

All-electrical measurements of direct spin Hall effect in GaAs with Esaki diode electrodesM. Ehlert,¹ C. Song,^{1,2} M. Ciorga,^{1,*} M. Utz,¹ D. Schuh,¹ D. Bougeard,¹ and D. Weiss¹¹*Institute of Experimental and Applied Physics, University of Regensburg, D-93040 Regensburg, Germany*²*Laboratory of Advanced Materials, Department of Material Science & Engineering, Tsinghua University, Beijing 100084, China*

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We report on measurements of direct spin Hall effect in a lightly n -doped GaAs channel with conductivity below $2000 \Omega^{-1} \text{ m}^{-1}$. As spin detecting contacts, we employed highly efficient ferromagnetic Fe/(Ga,Mn)As/GaAs Esaki diode structures. We investigate bias and temperature dependence of the measured spin Hall signal and evaluate the value of total spin Hall conductivity and its dependence on channel conductivity and temperature. From the results, we determine skew scattering and side-jump contribution to the total spin Hall conductivity and compare it with the results of experiments on higher conductive n -GaAs channels [Garlid, Hu, Chan, Palmström, and Crowell, *Phys. Rev. Lett.* **105**, 156602 (2010)]. As a result, we conclude that both skewness and side jump contribution cannot be treated as fully independent of the conductivity of the channel.

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I. INTRODUCTION

The spin Hall effect (SHE),¹ predicted in 1971,² has grown to become the subject of intensive theoretical^{3–6} and experimental^{7–12} studies over the last decade, as one of the phenomena exploiting the electron spin degree of freedom.¹³ The origin of the effect is coupling of spin and charge currents due to spin-orbit interaction in a given material. Although electrical in nature, it was initially observed optically^{7,8} and fully electrical measurements of a direct SHE were performed only very recently.¹⁰

In this paper, we describe the results of the measurements of direct SHE in lightly n -doped GaAs channels, with spin accumulation detected by probes containing (Ga,Mn)As/GaAs Esaki diode structures.¹⁴ The relatively high detection efficiency of the latter^{15,16} allows for effective measurement of low-level polarizations generated by SHE. The geometry of the measurements is similar to the one in Ref. 10. The charge current j_x flows along the channel with conductivity σ_{xx} . As a result of spin-orbit interaction, the scattering at impurities is spin-dependent leading to deflection of carriers with opposite spins into opposite directions, transverse to the driven charge current. This gives rise to the spin current j_s in the direction perpendicular to j_x with spins partially polarized in a direction perpendicular to the plane formed by j_x and j_s . The generated spin current leads then to the spin accumulation at the edges of the channel, which is probed by, placed above the channel, ferromagnetic voltage probes with (Ga,Mn)As/GaAs Esaki diode structures. Due to spin-charge coupling occurring in ferromagnetic materials,¹⁷ the spin accumulation in the channel leads to a voltage drop across the contact that can be experimentally measured.¹⁸ From the measurements, we extracted the value of spin Hall conductivity σ_{SH} , defined as $\sigma_{SH} = j_s/E_x$, where E_x is the electric field along the channel. We investigated also its dependence on the conductivity of the channel as well as on the temperature. From these dependencies, we were able to determine the contribution from skew scattering and side jump and compare it to both theoretical predictions⁵ and previous experimental results.¹⁰ In contrast to experiments by Garlid *et al.*,¹⁰ we focused our studies on n -GaAs layers with relatively low carrier concentration ($n \approx 2 \times 10^{16} \text{ cm}^{-3}$) and subsequent low

channel conductivities. These two experiments complement therefore each other in terms of the investigated range of channel conductivity values.

II. EXPERIMENTAL

Experimental devices were fabricated from a single wafer grown by molecular-beam epitaxy (MBE) on (001) GaAs substrates. This is one of the wafers used also for spin injection experiments described in Ref. 16. The wafer consists of a 1000-nm-thick n -type transport channel ($n \approx 2 \times 10^{16} \text{ cm}^{-3}$, as extracted from magnetotransport measurements), a 15-nm-thin $n \rightarrow n^+$ GaAs transition layer ($n^+ = 5 \times 10^{18} \text{ cm}^{-3}$), 8-nm n^+ -GaAs, and 2.2-nm low-temperature (LT)-grown $\text{Al}_{0.36}\text{Ga}_{0.64}\text{As}$, serving as a diffusion barrier, followed by LT-grown 15-nm-thick layer of $\text{Ga}_{0.95}\text{Mn}_{0.05}\text{As}$. The highly doped (Ga,Mn)As/GaAs pn -junction forms an Esaki diode.^{14,15} In the next step, the wafers were transferred, without breaking vacuum, into an attached metal-MBE chamber, where 2 nm [14 monolayers (MLs)] of Fe were epitaxially grown at room temperature, and finally covered by 4 nm (20 MLs) of Au.

The Hall bar devices were defined by optical lithography, chemically assisted ion beam etching and wet etching. Electron beam lithography was used to pattern the Fe/(Ga,Mn)As spin detecting contacts, oriented along the [110] direction, i.e., the easy axis of Fe. The top Fe layer made the contacts magnetically harder, thus assuring that the magnetization stayed aligned along the long axis of the contacts during Hanle measurements described in the next paragraph. After defining the contacts, top layers were etched away to confine the transport to the low-doped n -GaAs channel. A picture of one of the devices and the geometry used in experiments is shown in Fig. 1(a). A pair of 2.5- μm -wide spin probes is placed at Hall crosses, with a distance L from the edge of the bar. The experiments were performed on devices with $L = 5.25, 8.25, \text{ and } 11.25 \mu\text{m}$, measured from the center of the contact. Spin-detecting contacts are connected to big bonding pads via Ti/Au paths, which are isolated from the conducting channel by a 50-nm-thick layer of Al_2O_3 , deposited by atomic layer deposition (ALD). In the transport experiments, the current j_x is passed along the channel characterized by conductivity σ_{xx} .

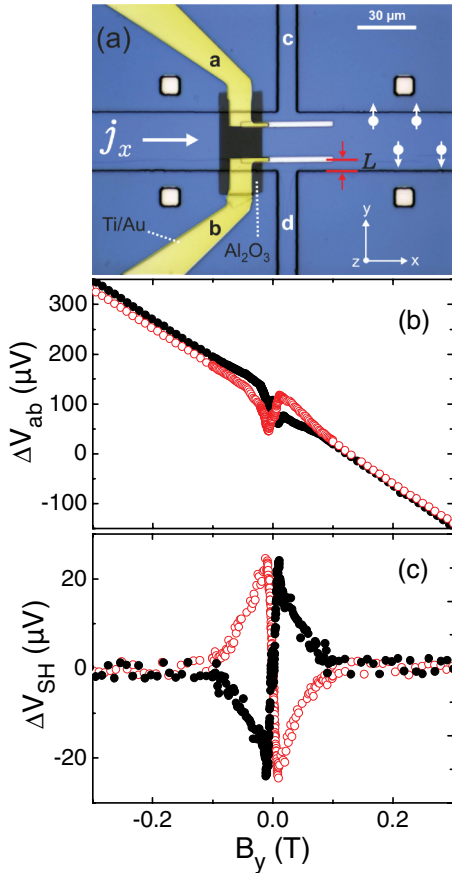


FIG. 1. (Color online) (a) Micrograph of a spin Hall device with experimental layout. A pair of ferromagnetic contacts (*a* and *b*) is placed at the Hall cross at a distance L from the channel edges. Voltage V_{ab} and Hall voltage V_{cd} is measured as a function of in-plane field \mathbf{B}_y , in the presence of charge current j_x . (b) V_{ab} as a function of \mathbf{B}_y for $j_x = 1.7 \times 10^3 \text{ A/cm}^2$ for initial orientation of magnetizations along $+x$ (solid black symbols) and $-x$ (open red symbols) directions. (c) Spin Hall voltage V_{SH} vs \mathbf{B}_y for the same current amplitude for both positive (solid black symbols) and negative (open red symbols) current directions after removing the background as described in the text.

Ferromagnetic Esaki diodes of $100 \mu\text{m} \times 100 \mu\text{m}$ size are also used as charge current leads, but placing them $\sim 200 \mu\text{m}$ from the nearest pair of spin Hall probes assures that the charge current flowing underneath the probes is fully unpolarized. Due to SHE, the carriers with opposite spins are accumulated at opposite edges of the channel, which can be described by spin accumulation μ_s . As a result of spin-charge coupling, this spin accumulation gives rise to a voltage^{17,18} $V(L) = -P\mu_s(L)$, where P is spin injection efficiency of the employed contact and $\mu_s(L)$ is a value of the spin accumulation directly underneath the contact placed at a distance L from the edge of the sample. The feasibility of a scheme employing structures described above for studying of spin dependent phenomena has been demonstrated in nonlocal spin injection experiments described in Ref. 16. Based on those measurements, we estimated the value of $P \approx 0.5$. Additionally, we performed similar measurements (not shown here) on the current devices using each of the ferromagnetic contacts as a detector of spin accumulation generated by electrical spin injection at

the other contact from the pair. Although that configuration was not optimal for a spin injection experiment and could not be used for quantitative analysis, it clearly demonstrated sensitivity of contacts to the polarized spins accumulated underneath. As spin accumulation at opposite edges of the channel has opposite spin orientation, the voltage between both contacts V_{SH} can be written as $|V_{SH}(L)| = 2P\mu_s(L)$, assuming the same spin injection efficiency for both contacts. During measurements, we were also monitoring the voltage V_{cd} resulting from the ordinary Hall effect, as this produced background to the spin Hall signal.

III. RESULTS AND DISCUSSION

Ferromagnetic electrodes can measure only spin components parallel to their own magnetization axis, which for our structure lies in the plane of the sample. As the SHE-induced spin polarization is aligned along the z direction, we apply external magnetic field \mathbf{B}_y to induce precession of the spins in xz plane due to Hanle effect. As a result of the precession, spins acquire an in-plane component that can be detected by spin-dependent contacts. Typical results of measurements are shown in Fig. 1(b) where we plot the voltage V_{ab} measured between a pair of contacts in the applied external magnetic field \mathbf{B}_y . The following procedure was applied to obtain the shown curves. First, a magnetic field \mathbf{B}_x was swept to the saturation value of 0.5 T and back to zero to align the magnetization along the contacts in $+x$ direction. Then, the sample was rotated in-plane by 90° and the field \mathbf{B}_y was swept from zero to 0.5 T to induce precession of the out-of plane spin component. The procedure was then repeated with \mathbf{B}_y swept from zero to -0.5 T. Although the raw curves, shown in Fig. 1(b), contain contributions from different backgrounds, they clearly show the features expected from a spin-related signal, namely, antisymmetric behavior near $\mathbf{B}_y = 0$ T and opposite sign of the signal for magnetizations aligned along $+x$ and $-x$ direction. To be able to fit the data using standard Hanle equations,¹⁸ we had to remove the background contribution. First, we removed the background due to ordinary Hall effect by subtracting the Hall voltage V_{cd} from measured V_{ab} . The remaining background was removed by taking advantage of the expected symmetry of the spin Hall signal. This was done by subtracting the curves taken for two different parallel configurations (magnetized at $+x$ and $-x$) and subsequently removing the even components from the data as the expected signal should be odd in \mathbf{B}_y . The traces obtained after removing the background are depicted in Fig. 1(c). We plot the data for two opposite current directions, clearly showing that the sign of the signal is changed by reversal of current direction, which is fully consistent with the theory of SHE.

Figures 2(a)–2(c) show the curves for $j_x = 1.7 \times 10^3 \text{ A/cm}^2$ and $T = 4.2 \text{ K}$ obtained for different distances of contacts from the channel edge, after removing all contributing backgrounds. For fitting we used standard Hanle effect equations^{15,18} for the case of perpendicular relative orientation of spins (in our case originating from SHE) and spin detector. We took the final size of the contacts into account by integrating the signal over their width. From the fits, we obtained a spin relaxation time of $\tau_s = 3.5 \text{ ns}$ and $V_{SH}(0) = 83 \mu\text{V}$, where $V_{SH}(0)$ is the voltage corresponding to the

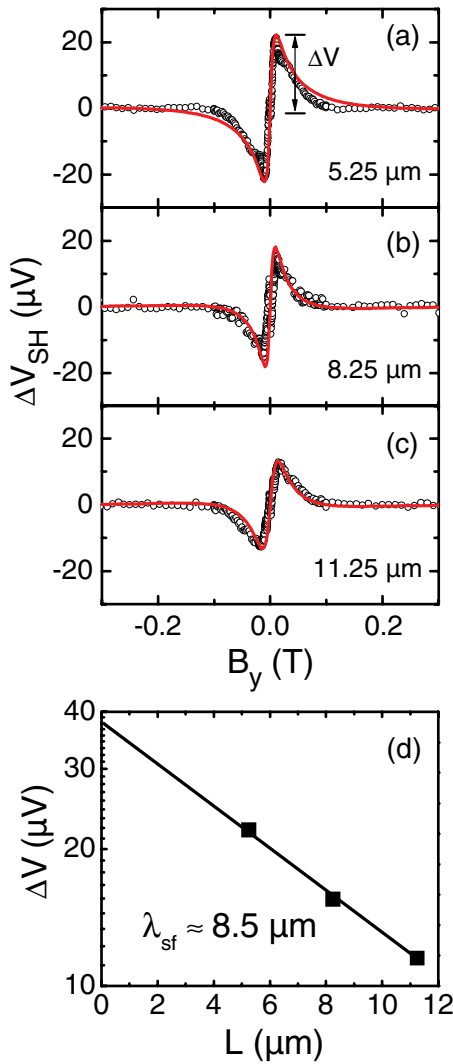


FIG. 2. (Color online) (a)–(c) Spin Hall voltage V_{SH} as a function of B_y at $T = 4.2$ K and for $j_x = 1.7 \times 10^3$ A/cm 2 for three different values of a distance between contact and the channel edge. Solid lines represent fits with the same set of parameters. (d) Magnitude of the spin Hall signal ΔV_{SH} vs distance between contact and the channel edge with the extracted value of the spin diffusion length λ_{sf} .

spin accumulation at the edges of the contact. The extracted value of τ_s is much smaller than expected for GaAs with such a doping level.¹³ The reason could be high electric field E_x in the channel (~ 120 V/cm for measurements shown in Fig. 2), which is expected to drastically decrease spin lifetime above the donor impact ionization threshold of ~ 10 V/cm.¹⁹ $V_{SH}(0)$ is directly related to the spin density polarization $P_n = (n^\uparrow - n^\downarrow)/(n^\uparrow + n^\downarrow)$ through the expression¹⁷

$$P_n = \frac{e V_{SH} g_n(E_F)}{2P n} = \frac{e V_{SH}}{2P} \frac{3m^*}{\hbar^2 (3\pi^2 n)^{2/3}}, \quad (1)$$

where $g_n(E_F)$ is the density of states at the Fermi energy and m^* is the effective mass of GaAs. From the measurements shown in Fig. 2, we obtain $P_n(0) = 3\%$ at the edges of the sample, which is roughly double the value of the spin polarization obtained for higher doped n -GaAs.¹⁰

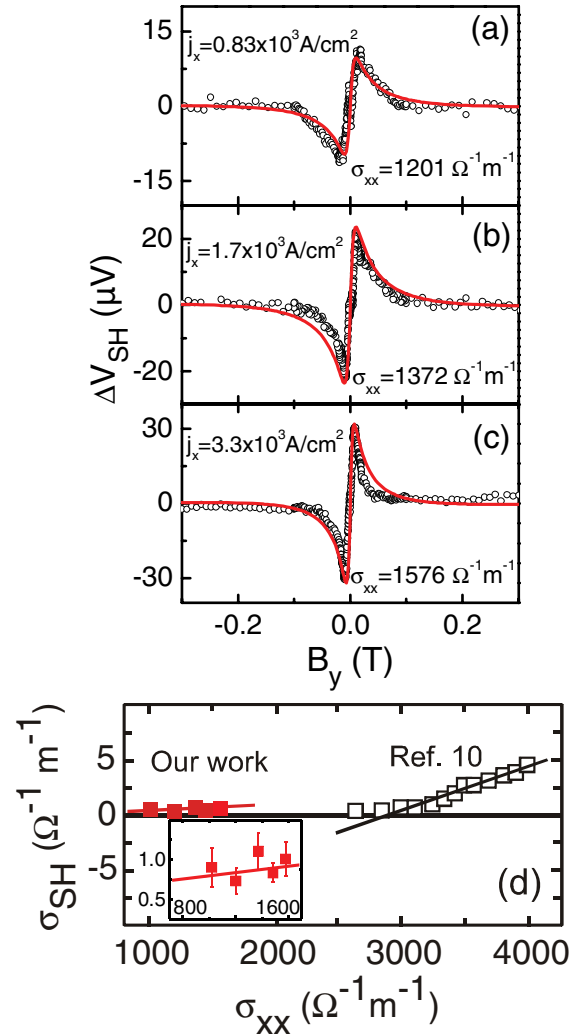


FIG. 3. (Color online) (a)–(c) Spin Hall voltage V_{SH} as a function of B_y at $T = 4.2$ K for three different channel current densities j_x corresponding to different conductivities σ_{xx} . We plot both experimental data (symbols) and corresponding fits (red line). (d) Dependence of the spin Hall conductivity on σ_{xx} extracted from our measurements at $T = 4.2$ K (full symbols) and taken from Ref. 10 (open symbols, $T = 30$ K). From the linear interpolation (solid line) with Eq. (3), we obtain the value of skewness parameter $\gamma = 4 \times 10^{-4}$ and side jump contribution $\sigma_{SJ} \approx 0.6 \Omega^{-1}\text{m}^{-1}$. From the linear fit shown for Ref. 10 data, one gets $\gamma = 4 \times 10^{-3}$ and $\sigma_{SJ} \approx -12 \Omega^{-1}\text{m}^{-1}$. (Inset) Zoom of our data.

Now we can move on to extracting the parameters related directly to SHE, namely, the magnitude of the spin Hall conductivity σ_{SH} and spin Hall angle $\alpha = \sigma_{SH}/\sigma_{xx}$. As mentioned before, a transverse spin current j_s is creating at the edges of the channel a spin accumulation $\mu_s(0) = j_s \lambda_{sf}/\sigma_{xx}$, which, via spin charge coupling, would lead to a voltage $|V_{SH}(0)| = 2P\mu_s(0)$ between lower and upper edges. Taking into account that $j_s = \sigma_{SH}E_x$ and $j = \sigma_{xx}E_x$, we derive

$$\sigma_{SH} = V_{SH}(0)\sigma_{xx}^2/2Pj\lambda_{sf}. \quad (2)$$

From our measurements, we obtained $V_{SH}(0) = 83 \mu\text{V}$ for $j = 1.7 \times 10^3$ A/cm 2 , $\lambda_{sf} = 8.5 \mu\text{m}$ [see Fig. 2(d)], and $\sigma_{xx} = 1370 \Omega^{-1}\text{m}^{-1}$. This finally gives $\sigma_{SH} \approx 1.1 \Omega^{-1}\text{m}^{-1}$

and $\alpha = 8 \times 10^{-4}$, i.e., values which are very consistent with other reports.^{5,10}

To analyze the obtained SHE signal in more details and to determine the contribution of side jump and skew scattering to the measured spin Hall conductivity, we performed bias dependence measurements for current densities in the range of $j = 3.3 \times 10^2 - 3.3 \times 10^3$ A/cm² at $T = 4.2$ K. In Figs. 3(a)–3(c), we show the spin Hall signal (symbols) for three different values of current density together with Hanle fits (solid lines) from which we can extract the spin Hall conductivity, in the way described above. Changing the current density tunes the value of the conductivity σ_{xx} in *n*-GaAs due to dependence of mobility on the electric field.^{10,20} This allows us to extract dependence of σ_{SH} on σ_{xx} , plotted in Fig. 3(d) as filled squares. According to Engel *et al.*,⁵ σ_{SH} can be approximated by

$$\sigma_{SH} \approx \frac{\gamma}{2}\sigma_{xx} + \sigma_{SJ}. \quad (3)$$

The first component in the above equation is due to skew scattering with γ being the so-called skewness parameter. The second component describes a side jump contribution. According to theory, it is independent on the conductivity of the channel⁵ and depends on density n and spin-orbit interaction parameter λ_{so} as

$$\sigma_{SJ} = -2ne^2\lambda_{so}/\hbar. \quad (4)$$

From a linear fit of our data with Eq. (3), we obtained the skewness parameter $\gamma \approx 4 \times 10^{-4}$ and the conductivity-independent side jump contribution $\sigma_{SJ} \approx 0.6 \Omega^{-1}\text{m}^{-1}$. The first value is a half of the value $\gamma \approx 1/900$ calculated in Ref. 5 and is approximately one order of magnitude smaller than the value obtained in Ref. 10. The value of the side jump contribution differs by $\sim 1 \Omega^{-1}\text{m}^{-1}$ from the one predicted by Eq. (4) (the fact that the experimental value has a positive sign is an artifact of linear extrapolation). This difference between theory and experiments is approximately one order of magnitude smaller than the one reported by Garlid *et al.*¹⁰ In order to make a more detailed comparison of our experimental results and the ones from Ref. 10, we plot in Fig. 3(d) also the dependence of the spin Hall conductivity on channel conductivity reported in that paper for $T = 30$ K (open symbols). One can see that the much higher values for skewness and side jump contribution, given in the latter, were extracted from spin Hall signals measured for conductivities larger than $\sim 3000 \Omega^{-1}\text{m}^{-1}$ (see the linear fit). In contrast, as a consequence of a lower doping, we performed measurements on channels with conductivities up to $\sim 1600 \Omega^{-1}\text{m}^{-1}$. Calculations of Engel *et al.*⁵ were performed for channels with parameters similar to our samples, which can explain why our results are closer to their theoretical predictions. One clearly sees, however, that data from Ref. 10 contain also values of σ_{SH} extracted for the conductivity range of ~ 2500 – $3000 \Omega^{-1}\text{m}^{-1}$. The corresponding data points deviate substantially from the extrapolated line from which γ and σ_{SJ} were extracted and are closer to our results. Our experiment provides then additional data points for channel conductivities below $2000 \Omega^{-1}\text{m}^{-1}$, which seem to fit well with data points for $\sigma_{xx} \approx 2500$ – $3000 \Omega^{-1}\text{m}^{-1}$ from Ref. 10. Both experiments complement each other well and together show that spin Hall conductivity can be well described by Eq. (3),

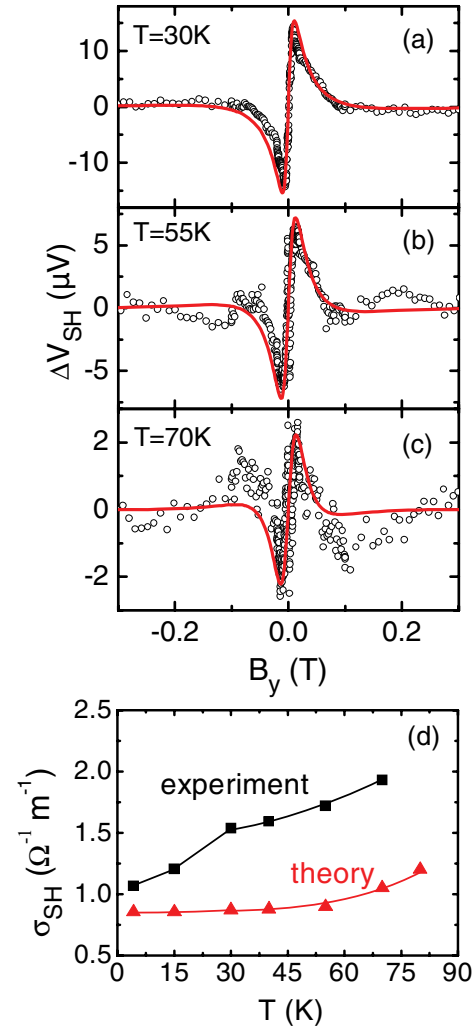


FIG. 4. (Color online) (a)–(c) Spin Hall voltage V_{SH} as a function of B_y at three different temperature values T for current density $j_x = 1.7 \times 10^3$ A/cm²; (d) temperature dependence of σ_{SH} for $j_x = 1.7 \times 10^3$ A/cm². Displayed are the experimental results (black squares) and predicted values (red triangles), derived from Eq. (3) using measured $n(T)$ and $\sigma_{xx}(T)$. Lines are just guides for the eye.

however, one cannot treat both skewness parameter γ and side jump contribution σ_{SJ} as fully independent on σ_{xx} . There seem to exist two regimes in σ_{xx} in which two different sets of parameters γ and σ_{SJ} determine spin Hall conductivity σ_{SH} .

Let us now briefly discuss possible explanations for the observed behavior of σ_{SH} . As mentioned above, we tuned the conductivity of the channel by applying different bias currents to the sample, i.e., creating different electric fields E_x in the channel. This is possible because in low doped GaAs electric field can influence both mobility, due to its effect on mean electron energy, and carrier concentration in the sample, due to impact ionization of donors.²⁰ One could argue that the latter could generally lead, according to Eq. (4), to changes in σ_{SJ} . This would require however a large change of density, whereas ordinary Hall measurements performed on our samples do not show a dependence of n on E_x , and the same applies to measurements reported in Refs. 10 and 21. As for the

skewness parameter γ , it is treated in Ref. 5 as independent of the electric field, at least up to ~ 200 V/cm. Both sets of data shown in Fig. 3(d) were obtained for approximately the same range of electric field E_x , i.e., ~ 30 – 200 V/cm for our data and ~ 5 – 200 V/cm for the other. This suggests that electric field dependence is rather not the reason for observed change in γ .

We performed also temperature studies of the spin Hall signal in the range of $T = 4.2$ – 80 K for $j = 1.7 \times 10^3$ A/cm². The results are summarized in Figs. 4(a)–4(c) showing experimental data (symbols) and Hanle fits (solid lines) for three different temperature values. In Fig. 4(d), we plot then the dependence of extracted spin Hall conductivity on temperature. The measured signal decreased with increasing temperature mainly as a result of decreasing τ_s . Above $T = 70$ K, the signal was no longer observable, which is consistent with spin injection experiments on the same wafer.¹⁶ Because channel conductivity increases with temperature we expected also an increase of σ_{SH} . This was indeed observed as shown in Fig. 4(d). In the same figure, we plot also the predicted dependence (red triangles) of σ_{SH} on temperature using Eq. (3) and the measured values of $\sigma_{xx}(T)$ and $n(T)$. We clearly see that extracted σ_{SH} increases faster with T than predicted, especially in the range of 4–30 K.

IV. SUMMARY

In summary, we conclusively demonstrated all-electrical measurements of spin Hall effect using Esaki diodes as ferromagnetic spin detectors. The high spin detection efficiency of the latter results in a relatively high amplitude of the measured signal, comparing, e.g., to experiments with Fe/GaAs Schottky diodes as spin sensitive contacts.¹⁰ This allowed us to efficiently study spin Hall effect in channels with lower conductivities than previously. The values of spin Hall conductivities extracted from our measurements are consistent with those calculated by Engel *et al.*⁵ and smaller than those presented in Ref. 10. Combined results of these two experiments show that both skewness and side jump contribution into spin Hall conductivity can be treated as independent on channel conductivity only in a certain regime of the latter and may have different values in different ranges of conductivity.

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