamma_{xy} \hat{e}_y + \gamma_{xz} \hat{e}_z) E_0^2 \sin 2\varphi$$

CPGE current occurs normal to the mirror reflection plane!



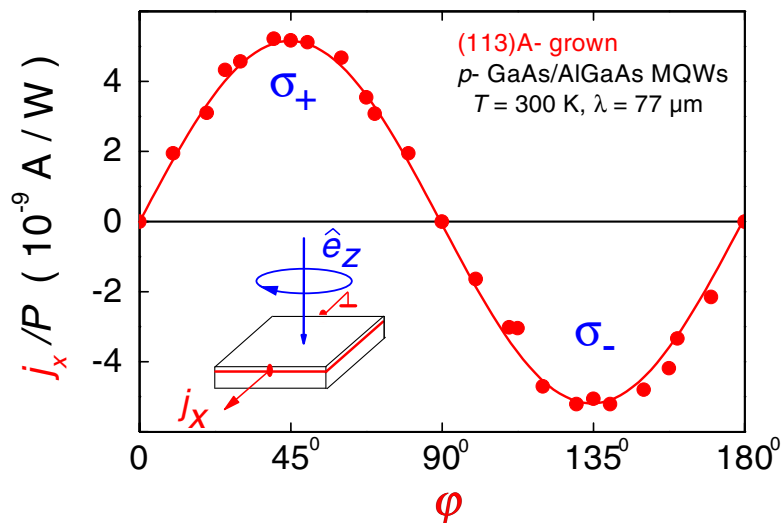
# Helicity dependent current

$C_s$  symmetry

(113)A or miscut - grown QWs

$$j_x = (\gamma_{xy} \hat{e}_y + \gamma_{xz} \hat{e}_z) E_0^2 \sin 2\phi$$

CPGE current occurs normal to the mirror reflection plane!

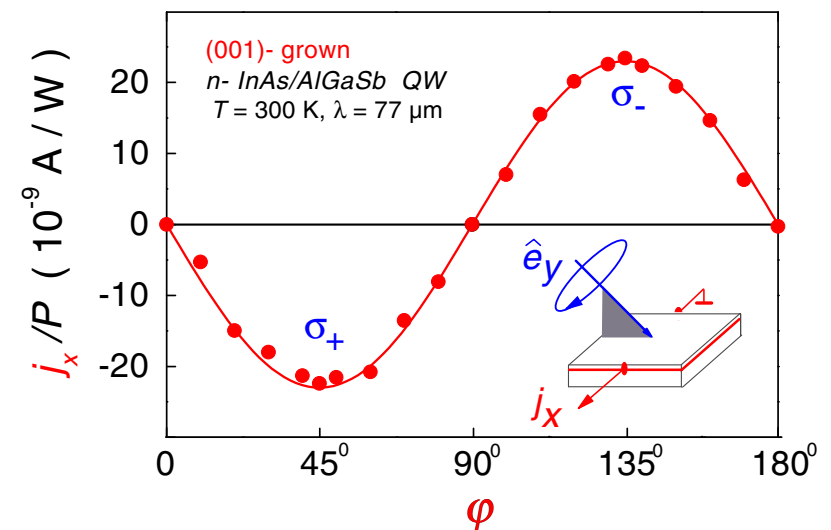


$D_{2d}$  or  $C_{2v}$  symmetry

in (001) - grown QWs,  $\hat{e}_y \parallel [110]$

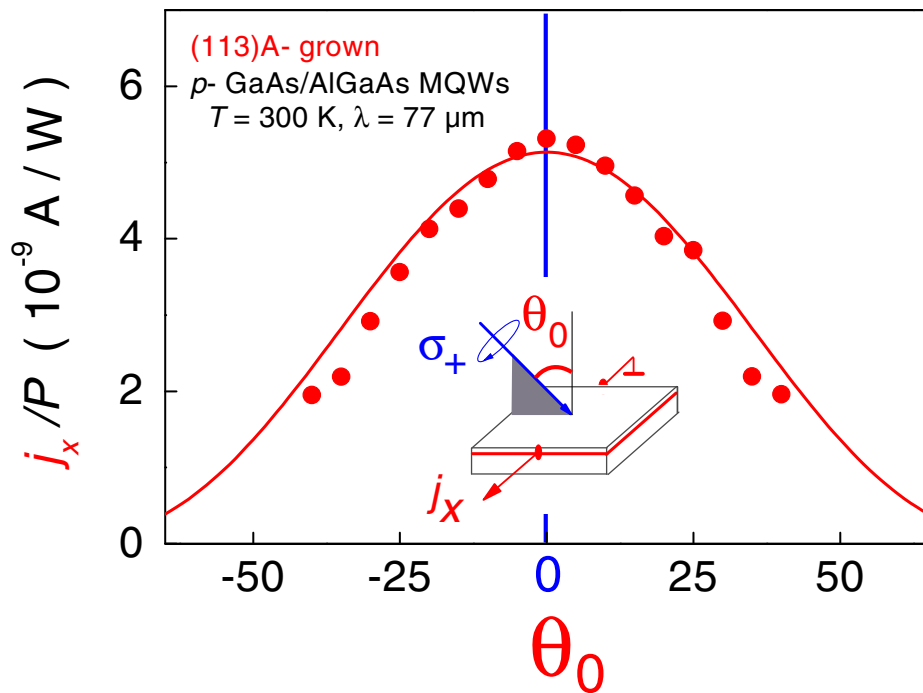
$$j_x = \gamma_{xy} \hat{e}_y E_0^2 \sin 2\phi$$

CPGE current occurs under oblique excitation only!

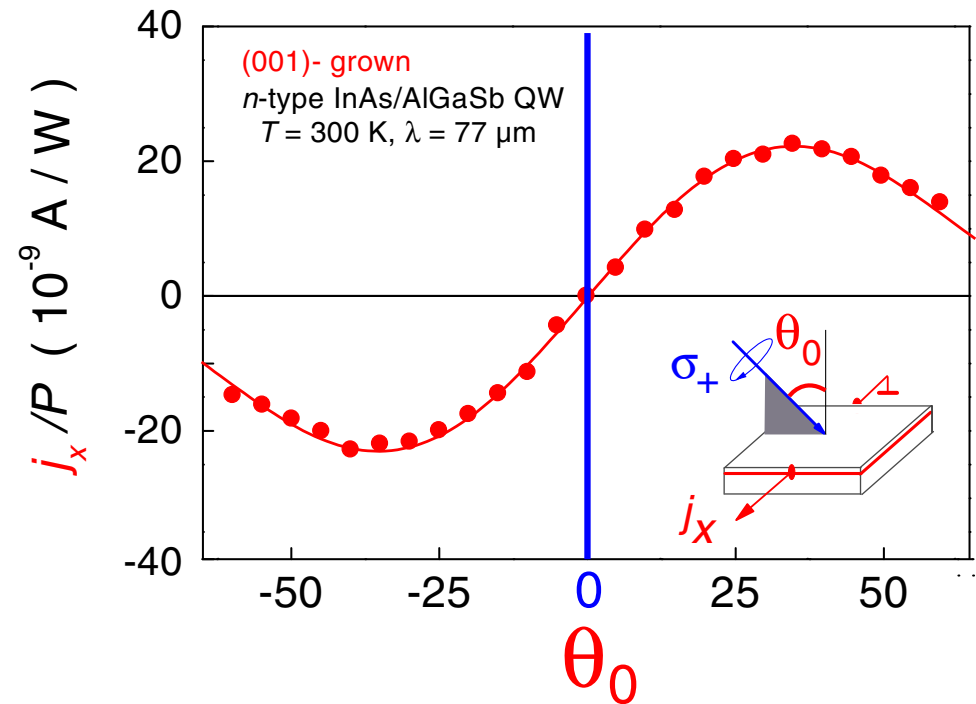


# Normal and Oblique Incidence

$C_S$  symmetry

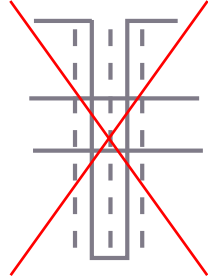


$C_{2v}$  symmetry



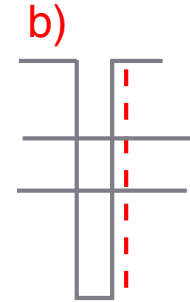
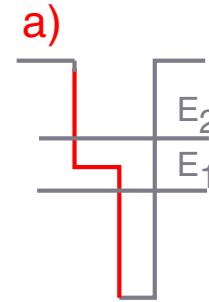
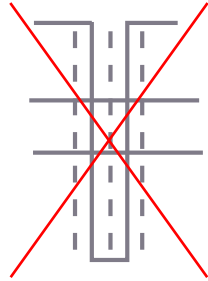
$\theta_0$  - angle of incidence

# Si:Ge quantum wells



symmetric Si:Ge QWs  
do not show CPGE.

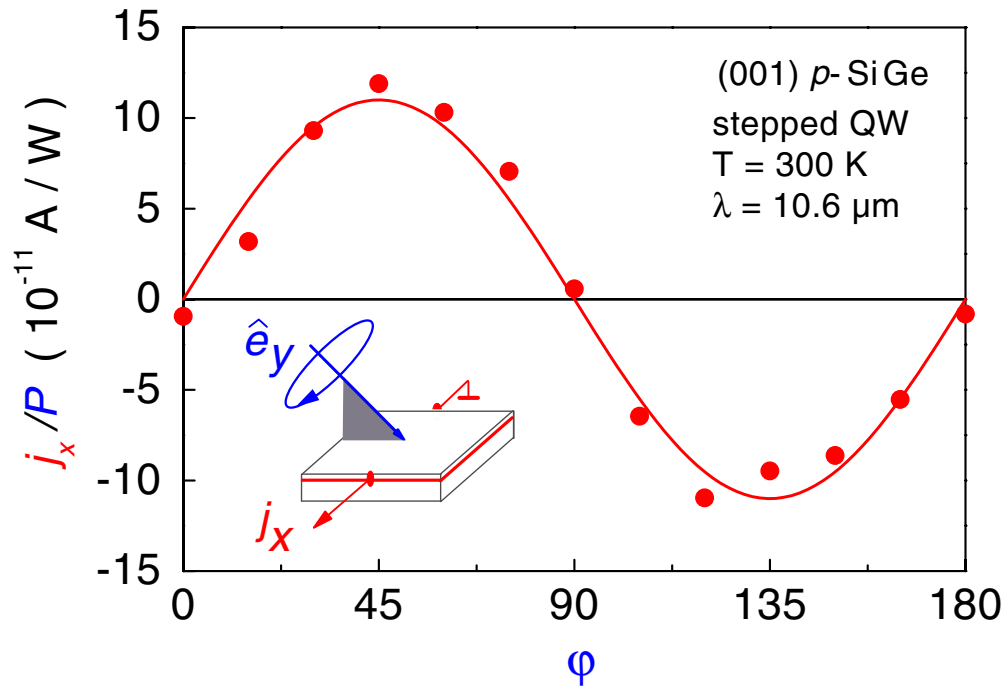
# Si:Ge quantum wells



symmetric Si:Ge QWs  
do not show CPGE.



asymmetric Si:Ge QWs !





# Spin-galvanic effect

$$j_{\alpha} = \sum_{\beta} Q_{\alpha\beta} S_{\beta}$$

*current*

*averaged spin*

e.g. for  $C_{2v}$ -symmetry and  $x \parallel [1\bar{1}0]$ :  $Q_{xy}, Q_{yx}$  are non-zero:

$$j_x = Q_{xy} S_y$$



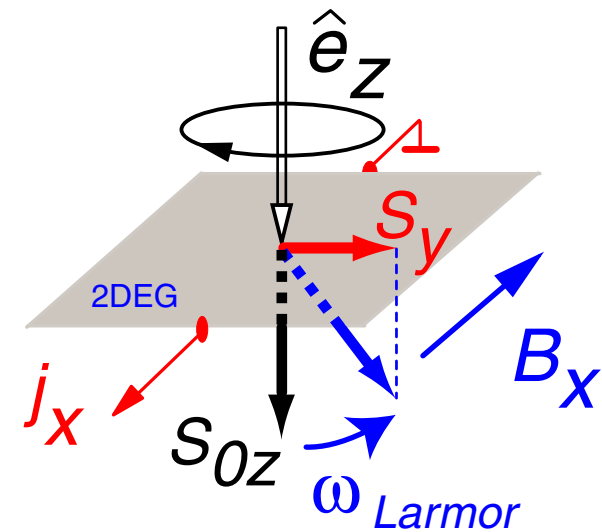
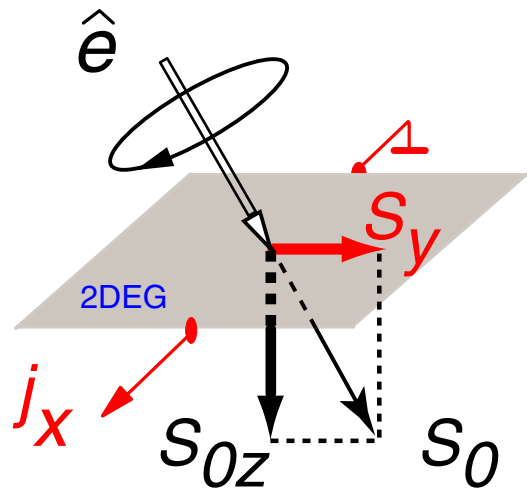
# Spin-galvanic effect

$$j_{\alpha} = \sum_{\beta} Q_{\alpha\beta} S_{\beta}$$

*current*                      *averaged spin*

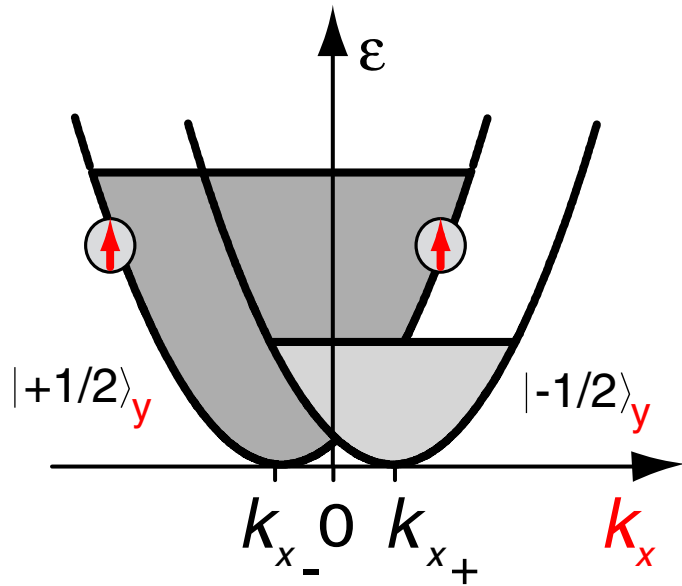
e.g. for  $C_{2V}$ -symmetry and  $x \parallel [1\bar{1}0]$ :  $Q_{xy}, Q_{yx}$  are non-zero:

$$j_x = Q_{xy} S_y$$



# Microscopic model

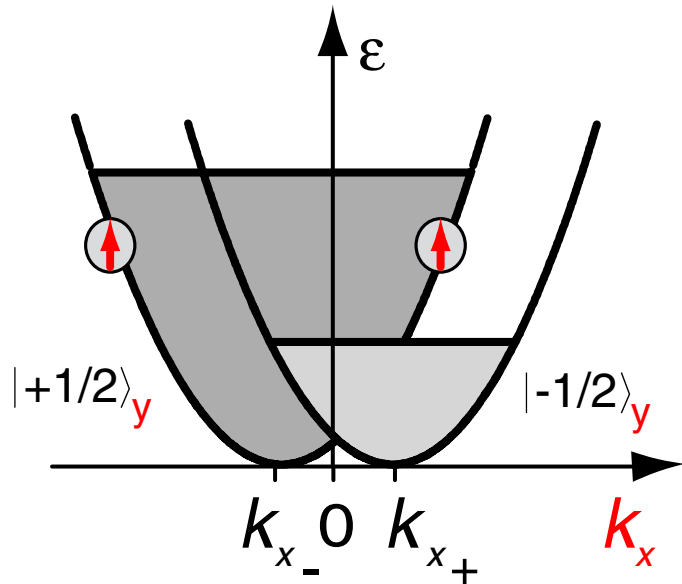
$$j_x = Q_{xy} S_y$$



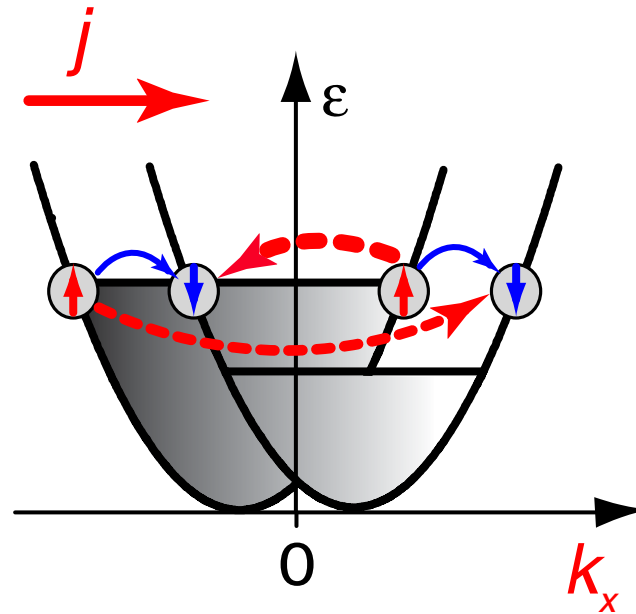
spin orientation

# Microscopic model

$$j_x = Q_{xy} S_y$$



spin orientation

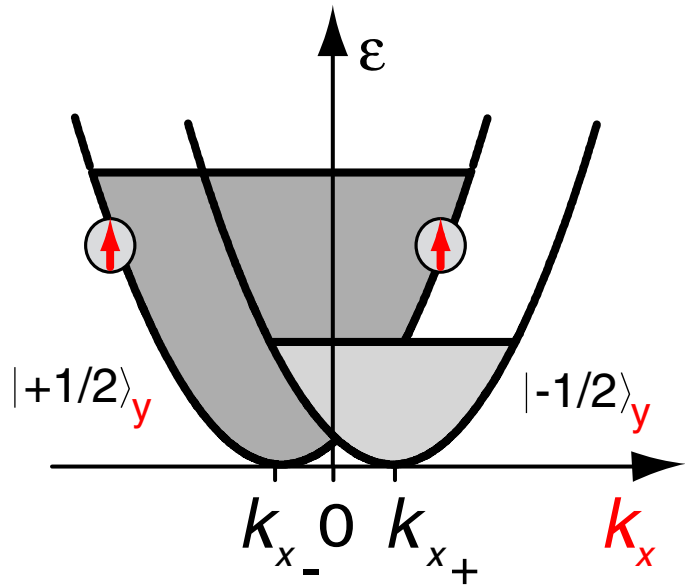


$k$ -dependent  
spin-flip scattering

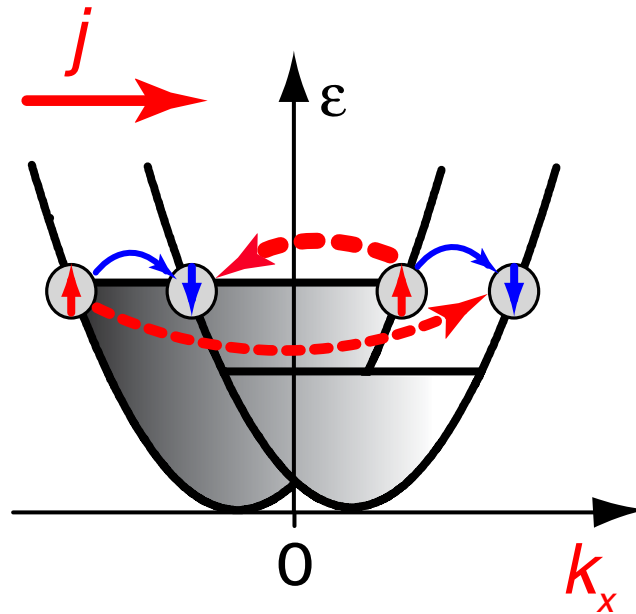
$$[v(k_{xf} - k_{xi})]^2 (k_{xf} + k_{xi})^2$$

# Microscopic model

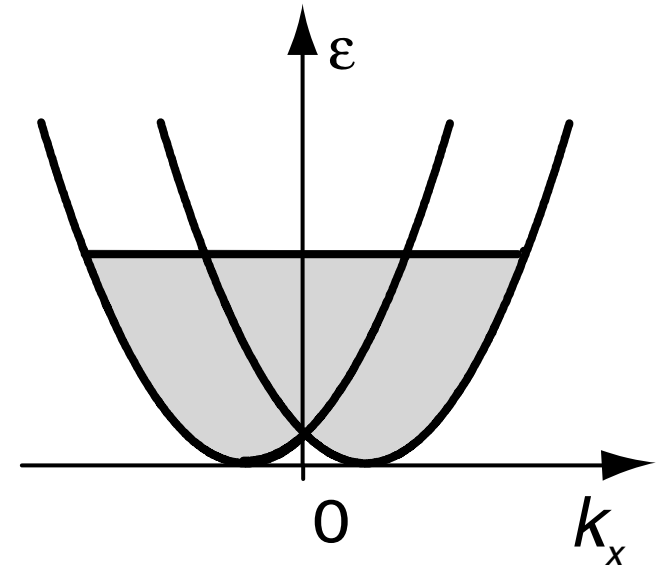
$$j_x = Q_{xy} S_y$$



spin orientation



$k$ -dependent  
spin-flip scattering



equilibrium

$$[v(k_{xf} - k_{xi})]^2 (k_{xf} + k_{xi})^2$$