Spin-orbit coupling in fluorinated graphene

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(Received 31 October 2014; revised manuscript received 30 January 2015; published 30 March 2015)

We report on theoretical investigations of the spin-orbit coupling effects in fluorinated graphene. First-principles density functional calculations are performed for the dense and dilute adatom coverage limits. The dense limit is represented by the single-side semifluorinated graphene, which is a metal with spin-orbit splittings of about 10 meV. To simulate the effects of a single adatom, we also calculate the electronic structure of a 10 × 10 supercell, with one fluorine atom in the top position. Since this dilute limit is useful to study spin transport and spin relaxation, we also introduce a realistic effective hopping Hamiltonian, based on symmetry considerations, which describes the supercell bands around the Fermi level. We provide the Hamiltonian parameters which are best fits to the first-principles data. We demonstrate that, unlike for the case of hydrogen adatoms, fluorine’s own spin-orbit coupling is the principal cause of the giant induced local spin-orbit coupling in graphene. The $sp^3$ hybridization induced transfer of spin-orbit coupling from graphene’s $\sigma$ bonds, important for hydrogenated graphene, contributes much less. Furthermore, the magnitude of the induced spin-orbit coupling due to fluorine adatoms is about 1000 times more than that of pristine graphene, and 10 times more than that of hydrogenated graphene. Also unlike hydrogen, the fluorine adatom is not a narrow resonant scatterer at the Dirac point. The resonant peak in the density of states of fluorinated graphene in the dilute limit lies 260 meV below the Dirac point. The peak is rather broad, about 300 meV, making the fluorine adatom only a weakly resonant scatterer.

DOI: 10.1103/PhysRevB.91.115141 PACS number(s): 72.80.Vp, 71.70.Ej, 73.22.Pr

I. INTRODUCTION

Functionalizing graphene with adatoms and admolecules is very attractive for spintronics research [1], as it offers new tools to tailor spin and magnetic properties [2] of this unique two-dimensional material [3]. On the one hand, adatoms—in particular paramagnetic ones such as hydrogen [4] and organic molecules [5]—can provide the mechanism [6,7] for the ultrafast spin relaxation seen in spin injection experiments [8–11]. On the other hand, even light adatoms such as hydrogen can induce giant spin-orbit coupling (SOC) [12,13] which makes novel spin transport phenomena such as the spin Hall effect [14] observable in graphene.

A particularly interesting adatom is fluorine. Being the most electronegative element, fluorine forms a strong covalent bond with carbon, affecting the stability of possible fluorine-graphene conformations [15]. Even before the synthesis of graphene there were theoretical studies of fluorinated graphite surfaces [16,17]. Magnetization measurements show that fluorinated graphene can induce spin 1/2 paramagnetic moments [18]. Magnetic moments also seem to be deduced from magnetotransport [19] and weak localization measurements [20]. However, theoretically the case for induced magnetic moments due to fluorine is controversial. Some density functional calculations predict a spin unpolarized ground state [5], while other calculations seem to predict a spin polarized one [21]. The difficulty seems to stem from the self-interaction error in the exchange-correlation functionals that tends to delocalize electronic states [22,23]. It may be that the standard density functional approximations will not be able to resolve this case, calling perhaps for more advanced quantum chemistry approaches. There are also investigations of the influence of charge doping on the magnetism in fluorine [24]. These studies show that charge doping not only affects the magnetism in fluorinated graphene but also leads to a transition from covalent to ionic bonding [25].

Here we focus on spin-orbit coupling induced by fluorine adatoms in graphene. We perform first-principles density functional calculations in the dense and dilute limits of fluorine coverage, to quantify the spin-orbit splitting of the relevant energy bands. Our dense limit is given by the single-side semifluorinated graphene (C$_2$F) which can be experimentally prepared by the chemical reduction of oxidized graphite surfaces [26]. Our study focuses on the chair conformation of C$_2$F which is metallic within DFT, as well as within GW calculations [27]. The computed phonon spectrum also shows the dynamical stability of this structure [27]. It is predicted that the ground state of C$_2$F should be a Néel antiferromagnet [28].

Our main finding is a giant enhancement of spin-orbit coupling, compared even to hydrogenated graphene [13]. The spin-orbit splitting reaches 30 meV. Such a splitting cannot come from graphene itself, as the $\sigma$ bonds are split by about 10 meV, which is the native spin-orbit splitting of the carbon atom. Instead, the splitting comes from the fluorine adatom. This conclusion is further confirmed by investigating the dilute limit, represented here by a 10 × 10 supercell. For this limit we also derive an effective minimal hopping orbital and spin-orbit Hamiltonian, with parameters obtained by fitting to our first-principles calculations. This realistic Hamiltonian should be useful for model calculations of spin transport and spin relaxation in fluorinated graphene. In particular, it shows that fluorine adatoms in the top position are not resonant scatterers at the Dirac point. We present tight-binding calculations for a large, 40 × 40, supercell, as well as analytical results for a single adatom, to show that fluorine leads to a very broad, indeed weak or marginal resonant scattering off the Dirac point: the peak lies 260 meV below the Dirac point, having the full width at half maximum of 300 meV.

Our first-principles results, for both the dense and dilute limits, were performed with the full potential linearized augmented plane wave method, within density functional
theory (DFT). We work with spin unpolarized ground states, to identify spin-orbit effects in the band structures. To model different concentrations of F adatoms we chose different supercells. The dense (1 × 1 supercell) and intermediate (5 × 5 supercell) coverages were calculated with the Wien2K code [29], using a vacuum spacing of 15 Å. The dilute limit (10 × 10 supercell) was calculated with FLEUR [30] in the film geometry. Spin-orbit coupling in these codes is included within the second-variational step in the muffin-tin spheres for valence electrons, while the core electrons are treated fully relativistically. All our first-principles calculations are well converged for fully relaxed structures.

The paper is organized as follows. In Sec. II we present DFT results of the electronic band structure calculation and specifically the spin-orbit coupling induced spin splitting of the bands for a semifluorinated graphene (50% coverage), representing our dense limit case. Section IIIA brings the same, but for a larger supercell, 10 × 10 supercell (0.5% coverage) representing our dilute limit. The dilute limit is then analyzed using a symmetry derived effective hopping Hamiltonian in Sec. IIIB. The model parameters of the Hamiltonian are fitted to the first-principles results. In Sec. IIIC we answer the question whether or not fluorine adatoms on graphene are resonant scatterers. Finally, a comparative analysis with hydrogenated graphene is provided in the Appendix, using an intermediate size 5 × 5 supercell.

II. DENSE LIMIT: SINGLE-SIDE SEMIFLUORINATED GRAPHENE C2F

The unit cell of C2F contains two carbon atoms and one fluorine which chemisorbs preferentially in the top position; see Fig. 1. Our calculated Bader charges show a transfer of about 0.45e from graphene to fluorine. The charged fluorine adatoms repel each other, stretching graphene whose lattice constant grows by about 4.1% in comparison to the typical carbon fluorine bond length [31] of 1.35 Å. The local corrugation allows for resonant scatterers. Finally, a comparative analysis with hydrogenated graphene is provided in the Appendix, using an intermediate size 5 × 5 supercell.

![Graphene structure](image)

**FIG. 1.** (Color online) Unit cells of the dense (50%) and intermediate (2%) fluorination limits. The lattice vectors are shown as black arrows and the unit cell is emphasized by the dashed lines. The inset shows the geometrical structure around a fluorine adatom, with labels for the adatom (F), fluorinated carbon (CF), the nearest (C\textsubscript{nn}), next nearest (C\textsubscript{nnn}), and the next-next nearest (C\textsubscript{nnn}) neighbors of the fluorinated carbon.

In Fig. 2 we show the calculated electronic band structure of C2F. The fully occupied valence bands range in energies from −23 eV to −1 eV. There are seven such bands which are occupied by 14 of the 15 valence electrons (the two carbons contribute 4 electrons each, and fluorine has 7 valence electrons). The band crossing the Fermi level, labeled as (b) in Fig. 2, is only partially occupied. The lowest valence band, at about −23 eV (not shown in the figure) stems from the fluorine 2s orbitals; this band is only weakly dispersive. In the energy region from −18 to −8 eV the band structure of C2F is dominated by the almost intact carbon σ bonds, resembling the band structure of pristine graphene at those energies. However, in the region from −8 to −6 eV we observe anticrossings in the band structure when moving away from the Γ point. At these energies the orbital resolved DOS (see Fig. 2) on the fluorinated carbon C\textsubscript{F} shows the presence of both p\textsubscript{z} and p\textsubscript{x} + p\textsubscript{y} orbitals. This is the manifestation of the structural sp\textsuperscript{3} hybridization—the C\textsubscript{F} atom is pulled out of the plane, the associated p orbitals start to overlap, and their interaction causes anticrossings.
Comparing the orbital resolved DOS for F and CF atoms in Fig. 2, we see two energy windows (−8, −6) eV and (5.5, 7) eV in which both atoms contribute dominantly pz orbitals. These are the bonding and antibonding states made of pz orbitals on F and CF. On the other hand, the px orbitals on the nearest neighbor carbon, Cnn, form the band at the Fermi level that is partially occupied [indicated by (b) at Fig. 2]. This band is weakly dispersive (ca. 2 eV bandwidth) since the geometrically allowed interaction among different Cnn carbons is of the next-nearest-neighbor type. Finally, fluorine px + py orbitals span the energy interval from −5 eV to −1.5 eV. These orbitals hybridize, due to their geometry, only weakly with others. Contributions of different orbitals are indicated by the labeled lines. We also note that there are small orbital contributions around the Fermi level which are most significant for the CF atom.

Spin-orbit splittings for the three bands around the Fermi level are shown in Fig. 3. The splittings vanish at the time reversal points Γ and M and reach values up to 30 meV for band (c). The splitting is smallest for band (a), which is formed by the px orbitals on the fluorinated carbon CF and fluorine, and has only a weak px and py component. As we turn off the spin-orbit coupling on F in our first-principles calculations, this band still shows a significant splitting, in contrast to band (b) and band (c), whose splitting drops to less than 1 meV. This demonstrates that band (a) has a significant part of its splitting due to sp3 deformation alone. On the other hand, bands (b) and (c) are formed to a large extent by fluorine px and py orbitals, whose atomic fine structure is imprinted in the bands as the enhanced spin-orbit splitting. The SOC splitting can be even more enhanced in the vicinity of the anticrossing points due to the more effective transfer of the spin-orbit coupling from the fluorine p levels to the underlying graphene system. In the present case such anticrossing enhancements are observed around the Γ point for the bands (b) and (c) (see the left panel of Fig. 2 at about −1 eV and the corresponding SOC splittings at Fig. 3), and also around the K point for the band (c) (see the left panel of Fig. 2 at about −4 eV and the corresponding SOC splitting at Fig. 3). The enhanced SOC splitting for the band (c) at the K point is attributed to the interaction with the band that is lying lower in energy at about −4 eV and which comprises mainly the fluorine px and py orbitals (see the orbital resolved electronic density at fluorine in Fig. 2).

III. DILUTE LIMIT

A. DFT results for 10 × 10 supercell

To describe chemisorption of an isolated fluorine on graphene we need to consider a large enough supercell with a single fluorine adatom to avoid interactions between periodic images of fluorine. We consider the fluorine atom on the top position, above a carbon atom, which has been reported as the energetically most favorable position [27,33]. For hydrogenated graphene [13] already a 5 × 5 supercell is sufficient to capture the essential features of the dilute limit. In the case of fluorinated graphene this supercell size is not enough as there is still a significant overlap between the fluorine-derived states. We treat this intermediate case in the Appendix. Here we focus on a 10 × 10 supercell (0.5% of adatom coverage) as a representative of the dilute limit for fluorine adatoms.

Our structural relaxation shows that for the 10 × 10 supercell the F−CF bond length equals 1.607 Å, the nearest-neighbor CF−Cnn bond length equals 1.469 Å, and the next-nearest-neighbor Cnn−Cnn distance equals 2.488 Å; see Fig. 1. The fluorinated carbon CF is pulled out of the graphene plane by about 0.423 Å, which is more than in the dense limit (0.312 Å).

In Fig. 4 we show the calculated electronic band structure and local DOS for selected atoms in the 10 × 10 fluorinated graphene supercell. We again focus on three bands—(a), (b), and (c)—near the Fermi level which, in the following, we call the conduction, midgap, and valence bands, respectively. The
midgap band extends over the energy window from $-0.1$ eV to $0.3$ eV and its bandwidth is by $0.2$ eV smaller than in the associated $5 \times 5$ system (see the Appendix). This implies that the Bloch modulation function of the midgap state becomes more localized and that the interaction among the fluorine adatoms is significantly weakened as compared to the more dense cases. From the DOS it is apparent that the main contribution to the electron density of conduction, midgap, and valence bands comes from the $p_z$ orbitals on fluorine F and nearest neighbor C$_{nn}$ carbon atoms. The orbital decomposition of the C$_F$ DOS contains besides the large amount of $p_z$ orbitals on carbon graphene carbon atoms. The orbital decomposition (without spin effects) we employ a local hybridization notation for all relevant atomic sites whose $p_z$ orbitals should be able to describe the electronic structure in the vicinity of the Fermi level, i.e., the conduction, midgap, and valence bands in the energy window from $-0.8$ to $0.8$ eV. Such a model is introduced in the following section.

The above orbital structure analysis suggests that a tight-binding model with only $p_z$ orbitals should be able to describe the electronic structure in the vicinity of the Fermi level, i.e., the conduction, midgap, and valence bands in the energy window from $-0.8$ to $0.8$ eV. Such a model is introduced in the following section.

B. Effective Hamiltonian with spin-orbit coupling

1. Orbital part

Employing local symmetries we derive and analyze an effective $p_z$ orbital tight-binding Hamiltonian including SOC relevant in the vicinity of the fluorine adatom in the top position; see Fig. 5. While we focus on fluorine to obtain realistic hopping parameters, the form of our Hamiltonian is transferable to other top-position adatoms on graphene.

Our first-principles analysis shows that the relevant states around the Fermi level originate from $p_z$ orbitals on carbon and fluorine atoms. To describe the orbital part of the band structure (without spin effects) we employ a local hybridization Hamiltonian which consists of an on-site energy $\epsilon_i$ term on the fluorine adatom and of the orbital hopping $T_i$ between the fluorine adatom and the fluorinated carbon.

![Diagram](image)

**FIG. 5.** (Color online) Left panel: mutual positions and adopted notation for all relevant atomic sites whose $p_z$ orbitals enter the model tight-binding Hamiltonian including local SOC. Shown are fluorine F, fluorinated carbon A = C$_F$, its three nearest B$_1$, B$_2$, B$_3$, and the six next-nearest a$_1$, . . . , a$_6$ neighbors. The principal axis for C$_3$ rotations is defined by the perpendicular F – A bond, while $c$$_v$ reflections are given by three A-B$_i$ lines and the principal axis. Right panel: schematic representation of the dominant orbital and spin-orbital hoppings.

The rest is described by the standard nearest-neighbor hopping Hamiltonian for graphene,

$$H_0 = -t \sum_{(i,j)} \sum_{\sigma \sigma'} (\hat{c}_{i,\sigma}^\dagger \hat{c}_{j,\sigma'} + \hat{c}_{j,\sigma'}^\dagger \hat{c}_{i,\sigma})$$

with the orbital hopping $t = 2.6$ eV; summation over $(i,j)$ runs over all pairs of graphene nearest neighbors. Operator $\hat{F}_\sigma$ (or $\hat{P}_\sigma$) annihilates (creates) an electron with spin $\sigma$ in the atomic $p_z$ orbital on fluorine F. Similarly, $\hat{c}_{i,\sigma}$ ($\hat{c}_{i,\sigma}^\dagger$) are the annihilation (creation) operators for $p_z$ orbitals on carbon graphene atoms. We also introduce $A_{\sigma}$ ($A_{\sigma}^\dagger$) and $B_{\sigma}$ ($B_{\sigma}^\dagger$), $i = 1, 2, 3$, as the annihilation (creation) operators on fluorinated carbon site A, as well as on its three nearest neighbors B$_1$, B$_2$, B$_3$. Our notation is illustrated in Fig. 5. Labels A and B derive from the corresponding sublattice; operators are typographically distinguished to avoid confusion.

Hamiltonian $H'$, Eq. (1), is consistent with the structural C$_{3v}$ symmetry that emerges locally due to fluorine top-position chemisorption. We recall that the point group C$_{3v}$ is generated by C$_3$ rotations around the fluorine-carbon bond (principal axis) and $c$$_v$—vertical reflections containing the principal axis and the A-B$_i$ bond. Using the full orbital Hamiltonian $H_0 + H'$ we have fitted our first-principles band structure of the $10 \times 10$ supercell. To find the optimal values of two tight-binding parameters $T_i$ and $\epsilon_i$ we have focused on conduction, midgap, and valence bands around the Fermi level, see bands (a), (b), and (c) in Fig. 4, as only those have a dominant $p_z$ character. Minimization of the least-square differences between the first-principles and model-computed band structures gives $T = 5.5$ eV and $\epsilon_i = -2.2$ eV. The near perfect agreement with the first-principles data is shown in Fig. 6. This figure also shows the model calculated DOS, using the triangle method (2d analog of the standard tetrahedron method).

2. Spin-orbit part

We now use symmetry arguments to derive the spin-orbit Hamiltonian $H_{SO}$ which gives the fine splittings of the bands around the Fermi level. Again, only $p_z$ orbitals will be used in the description. We identify nonzero matrix elements $\langle i,\sigma | H_{SO} | j,\sigma' \rangle$ between atomic $p_z$ orbitals at sites $i$ and $j$ hosting spins $\sigma$ and $\sigma'$ using invariance of the microscopic spin-orbit Hamiltonian,

$$H_{SO} = \frac{\hbar}{4m^2c^2} \hat{s} \cdot (\nabla \hat{V} \times \hat{p}),$$

under the relevant point-group symmetry and time reversal operations. Here, $m$ is the electron vacuum mass, $c$ the speed of light, and $V$ the total electrostatic potential energy experienced by the electron. Symbols $\hat{p}$ and $\hat{s}$ are the operators of momentum and spin, respectively. As we wish to construct a minimal...
Before we discuss the resulting hoppings, we make two technical comments. First, to obtain the actual phase factors for the matrix elements that correspond to similar atomic orbital configurations, e.g., for \( (\Lambda, \uparrow, \{|H_{SO}|a_{\sigma}\downarrow\}) \), one needs to employ appropriate symmetry operations. This is already accounted for in the SOC Hamiltonian \( \mathcal{H}_{SO} \) provided below. Second, the numerical prefactors are chosen such that the expansion of the SOC Hamiltonian near the K point is numerically prefactor-free, when considering a system coated by adatoms periodically (forming a supercell).

Let us discuss the two terms in Eqs. (4a) and (4b). Those are sublattice-resolved local intrinsic SOCs: \( \Lambda_{i}^A \) mediates spin-conserving hopping between fluorinated carbon A and its six next-nearest neighbors \( C_{nn} = \{B_1, B_2, B_3\} \), and \( \Lambda_{i}^B \) does the same for the nearest carbon atom at \( C_m = \{B_1, B_2, B_3\} \); refer to Fig. 5 for the labeling. Equation (4c) describes the local Rashba coupling that mediates the spin-flip hopping between fluorinated carbon A and its three nearest neighbors \( C_m \). The origin of the Rashba coupling, and hence of the fixed orientation of the perpendicular \( z \) axis stems from a local dipolar electric field that appears due to charge redistribution caused by the fluorine chemisorption. The induced dipolar field can also affect the spin-flip coupling between the nearest and next-nearest neighbor sites, \( C_m \) and \( C_{nn} \), but we do not consider terms like \( (B_1, \uparrow, \{|H_{SO}|a_{\sigma}\downarrow\}) \) in what follows.

The three terms in Eqs. (4d)–(4f) are specific for systems with \( C_{3v} \) structural symmetry. They are describing spin-flip hoppings which connect the next-nearest neighbor sites. The two terms in Eqs. (4d) and (4e) are sublattice-resolved PIA-SOC terms, introduced already for hydrogenated graphene [13] and silicene [38]. The acronym PIA stands for pseudospin-inversion-asymmetry induced SOC: compared to pristine graphene, sublattices A and B are, close to the impurity site, not equivalent. The generally complex matrix element \( (\Lambda_{i}^A, \uparrow, \{|H_{SO}|a_{\sigma}\downarrow\}) \) connects fluorinated carbon A with its six nearest neighbors \( C_{nn} \). We have checked that the imaginary part of this matrix element plays only a minor role in the energy band splittings, so we set \( \Lambda_{i}^A \) to be real in what follows. (In the dense limit, corresponding to pristine graphene, sublattices A and B are, close to the impurity site, not equivalent. The generally complex matrix element \( (\Lambda_{i}^A, \uparrow, \{|H_{SO}|a_{\sigma}\downarrow\}) \) connects fluorinated carbon A with its six nearest neighbors \( C_{nn} \).)

Similarly, the real SOC \( \Lambda_{i}^B \) mediates spin-flip hoppings among three nearest neighbors \( B_1, B_2, B_3 \). Our analysis shows that this term is crucial for explaining the fine band structure splittings due to adatom induced SOC. Finally, parameter \( \Lambda_{FC} \) describes allowed spin-flip hoppings among the fluorine F and three Cnn carbon atoms \( B_1, B_2, B_3 \). In our fitting procedure we find that for fluorine adatoms this term is negligible.

We now give a minimal SOC Hamiltonian for a top-position chemisorbed adatom:

\[
\mathcal{H}_{SO} = \frac{i\Lambda_{i}^A}{3\sqrt{3}} \sum_{c \in C_{nn}} \sum_{\sigma} [\hat{A}_{\sigma} \nu_{ij}(\xi_{c})\sigma \hat{e}_{j,\sigma} + \text{H.c.}] \\
+ \frac{i\Lambda_{i}^B}{3\sqrt{3}} \sum_{(i,j)} \sum_{\sigma} \hat{B}_{i,\sigma} \nu_{ij}(\xi_{c})\sigma \hat{B}_{j,\sigma}
\]

FIG. 6. (Color online) Left panel: electronic band structure of the dilute fluorinated graphene in 10 × 10 supercell configuration; the first-principles data are presented by black dotted lines and the tight-binding model data by blue solid lines. The model calculation is based on the orbital Hamiltonian \( \mathcal{H}_0 + \mathcal{H}' \) with the parameters \( T = 5.5 \text{ eV} \) and \( \epsilon_f = -2.2 \text{ eV} \) that are chosen by fitting the conduction (a), midgap (b), and valence band (c) along the M-K-Γ panel: DOS per atom and spin corresponding to the tight-binding Hamiltonian, and \( \mathcal{H}_{SO} \) is given by Eq. (4f) below. The two terms in Eqs. (4a) and (4b) are sublattice-resolved local intrinsic SOCs: \( \Lambda_{i}^A \) mediates spin-conserving hopping between fluorinated carbon A and its six next-nearest neighbors \( C_{nn} = \{B_1, B_2, B_3\} \), while \( \Lambda_{i}^B \) does the same for the nearest carbon atom \( C_m = \{B_1, B_2, B_3\} \). The origin of the Rashba coupling, and hence of the fixed orientation of the perpendicular \( z \) axis stems from a local dipolar electric field that appears due to charge redistribution caused by the fluorine chemisorption. The induced dipolar field can also affect the spin-flip coupling between the nearest and next-nearest neighbor sites, \( C_m \) and \( C_{nn} \), but we do not consider terms like \( (B_1, \uparrow, \{|H_{SO}|a_{\sigma}\downarrow\}) \) in what follows.

The three terms in Eqs. (4d)–(4f) are specific for systems with \( C_{3v} \) structural symmetry. They are describing spin-flip hoppings which connect the next-nearest neighbor sites. The two terms in Eqs. (4d) and (4e) are sublattice-resolved PIA-SOC terms, introduced already for hydrogenated graphene [13] and silicene [38]. The acronym PIA stands for pseudospin-inversion-asymmetry induced SOC: compared to pristine graphene, sublattices A and B are, close to the impurity site, not equivalent. The generally complex matrix element \( (\Lambda_{i}^A, \uparrow, \{|H_{SO}|a_{\sigma}\downarrow\}) \) connects fluorinated carbon A with its six nearest neighbors \( C_{nn} \). We have checked that the imaginary part of this matrix element plays only a minor role in the energy band splittings, so we set \( \Lambda_{i}^A \) to be real in what follows. (In the dense limit, corresponding to pristine graphene, sublattices A and B are, close to the impurity site, not equivalent. The generally complex matrix element \( (\Lambda_{i}^A, \uparrow, \{|H_{SO}|a_{\sigma}\downarrow\}) \) connects fluorinated carbon A with its six nearest neighbors \( C_{nn} \).)
The creation and annihilation operators are defined in the discussion after Eq. (2). Symbol \( \hat{\sigma} \) represents the array of Pauli matrices acting on the spin space; the sign factor \( \nu_{ij} \) equals +1 if the next-nearest neighbor hopping path \( j \rightarrow k \rightarrow i \) via a common neighbor \( k \) is counterclockwise (-1 for clockwise). Vectors \( d_{ij} \) and \( D_{ij} \) are unit vectors in the \( xy \) plane (perpendicular to the \( \overrightarrow{F} \) bond) pointing from the projected site \( j \) to \( i \). The last term in Eq. (5) is the intrinsic SOC of pristine graphene for which \( \lambda_1 = 12 \) \( \mu \)eV; see Ref. [34]. We have implemented this term for all next-nearest neighbors not participating in SOC hopping with the coupling constants \( \Lambda^B_1 \) and \( \Lambda^B_2 \); this fact is indicated by the prime at the corresponding summation symbol.

3. Fits to first-principles results

The fit of our tight-binding model to the first-principles calculations of the 10 \( \times \) 10 supercell of fluorinated graphene is given in Fig. 7. Spin-orbit splittings of bands (a), (b), and (c) from Fig. 4 are shown. The splittings reach maxima of 0.1, 0.35, and 0.3 meV for the three (a), (b), and (c) bands, respectively. Keeping the orbital parameters fixed we focused on reproducing SOC induced splittings employing the full model Hamiltonian \( \hat{H}_0 + \hat{H} + \hat{H}_{SO} \). We explored various combinations of \( \Lambda \)'s that enter Eq. (5) to generate a minimum robust set of parameters capable to explain the observed SOC splittings. Minimizing the sum of least-square differences for SOC splittings of conduction, midgap, and valence bands along the full M-K-\( \Gamma \)-M line, we have obtained the minimal SOC basis with \( \Lambda^A_1 = 3.3 \) meV, \( \Lambda^B_{PA} = 7.3 \) meV, and \( \Lambda_R = 11.2 \) meV only; see Fig. 7. This indicates that all remaining group-theory allowed SOC parameters in Hamiltonian \( \hat{H}_{SO} \), Eq. (5), can be safely omitted. For the valence and conduction bands near the \( \Gamma \) point we observe marked discrepancies between the tight-binding model and first-principles calculations. The reason is the admixture of 2\( s \) and 3\( d \) orbitals that contribute to DOS as much as 2\( p_z \) orbitals near \( \Gamma \), i.e., at energies below \(-0.6 \) eV for the valence band and above 0.9 eV for the conduction band; see Fig. 4. Since our symmetry inspired effective SOC Hamiltonian accounts for \( p_z \) orbitals, discrepancies such as those around \( \Gamma \) are to be expected. Nevertheless, it is rather remarkable that with only three SOC parameters we are able to near perfectly match all the characteristic features accompanying SOC splittings along the whole M-K-\( \Gamma \)-M line for all three bands around the Fermi level. Such a close agreement with first-principles results is to some extent fortuitous, given by the almost sole \( p_z \) character of the bands around the Fermi level. At the same time it gives us confidence in our minimal phenomenological orbital and SOC hopping model, whose graphical representation is shown in Fig. 5.

In addition to the 10 \( \times \) 10 supercell, we have also calculated a smaller, 7 \( \times \) 7, supercell from first principles. The best-fit tight-binding model parameters in this case are \( T = 6.1 \) eV, \( \varepsilon_f = -3.3 \) eV, and \( \Lambda^B_0 = 3.2 \) meV, \( \Lambda^B_{PA} = 7.9 \) meV, and \( \Lambda_R = 11.3 \) meV. These values are very close to those of the 10 \( \times \) 10 supercell, further evidencing the robustness and consistency of our minimal tight-binding model. The spin-orbit parameters seem to be less sensitive to the supercell size than the orbital ones. Both supercell results are summarized in Table I. The intermediate case of a 5 \( \times \) 5 supercell, which we find to be insufficient to describe the dilute limit, and so unsuitable for our tight-binding analysis here, is treated in the Appendix.

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</table>
As in the dense limit, there are two principal causes of the enhanced spin-orbit coupling due to fluorine adatom: \( sp^3 \) hybridization of carbon orbitals (with spin orbit from the \( \sigma \) bonds) and the native spin-orbit coupling of fluorine. In order to separate and quantify these two contributions, we turned off the intra-atomic SOC on fluorine in the first-principles calculation; see Fig. 7. The splitting is significantly reduced, by an order of magnitude. We conclude that \( sp^3 \) distortion gives spin-orbit splitting in magnitude a decade smaller than what is induced by the native spin-orbit coupling of graphene. The giant enhancement of spin-orbit coupling in graphene due to fluorine adatoms comes almost solely from the spin-orbit coupling of fluorine and hybridization of fluorine \( p \) orbitals with those of carbon. To understand the microscopic mechanism of this SOC transfer one should build a multiorbital tight-binding model with all relevant orbitals on F, A, and B1, B2, B3 sites and then downfold the Hamiltonian matrix to the \( p_z \) orbital sector, as was done for graphene [37,39]. Such an analysis is beyond the scope of the present paper which aims at presenting an effective single-orbital model, given by Hamiltonian \( H_{SO} \), Eq. (5), that can be used for transport and spin relaxation studies.

In contrast, in hydrogenated graphene the microscopic physics behind the giant enhancement of spin-orbit coupling is \( sp^3 \) bonding, as shown by first-principles calculations [13]. The spin-orbit coupling comes from the carbon \( \sigma \) bonds, which are split by about 10 meV at \( \Gamma \). Part of this splitting is transferred to the \( \pi \) band upon \( sp^3 \) hybridization as a hydrogen is added on top of a carbon atom. In fact, spin-orbit splittings induced by hydrogen are similar in magnitude as what is represented by the dashed lines in Fig. 7; compare with Ref. [13]. The effective SOC Hamiltonian \( H_{SO} \), Eq. (5), can be also employed in the hydrogenated case, for which the most dominant SO couplings are \( \Delta^A_{\Gamma} = -0.21 \) meV, \( \Delta^{B}_{\Pi A} = -0.77 \) meV, and \( \Delta_{R} = 0.33 \) meV. Comparing spin-orbit coupling in pristine, hydrogenated, and fluorinated graphene, the magnitude grows roughly from 10 \( \mu \)eV, 1 meV, to 10 meV, respectively, reflecting different microscopic mechanisms behind the coupling in these systems.

C. “Is fluorine on graphene a resonant scatterer?”

Hydrogen chemisorbed on graphene acts as a resonant scatterer [6,36], giving a narrow pronounced peak in the DOS close to the Dirac point. In Fig. 8 we plot the tight-binding band structures for hydrogenated graphene using a 40 \( \times \) 40 supercell with a single hydrogen in the top position. The midgap band, formed of \( p_z \) orbitals on the nearest-neighbor C\(_{nn}\) carbon is very narrow, developing the resonance peak seen in the DOS. As the supercell size grows, the valence and conduction bands merge towards the Dirac cone structure of pristine graphene, leaving the flat midgap band almost intact. Such resonances are predicted to have profound effects on spin relaxation [6] and spin transport [40].

Fluorinated graphene in the dilute limit looks qualitatively different from hydrogenated graphene. The calculated tight-binding band structure of a 40 \( \times \) 40 supercell is shown in Fig. 9. We have used the same parameters as for the 10 \( \times \) 10 supercell in Table I, which we believe are representative for the dilute limit. The valence and conduction bands look similar to the corresponding bands of pristine graphene. The Dirac structure is almost intact. What used to be the midgap band (b) merges together with the conduction band (a), creating close to the \( K \) point a superimposed band structure with linear dispersion. The linear behavior is clearly seen at small energies in the DOS for which the gap at \( K \) is gradually decreasing. No resonant level is observed close to the Dirac point. However, there are significant changes in the Dirac cone structure occurring at energies below –0.1 eV, as seen in

![FIG. 8. (Color online) Extrapolated band structure and DOS of pristine (dashed) and hydrogenated (solid) graphene for a 40 \( \times \) 40 supercell. The left panel shows tight-binding model-calculated band structures along M-K-\( \Gamma \)-M lines. The right panel shows the corresponding DOS. Tight-binding orbital parameters for hydrogenated graphene, \( T_R = 7.5 \) eV and \( \epsilon_R = 0.16 \) eV, are taken from Ref. [13]. The band structure of hydrogenated graphene shows a narrow resonant peak in the vicinity of the Dirac point.](image1)

![FIG. 9. (Color online) Extrapolated band structure and DOS for the pristine (dashed) and fluorinated (solid) graphene for a 40 \( \times \) 40 supercell configuration. The left panel shows model-calculated band structures along M-K-\( \Gamma \)-M and the right panel the corresponding DOS. Characteristic changes in DOS for the dilute fluorinated graphene become obvious below –0.1 eV. Tight-binding orbital parameters used in the model calculations, \( T = 5.5 \) eV and \( \epsilon_T = -2.2 \) eV, are best fits to DFT results for 10 \( \times \) 10 supercell configuration.](image2)
Fig. 9. Here, DOS shows a multiple-peak structure due to anticrossings of the bands. The question arises of what would be the ultimate limit of a single fluorine adatom on an infinite graphene sheet. The above 40 × 40 supercell calculations indicate a broad resonance peaked somewhere below −0.2 eV. Fortunately, the orbital-hopping part of our Hamiltonian is analytically solvable in the single-adatom limit, and we can calculate the change $\Delta \nu(E)$ of the DOS due to a single fluorine adatom. Considering a very low concentration $\eta$ (just a prefactor) of adatoms, a typical change in the unperturbed DOS per atom and spin—ignoring multiple-scattering interference among different adatom scatterers—would be given by $\eta \Delta \nu(E)$. The tight-binding Hamiltonian (1) can be effectively downfolded, eliminating the fluorine $p_z$ orbitals by means of the Löwdin-Schrieffer-Wolff transformation. As a result $H'_F$ produces an energy dependent $\delta$-like interaction $H'_{\text{fold}}(E)$ localized at the fluorinated carbon $C_F$,

$$H'_{\text{fold}}(E) = \sum_{\sigma} \alpha(E) \hat{A}^\dagger_{\sigma} \hat{A}_\sigma, \quad \text{where } \alpha(E) = \frac{T^2}{E - \epsilon_f}. \quad (6)$$

Following Ref. [41], we obtain

$$\Delta \nu(E) = \frac{1}{\pi} \text{Im} \left[ \frac{\alpha(E)}{1 - \alpha(E)G_0(E)} \frac{\partial}{\partial E} G_0(E) \right]. \quad (7)$$

Here, $G_0(E)$ is the Green’s function per atom and spin for the unperturbed pristine graphene, which, within the energy range from $\pm 0.5$ eV up to $0.5$ eV, can be very well approximated by $G_0(E) \approx E / D^2 \left[ \ln \left| \frac{E^2}{D^2 - E^2} - i \pi \text{sgn}(E) \delta(D - |E|) \right| \right]$, \quad (8)

with the graphene bandwidth $D = \sqrt{3}\pi t \approx 6$ eV; see, for example, Refs. [6,36].

Our analytical results are shown in Fig. 10, in which we plot $\Delta \nu(E)$ as well as the full DOS per atom and spin, $\nu(E) = \nu_0(E) + \eta \Delta \nu(E)$, as functions of energy, for fluorinated graphene at very low concentrations. The quantity $\nu_0(E)$ describes the DOS per atom and spin of the unperturbed graphene, $\nu_0(E) \equiv -\frac{1}{\pi} \text{Im} G_0(E)$. To visualize the changes in DOS we take an unrealistically large concentration (whose effect is purely multiplicative) of $\eta = 0.5\%$. From Fig. 10 we see that fluorine dominantly affects the DOS at energies around $E \approx -0.26$ eV which corresponds to a pronounced peak in $\Delta \nu(E)$ with the FWHM $\approx 0.3$ eV. This gives the energy window ($-0.4$ eV, $-0.1$ eV) where we expect dominant orbital effects of fluorine chemisorption; see also results of Ref. [42]. There is a recent experimental evidence [43], based on electron-hole asymmetry in transport, indicating resonant scattering due to fluorination, but further studies are certainly called for.

IV. CONCLUSIONS

We studied, from first principles, the electronic structure and spin-orbit splitting of spin unpolarized fluorinated graphene. Two important limits were covered: a dense limit, represented by a $1 \times 1$ supercell with a single fluorine in the top position in the cell, and a dilute limit, represented by a $10 \times 10$ supercell, also with a single top-positioned fluorine adatom. We further looked at the intermediate case of a $5 \times 5$ supercell, to contrast differences with the case of hydrogenated graphene. All our investigated structures were structurally relaxed.

For the dilute limit we introduced a single-orbital tight-binding (hopping) Hamiltonian that very nicely reproduces the first-principles results. The orbital part of the Hamiltonian is based on the changes of the adatom energy and includes also hopping between the fluorine and fluorinated carbon. The spin-orbit part includes the usual intrinsic (spin-conserving next-nearest neighbor) and Rashba (spin-flip nearest neighbor) hoppings, as well as new PLA hoppings which describe spin-flip paths between next-nearest neighbors. We give a specific description of the Hamiltonian and the complex phases of the hopping, as well as best fits to the DFT obtained spin-orbit spin splittings. We also use our tight-binding Hamiltonian to investigate superlarge supercells ($40 \times 40$) to search for band structure resonances due to fluorine adatoms. Using nonperturbative analytical calculations we also obtain what would be a single-adatom representation of the changes in the density of states. We believe that our tight-binding model Hamiltonian is reliable to explain the physics near the Fermi level of fluorinated graphene and can be used in quantum transport simulations that involve orbital and spin-orbit effects, say momentum and spin relaxation, charge and spin transport, or the spin Hall effect.

We draw several conclusions from our investigations. (i) Fluorine induces a giant spin-orbit coupling, an order of magnitude greater than hydrogen. This is evidenced directly by the dense limit results, but also by the magnitudes of the obtained fits to our tight-binding model. (ii) The enhancement of spin-orbit coupling is not principally due to the $\sigma - \pi$ hybridization induced by structural deformation, as in the case of hydrogen. In fact, the giant enhancement of SOC on graphene band structure due to fluorine adatoms comes
from the native spin-orbit coupling of fluorine, and its orbital hybridization with carbon. (iii) Fluorine adatoms are only weak or marginal resonant scatterers. The resonant peak in the density of states lies 260 meV below the Dirac point. The peak is about 300 meV broad. This again contrasts with hydrogenated graphene which are perfect examples of narrow resonance scatterers at the Dirac point.

**ACKNOWLEDGMENTS**

We thank Jun Zhu for stimulating discussions. This work was supported by the DFG SFB Grant No. 689 and GRK Grant No. 1570, and by the European Union Seventh Framework Programme under Grant Agreement No. 604391 Graphene Flagship.

**APPENDIX: INTERMEDIATE LIMIT: 5 x 5 SUPERCELL**

In what follows we summarize our findings for the intermediate limit of a 5 × 5 supercell, which lies in between the dense and dilute ones. For hydrogenated graphene [13] such a supercell is already large enough to represent dilute coverage. Our 5 × 5 supercell is fully relaxed, with the lattice constant 12.297 Å, which differs by 0.2% from the same-size pure graphene supercell lattice constant (12.3 Å). Bader charge analysis shows that fluorine acquires a negative charge of 0.518e. In contrast, for the hydrogenated case there is almost zero charge transfer to hydrogen. In Fig. 11 we show the calculated electronic band structures for the fluorinated and hydrogenated graphene for comparison. In both cases one sees a formation of the midgap states around the Fermi level. However, the bandwidth of 0.6 eV for the fluorinated graphene is much larger than for hydrogenated graphene, for which the bandwidth is less than 0.1 meV [13].

The DOS for selected atoms in the vicinity of fluorine are shown in Fig. 12. Orbital resolved analysis shows a significant contribution of $p_z$ orbitals to the states in the studied energy window around the Fermi level. The spatial distribution of the $p_z$ orbitals can be visualized by the electronic density $\rho(\mathbf{r}) = \sum_{n,\mathbf{k}} |\phi_n^k(\mathbf{r})|^2$. In Fig. 13 we show a top view of the electronic density summed over the Kohn-Sham eigenstates $\phi_n^k$ including eigenstates with energies $\epsilon_n^k$ lying within the energy window $\epsilon_{\text{min}} = -0.2$ eV and $\epsilon_{\text{max}} = 0.6$ eV with respect to the Fermi level. The dashed line in the main figure corresponds to the cross-sectional view shown in Fig. 13. From the plot one sees that the midgap state represents a strongly delocalized state mostly situated on the “nonfluorinated” sublattice (i.e., sublattice B, fluorinated carbon C_F is on sublattice A). The appearance of such a delocalized state indicates that a 5 × 5 supercell is not large enough to represent the dilute fluorination limit, since there is still significant fluorine interaction among the periodic images.

We find that sublattice B is the main contributor to the midgap DOS (80%). The fluorine atom and the carbon atoms at sublattice A account for only 10% each. In the valence band

![Fig. 11. Calculated electronic band structures of fluorinated (left panel) and hydrogenated (right panel) graphene within 5 × 5 supercell configurations. Three bands (a), (b), and (c) correspond to the conduction, midgap, and valence band, respectively, as in the main text. Formation of the midgap state around the Fermi level dominates both band structures. However, for hydrogenated graphene this band is hardly dispersive, giving the pronounced resonance at the Dirac point.](image)

![Fig. 12. (Color online) Calculated orbital resolved atomic DOS for fluorinated graphene in a 5 × 5 supercell. The orbital resolved DOS is shown for the fluorine atom F, fluorinated carbon C_F, and its nearest, next-nearest, and next-next-nearest neighbors, C_{nn}, C_{nnn}, and C_{nnnn}, respectively.](image)

![Fig. 13. (Color online) Top view of the valence charge density plot of fluorinated graphene on a 5 × 5 supercell. The charge density was obtained by summing the absolute squares of the Kohn-Sham states lying in the energy interval between -0.2 eV and 0.6 eV. The dark (orange) surface is the isovalue of 0.002 Å⁻³ and the light (yellow) one corresponds to 0.001 Å⁻³. Dashed lines represent the cross-sectional view shown in the bottom right.](image)
FIG. 14. (Color online) SOC splittings for the conduction (a), midgap (b), and valence (c) bands with respect to the Fermi level of the initially fluorinated $5 \times 5$ system. Dashed lines are representing the SOC splittings without the intra-atomic SOC contributions from the F atom. For comparison the SOC splittings of the hydrogenated $5 \times 5$ system are provided by the dashed-dotted lines.

at $-0.6$ eV, sublattice B represents 54%, sublattice A 36%, and fluorine 10% of the local DOS. This decomposition can be seen in Fig. 12 where the orbital resolved DOS for F, C_F,

and all carbon atoms ($C_{nn}$, $C_{nnn}$, and $C_{nnnn}$) up to the third nearest neighbors of C_F are provided.

A large—predominantly $p_z$—contribution to the midgap states comes from the fluorine atom with 0.5 states/eV, see the first panel in Fig. 12. Atoms $C_{nn}$ and $C_{nnn}$ belonging to the sublattice B, both carry mainly $p_z$ character and contribute equally to the valence band edge at $-0.6$ eV and the midgap level. Their DOS is very similar in shape and value. The DOS at fluorinated carbon C_F has a more complex (visible also in the inset of Fig. 13), where $p_z$, $s$, and $d$ characters are identified, but they sum up to only 0.09 states/eV. The overall contribution of C_F within the energy region from $-2$ eV to 2 eV is very low. The DOS contribution from $C_{nnn}$ carbons at sublattice A is negligible for the midgap and the valence band edge and also possesses mainly $p_z$ character. The conduction band at energies above 0.8 eV has mainly $p_z$ character for all the atoms analyzed in Fig. 12.

Finally, Fig. 14 shows the absolute values of spin-orbit splittings for the conduction (a), midgap (b), and valence (c) bands. The largest splittings range from 0.26 meV for the conduction band, up to 1.1 meV for the valence band. If we turn off the intra-atomic SOC on fluorine, the splittings are drastically reduced, essentially to the hydrogenated graphene level. This nicely demonstrates the limit of what spin-orbit splittings can be achieved by $sp^3$ bonding. If a larger splitting is observed, the spin-orbit coupling comes most likely from the adatom itself, not from the host graphene lattice.