

# Proximity effects in graphene on monolayers of transition-metal phosphorus trichalcogenides $MPX_3$ ( $M$ : Mn, Fe, Ni, Co, and $X$ : S, Se)

Klaus Zollner<sup>✉\*</sup> and Jaroslav Fabian<sup>✉</sup>*Institute for Theoretical Physics, University of Regensburg, 93040 Regensburg, Germany*

(Received 22 April 2022; revised 13 July 2022; accepted 13 July 2022; published 20 July 2022)

We investigate the electronic band structure of graphene on a series of two-dimensional magnetic transition-metal phosphorus trichalcogenide monolayers,  $MPX_3$  with  $M = \{\text{Mn, Fe, Ni, Co}\}$  and  $X = \{\text{S, Se}\}$ , with first-principles calculations. A symmetry-based model Hamiltonian is employed to extract orbital parameters and sublattice resolved proximity-induced exchange couplings ( $\lambda_{\text{ex}}^A$  and  $\lambda_{\text{ex}}^B$ ) from the low-energy Dirac bands of the proximitized graphene. Depending on the magnetic phase of the  $MPX_3$  layer (ferromagnetic and three antiferromagnetic ones), completely different Dirac dispersions can be realized with exchange splittings ranging from 0 to 10 meV. Remarkably, not only the magnitude of the exchange couplings depends on the magnetic phase, but also the global sign and the type. Important, one can realize uniform ( $\lambda_{\text{ex}}^A \approx \lambda_{\text{ex}}^B$ ) and staggered ( $\lambda_{\text{ex}}^A \approx -\lambda_{\text{ex}}^B$ ) exchange couplings in graphene. From selected cases we find that the interlayer distance, as well as a transverse electric field, are efficient tuning knobs for the exchange splittings of the Dirac bands. More specifically, decreasing the interlayer distance by only about 10%, a giant fivefold enhancement of proximity exchange is found, while applying few V/nm of electric field, provides tunability of proximity exchange by tens of percent. We have also studied the dependence on the Hubbard  $U$  parameter and find it to be weak. Moreover, we find that the effect of SOC on the proximitized Dirac dispersion is negligible compared to the exchange coupling.

DOI: [10.1103/PhysRevB.106.035137](https://doi.org/10.1103/PhysRevB.106.035137)

## I. INTRODUCTION

Monolayer magnets are key ingredients for novel spintronics applications, such as in tunneling magnetoresistance and spin-orbit torque device architectures [1–6]. One step towards next generation devices is to achieve highly spin polarized currents and long-distance transfer of spin information in all two-dimensional (2D) van der Waals (vdW) heterostructures without the need of conventional ferromagnets (FM), where, for example, conductivity mismatch occurs at the interface [7–11]. Remarkably, recent experiments have shown that in graphene/CrSBr heterostructures, where CrSBr is a layered antiferromagnet, high spin polarization of the graphene conductivity arises solely due to proximity-induced exchange coupling [12,13]. Therefore, it is essential to study proximity effects in graphene, since it already intrinsically provides long-distance spin communication [14,15], but lacks an efficient spin manipulation knob.

Proximity effects in graphene can significantly alter the spin transport. For example, heterostructures with transition-metal dichalcogenides (TMDCs) provide a giant enhancement of the spin-orbit coupling (SOC) in graphene by proximity [16,17]. Moreover, the proximity SOC can be efficiently tuned by gating and twisting in graphene/TMDC heterostructures [18–24], allowing us to tailor, for example, the interconversion between spin and charge currents [23–37] or the spin-relaxation anisotropy [21,38–43]. Placing graphene

on a ferro- or antiferromagnet results in proximity-induced exchange coupling. Particularly interesting are magnetic semiconductors such as  $\text{Cr}_2\text{Ge}_2\text{Te}_6$  [1,44,45] or  $\text{CrI}_3$  [46–49], providing spin splitting for Dirac electrons but without contributing to transport. Moreover, the proximity-induced exchange coupling can also be tailored by gating and twisting [50,51], important in, for example, the realization and engineering of topological states in graphene [46,52,53].

Unlike ferromagnets, antiferromagnetic monolayers have not yet been systematically investigated for proximity effects in graphene. Transition-metal phosphorus trichalcogenides ( $MPX_3$ ) are particularly interesting: they are semiconducting, stable in air, and can offer different magnetic configurations [54–75]. In general,  $MPX_3$  monolayers are formed by transition-metal atoms,  $M = \{\text{Mn, Fe, Ni, Co}\}$ , arranged in a honeycomb lattice and surrounded by octahedrally coordinated chalcogen atoms,  $X = \{\text{S, Se}\}$ . Each honeycomb hexagon additionally has two vertically stacked P atoms at the center. Remarkably, the magnetic properties of the  $MPX_3$  crystals can be tuned by gating and straining [61]. In addition, these materials exhibit giant exciton binding energies of several hundred meV [76,77], even larger than in TMDCs, making them candidates for optospintronics applications. In Ni-based transition-metal phosphorus trichalcogenides, there is even evidence of topological superconductivity [64]. Heterostructures of  $\text{MnPSe}_3$  and  $\text{MoS}_2$  show a type-II band alignment, important for optics, and a stacking dependent lifting of spin and valley degeneracy in  $\text{MnPSe}_3$  [78], potentially interesting for valleytronics applications [79,80]. Moreover, it has been shown that antiferromagnetic  $\text{FePS}_3$  increases

\*klaus.zollner@physik.uni-regensburg.de

the coercive field and Curie temperature of the 2D itinerant ferromagnet  $\text{Fe}_3\text{GeTe}_2$  [81], while  $\text{NiPS}_3$  can be important to tailor interfacial spin-orbit torques [82].

Graphene on  $\text{MPX}_3$  monolayers is expected to exhibit strong proximity exchange, depending on the magnetic configuration, stacking, twisting, and gating. For example,  $\text{MnPS}_3$  is an Ising-type antiferromagnetic semiconductor (out-of-plane and alternating magnetic moments on Mn atoms), with the potential to induce staggered exchange coupling in graphene, as recently demonstrated [52]. In this study we consider monolayer graphene in proximity to various  $\text{MPX}_3$  monolayers, which can be either in the ferromagnetic, antiferromagnetic Néel, antiferromagnetic zigzag, or antiferromagnetic stripy phase. In order to unveil the proximity-induced exchange coupling in graphene, we calculate the low-energy Dirac dispersions of the heterostructures by density functional theory (DFT), and fit them to a symmetry-based model Hamiltonian. The effective model can be used for investigating spin transport, spin dynamics, and topologies of proximitized Dirac electrons in graphene/ $\text{MPX}_3$  structures. Such effective models are transferable due to the short-range character of the proximity effect: if a graphene/ $\text{MPX}_3$  interface is part of a vdW heterostructure, the model Hamiltonian we introduce can be applied directly to it.

Depending on the transition metal  $M = \{\text{Mn, Fe, Ni, Co}\}$ , the chalcogen atom  $X = \{\text{S, Se}\}$ , and the magnetic phase, the proximity-induced exchange coupling in graphene can be markedly different. In particular, we find proximity exchange couplings that range from about 0 to 10 meV, varying in sign and type. Most important, one can realize uniform (ferromagnetic) and staggered (antiferromagnetic) proximity exchange in graphene. From the selected case of graphene/ $\text{MnPS}_3$  in the antiferromagnetic Néel phase (ground state), we find that the interlayer distance, as well as a transverse electric field, are efficient tuning knobs for the exchange splittings of the Dirac bands. More specifically, decreasing the interlayer distance by only about 10%, a giant fivefold enhancement of proximity exchange is found, while applying just a few V/nm of electric field can tune the proximity exchange by tens of percent. We have also studied the dependence on the Hubbard  $U$  parameter and find it to be weak. Moreover, we find that the effect of SOC on the proximitized Dirac dispersion is negligible compared to the exchange coupling. Our findings should be useful for spin transport, spin relaxation, optospintronics applications, as well as for tailoring topological phases of the Dirac electrons in graphene [52,76,78].

The paper is organized as follows. In Sec. II we first discuss our computational methodology and the geometry setup. In Sec. III we then introduce the symmetry-based model Hamiltonian capturing the proximity-induced exchange coupling in graphene. In Sec. IV we show and discuss the electronic structure and fit results of the different magnetic phases on the example of the graphene/ $\text{MnPS}_3$  heterostructure. In addition, we report on the effect of the interlayer distance, a transverse electric field, the Hubbard  $U$ , and SOC on the proximitized Dirac dispersion. Finally, in Sec. V we summarize and conclude the paper.

## II. COMPUTATIONAL DETAILS AND GEOMETRY

The electronic structure calculations and structural relaxation of graphene on monolayers of the layered magnets  $\text{MPX}_3$  are performed by density functional theory (DFT) [83] with QUANTUM ESPRESSO [84]. Self-consistent calculations are carried out with the  $k$ -point sampling of  $24 \times 24 \times 1$  to get converged results for the proximity exchange splittings. We perform open shell calculations that provide the spin-polarized (magnetic) states of the  $\text{MPX}_3$  monolayers. A Hubbard parameter of  $U = 4.5$  eV is used for  $M = \{\text{Mn, Fe, Co, Ni}\}$   $d$  orbitals, as in recent calculations [78,85]. We use an energy cutoff for charge density of 700 Ry and the kinetic energy cutoff for wave functions is 70 Ry for the scalar relativistic pseudopotential with the projector augmented wave method [86] with the Perdew-Burke-Ernzerhof exchange correlation functional [87]. When SOC is included, we use the relativistic version of the pseudopotentials. For the relaxation of the heterostructures, we add van der Waals corrections [88–90] and use a quasi-Newton algorithm based on the trust radius procedure. In order to simulate quasi-2D systems, we add a vacuum of 20 Å to avoid interactions between periodic images in our slab geometry. To determine the interlayer distances, the atoms of graphene are allowed to relax only along  $z$  direction (vertical to the layers) and the atoms of  $\text{MPX}_3$  are allowed to move in all directions, until every component of each force is reduced below  $10^{-4}\text{Ry}/a_0$ , where  $a_0$  is the Bohr radius.

For some of our heterostructures, we crosscheck the results with the WIEN2k DFT code [91], using the relaxed structures obtained with QUANTUM ESPRESSO. We use a  $k$ -point sampling of  $18 \times 18 \times 1$  with the cutoff parameter  $RK_{\text{max}} = 4.6$ . The muffin-tin radii are  $R_M = 2.5$ ,  $R_P = 1.87$  (1.86),  $R_X = 1.96$  (2.27), and  $R_C = 1.32$  (1.34) for  $X = \text{S}$  (Se). Van der Waals corrections and a Hubbard  $U = 4.5$  eV are also included [89,92].

The heterostructures of graphene/ $\text{MPX}_3$  contain a  $5 \times 5$  supercell of graphene on a  $2 \times 2$   $\text{MPX}_3$  supercell, resulting in 90 atoms in the unit cell. We consider cases for  $M = \{\text{Mn, Fe, Ni, Co}\}$  and  $X = \{\text{S, Se}\}$ . In Figs. 1(a) and 1(b) we show the exact geometry of the heterostructures. The  $M$  atoms of the  $\text{MPX}_3$  monolayers form a hexagonal lattice. Depending on the  $M$  atom, the  $\text{MPX}_3$  monolayer can have a different magnetic ground state. We consider all of our  $\text{MPX}_3$  substrates to be either in the ferromagnetic, antiferromagnetic Néel, antiferromagnetic zigzag, or antiferromagnetic stripy phase, as shown in Figs. 1(c)–1(f), but with magnetizations to be collinear with the  $z$  direction. Note that structural relaxation was performed only for the ferromagnetic phase. The relaxed geometries are then employed for all other magnetic phases as well. We find that the forces in the other magnetic phases are below  $10^{-3}\text{Ry}/a_0$ , justifying this approach. In addition, we consider only geometries with  $0^\circ$  relative twist angle and the stacking as shown in Fig. 1(a).

In Table I we summarize the experimental lattice constants of all considered monolayers, as well as their strained lattice constants used for the heterostructure calculations. We also list the Néel temperature  $T_N$ , the experimentally determined magnetic ground state for each  $\text{MPX}_3$ , and the DFT-relaxed interlayer distance  $d_{\text{int}}$  between graphene and the  $\text{MPX}_3$ . For

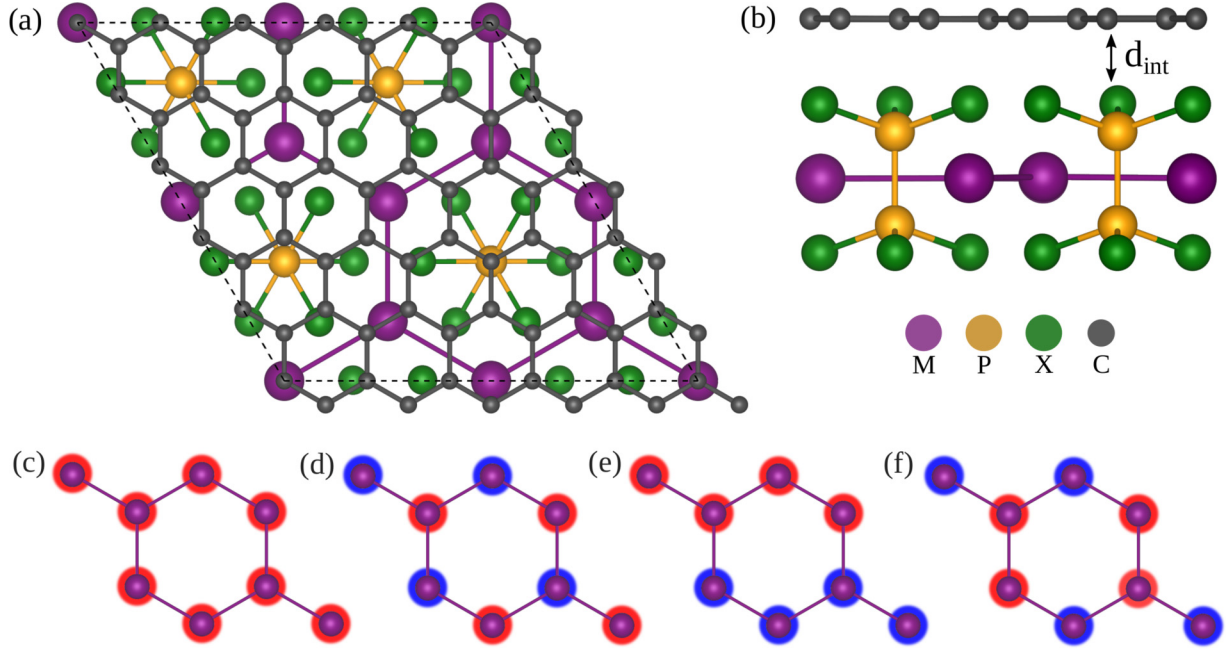


FIG. 1. (a) and (b) Top and side view of the graphene/ $MPX_3$  heterostructure. Dashed line in (a) defines the heterostructure unit cell and in (b) we define the interlayer distance  $d_{\text{int}}$ . Different colors correspond to different atom types. Depending on the  $MPX_3$  crystal, the hexagonal  $M$  lattice can show the (c) ferromagnetic, (d) antiferromagnetic Néel, (e) antiferromagnetic zigzag, and (f) antiferromagnetic stripy phase. Red (blue) spheres indicate magnetization of the  $M$  atom along  $z$  ( $-z$ ) direction.

example,  $MnPS_3$  is a semiconductor, with an optical gap of about 2.3 eV [68,93]. According to experiments, the lattice constant is  $a = 6.39$  Å, it has a Néel temperature of  $T_N = 74$  K, and the magnetic ground state is the antiferromagnetic Néel one [54], see Fig. 1(d). Due to lattice mismatch with graphene, we strain the  $MnPS_3$  layer by about  $-2.9\%$  to get the mentioned supercell with commensurate lattices. The relaxed interlayer distance with graphene is  $d_{\text{int}} = 3.457$  Å.

### III. LOW ENERGY MODEL HAMILTONIAN

From our first-principles calculations we obtain the low energy Dirac band structure of the proximitized graphene and extract realistic parameters for an effective Hamiltonian describing the low-energy bands. The goal is to find an effective description for the low-energy physics, which is relevant for studying transport [23,24,26,45,94], topology [52,95], spin relaxation [38,43,96,97], or emergent long-range or-

der [98]. Due to the short-range nature of the proximity effects in van der Waals heterostructures, the effective models are transferable [99–101]. For example, a bilayer-graphene encapsulated from two sides by different materials can be described by combining the effective models for two proximitized graphene sheets, coupled by bilayer-graphene interlayer couplings [99,100].

The systems we consider have broken time-reversal symmetry and either  $C_3$  or no symmetry, depending on the magnetic phase of the underlying  $MPX_3$ . The following Hamiltonian, derived from symmetry [102–104], is able to describe the graphene bands in the vicinity of the Dirac points when proximity exchange is present:

$$\mathcal{H} = \mathcal{H}_0 + \mathcal{H}_\Delta + \mathcal{H}_{\text{ex}} + E_D, \quad (1)$$

$$\mathcal{H}_0 = - \sum_s f_s(\mathbf{q}) |\Psi_A, s\rangle \langle \Psi_B, s| + \text{H.c.}, \quad (2)$$

TABLE I. Investigated crystallographic and magnetic information collected from Refs. [54,56,58–66,105–117], for the considered monolayers used in the graphene/ $MPX_3$  heterostructures. The experimental (expt) and the employed heterostructure (het) lattice constants  $a$ . The strain for each subsystem, is calculated as  $(a_{\text{het}} - a_{\text{expt}})/a_{\text{expt}}$ . We also list the Néel temperature  $T_N$ , the experimentally determined magnetic ground state for each  $MPX_3$ , as shown in Figs. 1(c)–1(e), and the DFT-relaxed interlayer distance  $d_{\text{int}}$  between graphene and the  $MPX_3$ .

	Graphene	$MnPS_3$	$MnPS_3$	$FePS_3$	$FePS_3$	$NiPS_3$	$NiPS_3$	$CoPS_3$	$CoPS_3$
$a$ (expt) (Å)	2.46	6.39	6.08	6.26	5.94	6.13	5.82	6.19	5.90
$a$ (het) (Å)	2.48 (2.44) <sup>a</sup>	6.20	6.10	6.20	6.10	6.20	6.10	6.20	6.10
Strain (%)	0.8 (−0.8)	−2.9	0.3	−1.0	2.7	1.1	4.8	0.2	3.4
$T_N$ (K)	–	74	78	119	120	206	154	–	120
Ground state	–	Néel	Néel	zigzag	zigzag	zigzag	zigzag	–	zigzag
$d_{\text{int}}$ (Å)	–	3.457	3.422	3.471	3.448	3.474	3.440	3.488	3.430

<sup>a</sup>For graphene/ $MPS_3$  (graphene/ $MPS_3$ ) structures we stretch (compress) the graphene lattice constant to 2.48 Å (2.44 Å).

$$\mathcal{H}_\Delta = \Delta \sigma_z \otimes s_0, \quad (3)$$

$$\mathcal{H}_{\text{ex}} = (-\lambda_{\text{ex}}^A \sigma_+ + \lambda_{\text{ex}}^B \sigma_-) \otimes s_z. \quad (4)$$

The orbital structural function we use is  $f_s(\mathbf{q}) = t_{1,s} + t_{2,s}e^{i\mathbf{q}\mathbf{R}_2} + t_{3,s}e^{-i\mathbf{q}\mathbf{R}_3}$ , where we denote  $t_{\alpha,s}$  as the spin ( $s = \{\uparrow, \downarrow\}$ ) and direction ( $\alpha = \{1, 2, 3\}$ ) dependent hopping parameters, along direction  $\mathbf{R}_\alpha = a(\cos \frac{2\pi(\alpha-1)}{3}, \sin \frac{2\pi(\alpha-1)}{3})$ . The wave vector is  $\mathbf{q} = \tau\mathbf{K} + \mathbf{k}$ , for the valley index  $\tau = \pm 1$  and  $\tau\mathbf{K} = \pm(\frac{4\pi}{3a}, 0)$  with the lattice constant  $a$ .

This orbital structural function is a generalized case for the orbital Hamiltonian as defined in Ref. [102]. Typically, the standard linearized orbital Hamiltonian is used [97,102], but with our definition we can describe cases where the nearest-neighbor hoppings are spin dependent and can be different along different spatial directions. This is necessary, because the magnetic phase of the  $\text{MPX}_3$  monolayer substrate determines the symmetry of the system and the dependence of hoppings on spatial directions. Additionally, because the substrate is magnetic, hoppings can be spin dependent.

The Pauli spin matrices are  $s_j$ , acting on spin space ( $\uparrow, \downarrow$ ), and pseudospin matrices are  $\sigma_j$ , acting on sublattice space ( $C_A, C_B$ ), with  $j = \{0, x, y, z\}$  where  $j = 0$  denotes the  $2 \times 2$  unit matrix. For shorter notation we use  $\sigma_\pm = \frac{1}{2}(\sigma_x \pm \sigma_0)$ . The staggered potential gap is  $\Delta$  and the parameters  $\lambda_{\text{ex}}^A$  and  $\lambda_{\text{ex}}^B$  represent the sublattice-resolved proximity-induced exchange couplings. The four basis states are  $|\Psi_A, \uparrow\rangle, |\Psi_A, \downarrow\rangle, |\Psi_B, \uparrow\rangle$ , and  $|\Psi_B, \downarrow\rangle$ . The model Hamiltonian is centered around the Fermi level at zero energy. Since first-principles results capture charge-transfer effects, we also introduce the parameter  $E_D$  (termed Dirac point energy) which shifts the Dirac bands.

For each considered heterostructure, we calculate the proximitized low energy Dirac bands in the vicinity of the  $K$  point. To extract the fit parameters from the first-principles data, we employ a least-squares routine [118], taking into account band energies, splittings, and spin expectation values (spin up and spin down).

#### IV. BAND STRUCTURE AND FIT RESULTS

In the following we first neglect SOC in the calculations, since we are mainly interested in the proximity-induced exchange couplings. The effects of SOC are discussed at a later point. For our analysis of proximity effects, we consider graphene on the magnetic monolayers  $\text{MPX}_3$ , for different magnetic phases, as shown in Figs. 1(c)–1(f). Depending on the magnetic phase of the  $\text{MPX}_3$ , the system shows either threefold symmetry for ferromagnetic and antiferromagnetic Néel phases or lacks all symmetries in the antiferromagnetic zigzag and stripy phases. In the following we explicitly show and discuss the band structure and model calculations (with fitted parameters) for graphene on  $\text{MnPS}_3$  as an exemplary case. In the Supplemental Material we show the band structure and the fitted results for the remaining  $\text{MPX}_3$  substrates [119]. Furthermore, for graphene on  $\text{MnPS}_3$  in the antiferromagnetic Néel phase (the ground state), we discuss the influence of the interlayer distance, the Hubbard  $U$ , and a transverse electric field on the fitted parameters.

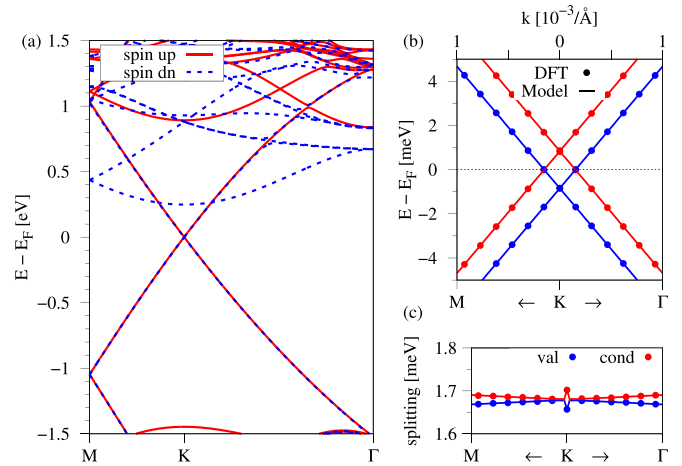


FIG. 2. (a) DFT-calculated band structure of the graphene/ $\text{MnPS}_3$  heterostructure along the high-symmetry path  $M$ - $K$ - $\Gamma$  without SOC, when the  $\text{MnPS}_3$  is in the ferromagnetic phase. Red solid (blue dashed) lines correspond to spin up (spin down). (b) Zoom to the DFT-calculated (symbols) low energy Dirac bands near the  $K$  point with a fit to the model Hamiltonian (solid line). (c) The splitting of valence and conduction band.

#### A. Ferromagnetic phase

First, we consider the  $\text{MnPS}_3$  monolayer to be in the ferromagnetic phase in which the heterostructure has a threefold symmetry and our model can be further simplified by setting  $t_{1,s} = t_{2,s} = t_{3,s}$  for both spin species  $s$ , respectively. In Fig. 2(a) we show the corresponding DFT-calculated band structure of the graphene/ $\text{MnPS}_3$  without SOC. We find that the graphene Dirac states are located at the Fermi level and are well preserved. The parabolic spin down band above the Dirac cone originates from the magnetic substrate. In Fig. 2(b) we show a zoom to the low energy Dirac bands near the  $K$  point. We find that the model perfectly agrees with the DFT-calculated dispersion by using the parameters summarized in Table II. In this ferromagnetic case, uniform exchange parameters  $\lambda_{\text{ex}}^A \approx \lambda_{\text{ex}}^B \approx -0.8$  meV are found. The calculated positive and uniform spin polarization on graphene is consistent with this picture, see the Supplemental Material [119]. The staggered potential  $\Delta$  is small ( $\approx 10$   $\mu\text{eV}$ ), indicating that nearly no sublattice symmetry breaking is present. The orbital hopping parameters  $t_s$  are only slightly different for the two spin species. Using these parameters, not only the dispersion but also the band splittings, of about 1.7 meV, can be perfectly reproduced, see Fig. 2(c).

#### B. Antiferromagnetic Néel phase

Second, we consider the  $\text{MnPS}_3$  monolayer to be in the antiferromagnetic Néel phase, which is the ground state for this material. As before, we calculate the dispersion and employ our model Hamiltonian. Again, the heterostructure has a threefold symmetry in the antiferromagnetic Néel phase and we can use  $t_{1,s} = t_{2,s} = t_{3,s}$  for the fitting procedure. The calculation and fitting results are summarized in Fig. 3. The Dirac bands of graphene are again well preserved and located at the Fermi level. Also the model agrees perfectly with the

TABLE II. Fit parameters of Hamiltonian  $\mathcal{H}$  for the graphene/ $MPX_3$  heterostructures for different magnetic phases (FM = ferromagnetic, AFM = antiferromagnetic) of the  $MPX_3$ . Calculations were performed without SOC. We list the hopping parameters  $t_{\alpha,s}$ , the staggered potential  $\Delta$ , proximity exchange parameters  $\lambda_{\text{ex}}^A$  and  $\lambda_{\text{ex}}^B$ , the Dirac point energy  $E_D$ , and the total energy  $E_{\text{tot}}$ , with respect to the ground state.

$MPX_3$	Magnetic phase	$t_{1,\uparrow}, t_{2,\uparrow}, t_{3,\uparrow}/t_{1,\downarrow}, t_{2,\downarrow}, t_{3,\downarrow}$ (eV)	$\Delta$ ( $\mu\text{eV}$ )	$\lambda_{\text{ex}}^A$ ( $\mu\text{eV}$ )	$\lambda_{\text{ex}}^B$ ( $\mu\text{eV}$ )	$E_D$ (meV)	$E_{\text{tot}}$ (meV)
MnPS <sub>3</sub>	FM	2.5038/2.5030	19.2	-219.6	-220.1	-0.047	231.4
	AFM Néel	2.5032/2.5032	42.3	-11.4	-13.0	0.029	0
	AFM zigzag	2.5057,2.5032,2.5008/2.4997,2.5021,2.5046	629.2	469.5	463.1	0.060	91.8
	AFM stripy	2.5035,2.5034,2.5033/2.5030,2.5032,2.5035	112.3	41.3	43.8	0.007	116.4
	FM <sup>a</sup>	2.5083/2.5070	68.9	-215.0	-232.9	-0.004	164.9
MnPS <sub>3</sub>	AFM Néel <sup>a</sup>	2.5088/2.5086	67.7	20.2	-38.5	-0.001	0
	FM	2.6144/2.6093	13.2	-850.9	-828.5	-0.004	238.8
	AFM Néel	2.6126/2.6126	52.9	-17.0	8.2	0.007	0
	AFM zigzag	2.6136,2.6116,2.6097/2.6100,2.6120,2.6140	496.6	362.4	383.2	0.073	103.5
	AFM stripy	2.6123,2.6122,2.6122/2.6120,2.6122,2.6124	32.9	35.1	12.0	-0.041	113.7
FePSe <sub>3</sub>	FM <sup>a</sup>	2.6192/2.6109	24.5	-954.3	-1016.3	0.031	212.4
	AFM Néel <sup>a</sup>	2.6173/2.6173	35.4	14.6	-19.2	0.001	0
	FM	2.5050/2.3475	3261.2	992.2	-5926.5	-8.6	1511.1
	AFM Néel <sup>b</sup>	-	-	-	-	-	1040.1
	AFM zigzag	2.5054,2.5027,2.5015/2.5003,2.5026,2.5039	289.3	196.4	428.3	-0.001	0
FePS <sub>3</sub>	AFM stripy	2.5028,2.5028,2.5031/2.4988,2.4997,2.5006	196.7	99.2	-94.1	0.880	275.5
	FM	2.6151/2.5824	364.7	430.8	-786.4	331.5	1735.0
	AFM Néel	2.6110/2.6109	126.9	-14.7	-63.2	550.9	1451.7
	AFM zigzag	2.5996,2.5936,2.5891/2.6003,2.6019,2.6051	570.7	668.5	458.4	-0.229	0
	AFM stripy	2.5452,2.5343,2.5470/2.5347,2.5429,2.5446	342.1	-183.9	455.0	-0.034	134.5
NiPSe <sub>3</sub>	FM	2.5036/1.9911	53.7	10764.4	10575.8	85.0	479.0
	AFM Néel	2.4797/2.4795	75.7	-36.0	-0.7	0.018	82.0
	AFM zigzag	2.4851,2.4814,2.4779/2.4858,2.4883,2.4907	655.3	549.4	609.2	-0.126	0
	AFM stripy <sup>b</sup>	-	-	-	-	-	535.7
	FM	2.6130/2.3893	860.3	1538.5	115.1	387.2	291.1
NiPS <sub>3</sub>	AFM Néel	2.5732/2.5755	114.6	53.1	-65.9	265.6	37.8
	AFM zigzag	2.1102,2.1146,2.1169/2.0470,2.0545,2.0610	79.3	144.9	303.6	293.7	0
	AFM stripy <sup>b</sup>	-	-	-	-	-	341.6
	FM	2.4221/2.5022	0.9	-3097.7	-3069.9	364.1	127.8
	AFM Néel	2.4786/2.4797	87.6	-91.7	39.5	363.4	1120.1
CoPSe <sub>3</sub>	AFM zigzag	2.4506,2.4461,2.4415/2.4526,2.4509,2.4495	346.8	-12.2	37.4	370.4	1306.7
	AFM stripy	2.4784,2.4781,2.4769/2.4848,2.4854,2.4847	65.2	55.9	-60.2	362.2	0
	FM	2.6103/2.5989	43.7	-1337.2	-1261.7	562.7	534.0
	AFM Néel	2.5280/2.5269	115.2	-63.8	25.3	0.103	19.2
	AFM zigzag	2.4576,2.4494,2.4414/2.5166,2.5237,2.5304	1371.3	1349.9	1442.2	0.067	0
CoPS <sub>3</sub>	AFM stripy <sup>b</sup>	-	-	-	-	-	229.9

<sup>a</sup>Calculated with WIEN2k [91].

<sup>b</sup>A reasonable fit could not be performed, as can be seen from the DFT-calculated band structure in the Supplemental Material.

DFT-calculated dispersion and band splittings, employing the parameters from Table II. Compared to the ferromagnetic phase, band splittings are drastically diminished in magnitude from about 1.7 meV to 20  $\mu\text{eV}$ . We can understand this by the following argument. In the antiferromagnetic Néel phase, the average proximity exchange on the graphene sublattices is reduced, because Mn atoms have alternating magnetizations. Therefore, the exchange field felt by graphene is strongly diminished. In contrast in the ferromagnetic phase, all Mn atoms have the same magnetization and proximity effects are much stronger. In addition, for the ferromagnetic phase, sublattice resolved proximity exchange parameters had the same sign, while for the antiferromagnetic Néel phase, we

find opposite sign,  $\lambda_{\text{ex}}^A < 0$  and  $\lambda_{\text{ex}}^B > 0$ . The calculated spin polarization, being opposite on the graphene sublattices, supports this result of staggered exchange couplings [119]. This is a very important finding, since the magnetic phase decides not only about the magnitude, but also the type of proximity exchange coupling, which can have dramatic consequences for topological phases in proximitized graphene [52].

### C. Antiferromagnetic zigzag phase

Third, we consider the MnPS<sub>3</sub> monolayer to be in the antiferromagnetic zigzag phase. Now, the heterostructure has no symmetry and nearest-neighbor hopping amplitudes are

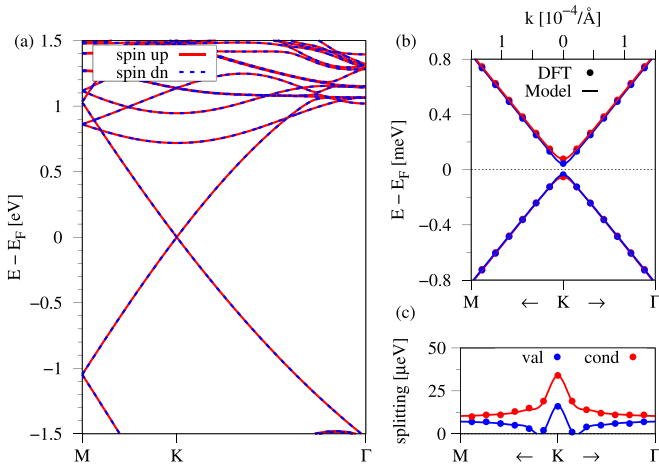


FIG. 3. Same as Fig. 2, but for the MnPS<sub>3</sub> in the antiferromagnetic Néel phase.

becoming inequivalent  $t_{1,s} \neq t_{2,s} \neq t_{3,s}$ . This asymmetry in the hopping amplitudes leads to the shift of the Dirac point in momentum space [120,121]. Because the system is additionally magnetic, spin up and spin down Dirac points do not need to be shifted equally away from the  $K$  point. In the Supplemental Material [119] we explicitly show a 2D map of the low energy Dirac bands in momentum space, corresponding to Fig. 4(b). Especially in this case we take into account DFT-calculated bands not along a high-symmetry path, but in a small  $k$ -space region around the  $K$  point, to obtain accurate fitting results. In Fig. 4 we summarize our calculation and fit results for the graphene/MnPS<sub>3</sub> heterostructure when the MnPS<sub>3</sub> is in the antiferromagnetic zigzag phase. The global band structure of the zigzag and the Néel phases are quite similar at first glance. However, proximity-induced exchange coupling in graphene is completely different and the Dirac cones for spin up and spin down are indeed shifted in momentum space, see Fig. 4(b). As a result, band splittings are strongly direction dependent, see Fig. 4(c). However, our model is also capable of describing this situation with parameters sum-

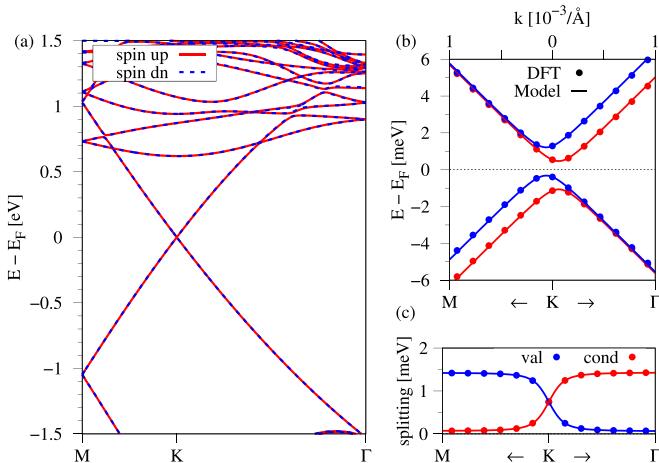


FIG. 4. Same as Fig. 2, but for the MnPS<sub>3</sub> in the antiferromagnetic zigzag phase.

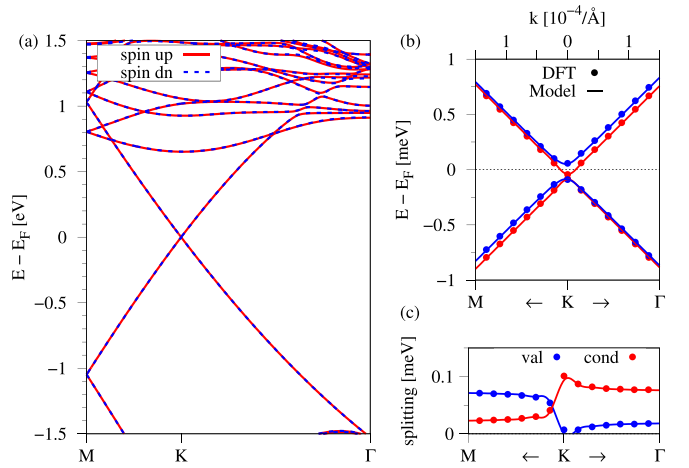


FIG. 5. Same as Fig. 2, when the MnPS<sub>3</sub> is in the antiferromagnetic stripy phase.

marized in Table II, as can be seen in Figs. 4(b) and 4(c). Interestingly, sublattice-resolved proximity exchange parameters of the antiferromagnetic zigzag phase are about 0.4 meV in magnitude, half of the value and opposite in sign compared to the ferromagnetic case, see Table II. Comparing the calculated spin polarizations on graphene in the ferromagnetic and antiferromagnetic zigzag phases [119], the opposite sign of proximity exchange is reasonable. In addition, the staggered potential parameter  $\Delta$  is drastically enhanced compared to the other phases. Therefore, mainly one sublattice contributes to the spin polarization in the antiferromagnetic zigzag phase, while in the ferromagnetic phase, both sublattices contribute equally.

So far we have seen all types of sublattice-resolved proximity-induced exchange coupling in graphene, uniform (positive and negative) and staggered, only by changing the magnetic phase of the MnPS<sub>3</sub> substrate.

#### D. Antiferromagnetic stripy phase

Finally, we consider the MnPS<sub>3</sub> monolayer to be in the antiferromagnetic stripy phase. The calculated band structure and low energy fit results are shown in Fig. 5. Similar to the zigzag phase, the heterostructure has no symmetry and hopping amplitudes become inequivalent  $t_{1,s} \neq t_{2,s} \neq t_{3,s}$ . All relevant features of the dispersion are nearly identical to the antiferromagnetic zigzag phase. The main difference is that sublattice resolved proximity exchange couplings and Dirac band splittings are much smaller in magnitude. Looking at the calculated spin polarization in real space [119], we find a similar picture as for the antiferromagnetic Néel phase, with opposite polarizations on the graphene sublattices. This scenario arises due to the small sublattice symmetry breaking  $\Delta$  and small but uniform exchange parameters  $\lambda_{ex}$  in combination with slightly asymmetric hoppings.

In order to unveil specific trends on how the proximity-induced exchange depends on the specific material and magnetic phase, we plot in Fig. 6 the average coupling  $\lambda_{ex} = (\lambda_{ex}^A + \lambda_{ex}^B)/2$  (listed in Table II). We only show the results for the ferromagnetic, antiferromagnetic Néel, and antiferromagnetic zigzag phases, since in the antiferromagnetic stripy

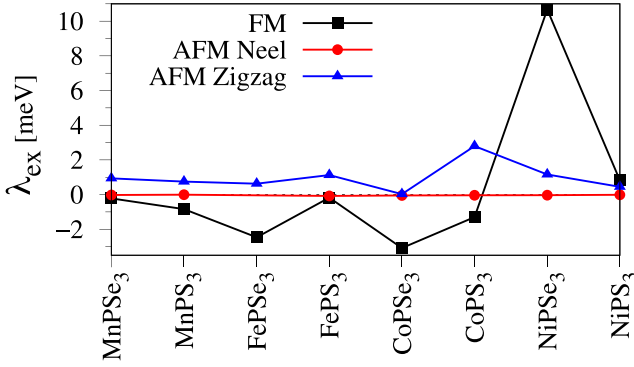


FIG. 6. The average proximity exchange coupling  $\lambda_{\text{ex}}$  as a function of the substrate material and the magnetic phase (FM = ferromagnetic, AFM = antiferromagnetic).

phase we do not have data for all material combinations. In addition, the stripy phase is only energetically favorable in the case of CoPS<sub>3</sub>.

Let us first discuss the dependence in the ferromagnetic phase (black data points). From Fig. 6 it is evident that  $\lambda_{\text{ex}}$  increases in magnitude in ascending order of the transition metal (Mn, Fe, Co, Ni), for Se-based MPX<sub>3</sub> materials. In addition, Mn, Fe, and Co provide negative  $\lambda_{\text{ex}}$ , while Ni provides positive  $\lambda_{\text{ex}}$ . The reason for the increasing magnitude can be seen from the density of states (DOS), see the Supplemental Material [119]. Focusing on Se-based materials, the transition metal DOS contribution near the Dirac point continuously increases from Mn to Ni. Since these states from the transition metals provide magnetism and can couple to the Dirac electrons, the proximity exchange increases. In general it also seems that Se-based materials provide stronger proximity exchange compared to S-based ones. Focusing on the two antiferromagnetic phases (red and blue data points), we find that proximity exchange is much more suppressed compared to the ferromagnetic phase. This can be understood from the fact that an antiferromagnetic substrate has alternating magnetizations and therefore the exchange field that graphene can pick-up is diminished. In general, the antiferromagnetic Néel phase provides the smallest proximity exchange in graphene, while the antiferromagnetic zigzag phase can still provide moderate exchange coupling. This may be attributed to the different arrangements of magnetic metal ions below graphene. In the Néel phase, magnetic ions with different magnetization orientations form a regular pattern (considering one metal ion, the three nearest neighbors have opposite magnetizations). In contrast, in the zigzag phase, there are at least small “domains” (zigzag stripes), where the magnetization is uniform (considering one metal ion, two nearest neighbors have the same magnetization).

### E. Distance study

Proximity exchange coupling is a short range effect and can be strongly enhanced by diminishing the interlayer distance between materials, as experimentally demonstrated for proximity SOC in graphene/TMDC heterostructures [94,122]. In addition, in first-principles calculations, the equilibrium interlayer distance depends on the exchange-correlation functional

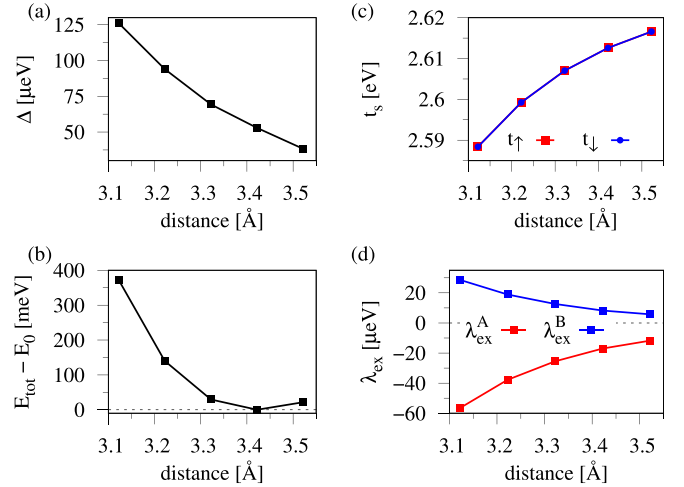


FIG. 7. Interlayer distance dependence of (a) the staggered potential  $\Delta$ , (b) the total energy  $E_{\text{tot}}$ , (c) the spin dependent hopping parameters  $t_{\uparrow}$  and  $t_{\downarrow}$ , and (d) the sublattice resolved proximity exchange parameters  $\lambda_{\text{ex}}^{\text{A}}$  and  $\lambda_{\text{ex}}^{\text{B}}$  for the graphene/MnPS<sub>3</sub> heterostructure when the MnPS<sub>3</sub> is in the antiferromagnetic Néel phase.

and the vdW corrections, as for example demonstrated for graphite and hexagonal boron nitride [123].

How does the interlayer distance affect proximity exchange effects in our bilayers? As an exemplary case we consider MnPS<sub>3</sub> in the antiferromagnetic Néel phase (ground state) and tune the distance  $d_{\text{int}}$  between graphene and the MnPS<sub>3</sub> monolayer. Especially this structure is interesting, since sublattice resolved proximity exchange parameters have opposite sign,  $\lambda_{\text{ex}}^{\text{A}} < 0$  and  $\lambda_{\text{ex}}^{\text{B}} > 0$ , see Table II, potentially important for the realization of novel topological states [52].

In Fig. 7 we show the evolution of the fit parameters and the total energy as a function of the interlayer distance for the graphene/MnPS<sub>3</sub> heterostructure. We notice that the staggered potential  $\Delta$  increases with decreasing distance, because the sublattice-symmetry breaking in graphene gets stronger. The total energy is minimized for the relaxed interlayer distance given in Table I. The two spin dependent hopping parameters  $t_{\uparrow}$  and  $t_{\downarrow}$  have nearly the same value for this system, as can be seen in Table II, and decrease with decreasing van der Waals gap. The proximity exchange parameters  $\lambda_{\text{ex}}^{\text{A}}$  and  $\lambda_{\text{ex}}^{\text{B}}$  increase in magnitude with decreasing interlayer distance. We find that by decreasing  $d_{\text{int}}$  by about 10%, one can achieve a significant fivefold enhancement of proximity exchange couplings. Important, the sign of both parameters  $\lambda_{\text{ex}}^{\text{A}} < 0$  and  $\lambda_{\text{ex}}^{\text{B}} > 0$  is not affected.

In the Supplemental Material [119] we additionally show the evolution of the fit parameters as a function of the interlayer distance for the graphene/MnPS<sub>3</sub> heterostructure in the antiferromagnetic Néel phase. There we even find a crossover from uniform to staggered exchange couplings, when decreasing the interlayer distance. In conclusion, we expect similar behavior for the other material combinations and the different magnetic phases.

### F. Hubbard $U$

The Hubbard  $U$  parameter is variable for the DFT calculations. How does the  $U$  affect proximity exchange splittings?

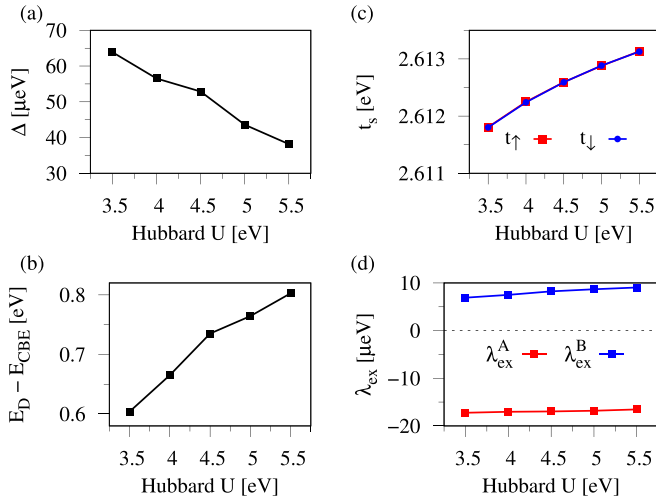


FIG. 8. Hubbard  $U$  dependence of (a) the staggered potential  $\Delta$ , (b) the band offset of the Dirac point  $E_D$ , with respect to the  $\text{MnPS}_3$  conduction band edge,  $E_{CBE}$ , at the  $K$  point, (c) the spin dependent hopping parameters  $t_\uparrow$  and  $t_\downarrow$ , and (d) the sublattice resolved proximity exchange parameters  $\lambda_{ex}^A$  and  $\lambda_{ex}^B$  for the graphene/ $\text{MnPS}_3$  heterostructure when the  $\text{MnPS}_3$  is in the antiferromagnetic Néel phase.

Again, we consider graphene on  $\text{MnPS}_3$  in the antiferromagnetic Néel phase and tune the  $U$  parameter between 3.5 and 5.5 eV, which is a typical range of values for  $d$  orbitals in strongly correlated materials. The results are summarized in Fig. 8. Overall, the fit parameters  $\Delta$ ,  $t_\uparrow$ ,  $t_\downarrow$ ,  $\lambda_{ex}^A$ , and  $\lambda_{ex}^B$ , barely change because for the graphene/ $\text{MnPS}_3$  heterostructure, the Dirac bands are located at the Fermi level and well isolated from the substrate's bands, see Fig. 3(a). Even though the Hubbard  $U$  shifts the Mn  $d$  orbital levels in energy and tunes the band offset, the graphene states are nearly unaffected.

However, the effect of the Hubbard  $U$  on the fitted parameters can be also quite strong, as we demonstrate in the case of  $\text{NiPSe}_3$  in the antiferromagnetic zigzag phase (see the Supplemental Material [119]). There, we find that proximity exchange couplings can be tuned from about 400 to 700 μeV within our considered range of the  $U$  parameter.

### G. Transverse electric field

In experiment, gating is a tool to control proximity-induced exchange coupling as well as the doping level. How does a transverse electric field affect the Dirac bands in our scenario? Similar to before, we consider graphene on  $\text{MnPS}_3$  in the antiferromagnetic Néel phase and apply an electric field across the heterostructure. The results are summarized in Fig. 9. Within our calculated field range of  $-2$  to  $3$  V/nm, we find that the fitted parameters barely change. Most important, we can strongly tune the band offset of the Dirac point  $E_D$  with respect to the  $\text{MnPS}_3$  conduction band edge  $E_{CBE}$  at the  $K$  point, see Fig. 9(b). For a field of  $3$  V/nm, we can bring the Dirac point at about  $0.25$  eV below the conduction band edge of the  $\text{MnPS}_3$ . In addition, it seems that the closer the Dirac cone gets to the conduction band edge, staggered potential and exchange couplings increase, while the hopping amplitudes decrease. Even though the proximity exchange couplings are

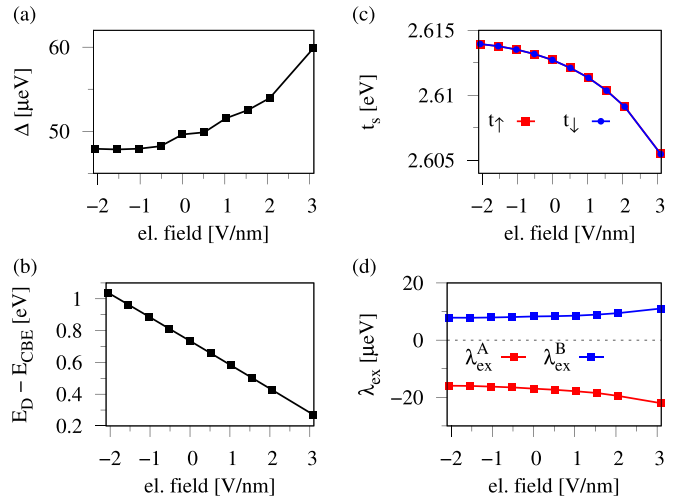


FIG. 9. Transverse electric field dependence of (a) the staggered potential  $\Delta$ , (b) the band offset of the Dirac point  $E_D$ , with respect to the  $\text{MnPS}_3$  conduction band edge  $E_{CBE}$  at the  $K$  point, (c) the spin dependent hopping parameters  $t_\uparrow$  and  $t_\downarrow$ , and (d) the sublattice resolved proximity exchange parameters  $\lambda_{ex}^A$  and  $\lambda_{ex}^B$  for the graphene/ $\text{MnPS}_3$  heterostructure when the  $\text{MnPS}_3$  is in the antiferromagnetic Néel phase.

small in value, their relative tunability is giant, since they can be enhanced by about 30% by tuning the field from  $-2$  to  $3$  V/nm. In general, the tunability should hold also for other magnetic phases, where proximity exchange is stronger.

### H. Effects of SOC

So far we have not included SOC in the calculations. Since the number of possible heterostructures in different magnetic phases is too large, we limit ourselves to a few selected cases and check how the inclusion of SOC influences the low energy graphene Dirac bands. For simplicity, we only consider Mn-based  $\text{MPX}_3$  monolayers in the ferromagnetic phase. This should be enough to find out about the magnitude of the proximity-induced SOC, which we can compare to the induced exchange coupling. In addition, when SOC is included, we employ constrained magnetization calculations (forcing the magnetization parallel to  $z$  direction), since QUANTUM ESPRESSO implements noncollinear magnetism. Note, that the plane wave and pseudopotential method, implemented in QUANTUM ESPRESSO, does not correctly reproduce the intrinsic SOC values of bare monolayer graphene ( $12$  μeV), since the relevant  $d$  orbitals are not present [124,125]. However, proximity-induced SOC (if present) is captured.

In Fig. 10 we show the DFT-calculated low energy bands near the  $K$  and  $K'$  points of the graphene/ $\text{MnPS}_3$  heterostructure, when  $\text{MnPS}_3$  is in the ferromagnetic phase and SOC is included. We find that bands near the  $K$  and  $K'$  valleys are nearly identical and fully  $s_z$  polarized, indicating that proximity-induced SOC is negligible compared to the exchange one. Indeed, comparing the calculated low energy bands from Fig. 10 (with SOC) and Fig. 2 (without SOC), we find no marked change by inclusion of SOC. This result is not surprising, because recent calculations have shown that SOC effects are small in bare monolayer  $\text{MnPS}_3$  in the antiferro-



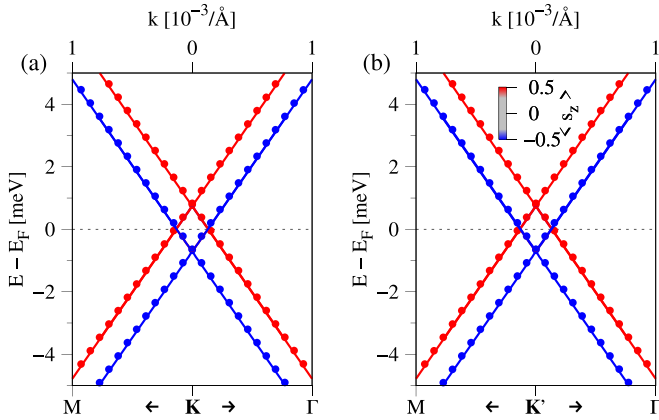


FIG. 10. (a) DFT-calculated low energy Dirac bands near the  $K$  point for the graphene/ $\text{MnPS}_3$  heterostructure, when  $\text{MnPS}_3$  is in the ferromagnetic phase and SOC is included. The symbols are color coded by their  $s_z$  spin expectation value. (b) Same as (a) but near the  $K'$  point.

magnetic Néel phase [68]. Therefore, also proximity-induced SOC is small, even though we consider the ferromagnetic phase here. Similar results hold for  $\text{MnPSe}_3$  in the ferromagnetic phase (low-energy dispersions with SOC are not shown).

### I. Further discussion

In some cases, band hybridization (anticrossings) additionally affect the Dirac bands, leading to renormalized proximity-induced exchange splittings, as previously shown for graphene/hBN/Co heterostructures [104]. Similar things can happen here, for example in the case of graphene/ $\text{NiPSe}_3$  in the ferromagnetic phase, spin down bands originating from the  $\text{NiPSe}_3$  are located near the Dirac point energy and hybridize with the spin down Dirac states, see the band structure in the Supplemental Material [119]. As a consequence, the effective proximity exchange parameters are much larger (10 meV) than for any other case we consider here. Also the spin down hopping parameter  $t_\downarrow$  differs by about 0.5 eV from the spin up one  $t_\uparrow$ , see Table II. For the graphene/ $\text{NiPS}_3$  structure in the antiferromagnetic zigzag phase, the band hybridization is even more pronounced, since  $\text{NiPS}_3$  bands from both spin species are present near the Dirac point.

Whenever bands, which originate from the magnetic  $\text{MPX}_3$  substrate, are located near the Dirac point energy, band hybridization can occur. As a consequence, the spin splitting of the graphene Dirac states is affected, in addition to the bare proximity-induced exchange coupling. By comparing the band structures and fitted parameters from all of our structures, this happens only in a few cases we consider here. However, from previous studies [104,126], we know that band offsets can be influenced by the interlayer distance, a transverse electric field, or the Hubbard  $U$ . In our exemplary case of  $\text{MnPS}_3$  in the antiferromagnetic Néel phase, we have seen that the interlayer distance strongly affects proximity exchange, while the Hubbard  $U$  does not, since band hybridization effects are absent (given the large band offset). This behavior can be very different in other heterostructures, especially in cases where band hybridization already occurs.

Does another DFT code give similar results? We additionally employ the full-potential linearized augmented plane wave code WIEN2k [91] and recalculate the dispersion for some of our structures. The fit results are also summarized in Table II. We consider graphene on  $\text{MnPS}_3$  and  $\text{MnPSe}_3$  in the ferromagnetic and antiferromagnetic Néel phases, respectively. Because of the broken symmetry in the antiferromagnetic zigzag and stripy phases, WIEN2k calculations are computationally too demanding and thus not included in this study. The purpose to employ two different codes is to test the robustness of our predictions (magnitudes and signs of proximity exchange parameters).

Both codes predict the antiferromagnetic Néel phase to be the ground state for  $\text{MnPSe}_3$  and  $\text{MnPS}_3$ , in agreement with experimental data. For both substrates in both magnetic phases, WIEN2k predicts similar proximity exchange splittings as QUANTUM ESPRESSO. For  $\text{MnPSe}_3$ , results of the antiferromagnetic Néel phase differ. The different DFT codes predict small exchange parameters, but of different type (WIEN2k predicts staggered ones, while QUANTUM ESPRESSO predicts uniform ones). For  $\text{MnPS}_3$  in the antiferromagnetic Néel phase, the sublattice resolved proximity exchange parameters are staggered for both codes, but with a global sign change. The results for the ferromagnetic phases coincide for both materials and both codes. Indeed, when proximity exchange is larger than about 100  $\mu\text{eV}$ , both codes essentially agree, as we can see from the ferromagnetic phase results. However, when the proximity effects become rather small (few to tens of  $\mu\text{eV}$ ), the codes reach their limits in numerical accuracy and discrepancies may arise, as we can see from the antiferromagnetic Néel phase results. We conclude that, whenever exchange parameters are small (few to tens of  $\mu\text{eV}$ ), a precise prediction of results is computationally very challenging and the extracted parameters should be treated with caution. However, we do not see this as a critical problem, since the magnitudes of the proximity exchange in the different magnetic phases are the same, independent of the DFT code. The proximity effects depend on the hybridization of the orbitals across the interface, and on the energies of the orbitals that take part of the hybridizations. The energetics of higher lying orbitals depends on the code, which is most likely causing the discrepancies.

Finally, we want to comment on the magnetic easy axis of the substrate  $\text{MPX}_3$  materials. In our calculations we have considered only out-of-plane (collinear to  $z$  direction) magnetic configurations. Otherwise, the calculations would be computationally very demanding since noncollinear magnetism needs to be treated, which is accompanied by inclusion of SOC. However, for some  $\text{MPX}_3$  monolayers, experiments and theory indicate in-plane antiferromagnetism, such as for  $\text{NiPS}_3$  [56,117]. Therefore, one should keep in mind that our presented results of proximity exchange may be different in real samples. With our DFT approach, we can give at most rough predictions and indications. Nevertheless, we find that the class of magnetic  $\text{MPX}_3$  monolayers is highly interesting in terms of proximity effects, as different types and magnitudes of exchange coupling can be induced in graphene. We also hope that future experiments can confirm at least some of our findings and that the potential of these materials will be recognized for future spintronics applications.

## V. SUMMARY

In this work we have considered heterostructures of graphene and the magnetic transition-metal phosphorus trichalcogenides  $MPX_3$ . From first-principles calculations, we have extracted the proximitized Dirac bands of graphene, which we fitted to a model Hamiltonian, including orbital and proximity exchange parameters. We found that, depending on the magnetic phase of the  $MPX_3$  substrate layer, the metal atom  $M = \{\text{Mn, Fe, Ni, Co}\}$ , and the chalcogen atom  $X = \{\text{S, Se}\}$ , very different proximity-induced exchange couplings can be realized in graphene. Not only that the exchange splittings range from about 0 to 10 meV, also the sign and type of the exchange couplings differ from case to case. We demonstrated, that the  $MPX_3$  family of magnetic monolayers are a platform to induce uniform ( $\lambda_{\text{ex}}^{\text{A}} \approx \lambda_{\text{ex}}^{\text{B}}$ ), as well as staggered ( $\lambda_{\text{ex}}^{\text{A}} \approx -\lambda_{\text{ex}}^{\text{B}}$ ) exchange couplings in graphene, leading to very different spin polarizations. In addition, decreasing the interlayer distance between graphene and the substrate is

a very efficient tool to enhance proximity-induced exchange couplings. An applied transverse electric field can potentially result in a similar tunability, but was not observed in our exemplary case. The Hubbard  $U$ , which is a parameter in the DFT calculation, can have a huge impact on Dirac band splittings, since the  $U$  determines the band alignment and to some extent the coupling of the monolayers. Finally, we found that for Mn-based materials in the ferromagnetic phase, the proximity-induced SOC is negligible compared to the exchange parameters.

## ACKNOWLEDGMENTS

This work was funded by the Deutsche Forschungsgemeinschaft (DFG, German Research Foundation) SFB 1277 (Project No. 314695032), SPP 2244 (Project No. 443416183), and the European Union Horizon 2020 Research and Innovation Program under Contract No. 881603 (Graphene Flagship).

- 
- [1] K. Zollner, M. D. Petrović, K. Dolui, P. Plecháč, B. K. Nikolić, and J. Fabian, Scattering-induced and highly tunable by gate damping-like spin-orbit torque in graphene doubly proximitized by two-dimensional magnet  $\text{Cr}_2\text{Ge}_2\text{Te}_6$  and monolayer  $\text{WS}_2$ , *Phys. Rev. Research* **2**, 043057 (2020).
- [2] K. Dolui, M. D. Petrovic, K. Zollner, P. Plechac, J. Fabian, and B. K. Nikolic, Proximity spin-orbit torque on a two-dimensional magnet within van der Waals heterostructure: Current-driven antiferromagnet-to-ferromagnet reversible nonequilibrium phase transition in bilayer  $\text{CrI}_3$ , *Nano Lett.* **20**, 2288 (2020).
- [3] T. Song, X. Cai, M. W.-Y. Tu, X. Zhang, B. Huang, N. P. Wilson, K. L. Seyler, L. Zhu, T. Taniguchi, K. Watanabe, M. A. McGuire, D. H. Cobden, D. Xiao, W. Yao, and X. Xu, Giant tunneling magnetoresistance in spin-filter van der Waals heterostructures, *Science* **360**, 1214 (2018).
- [4] M. Alghamdi, M. Lohmann, J. Li, P. R. Jothi, Q. Shao, M. Aldosary, T. Su, B. P. T. Fokwa, and J. Shi, Highly efficient spin-orbit torque and switching of layered ferromagnet  $\text{Fe}_3\text{GeTe}_2$ , *Nano Lett.* **19**, 4400 (2019).
- [5] V. Ostwal, T. Shen, and J. Appenzeller, Efficient spin-orbit torque switching of the semiconducting van der Waals ferromagnet  $\text{Cr}_2\text{Ge}_2\text{Te}_6$ , *Adv. Mater.* **32**, 1906021 (2020).
- [6] B. Zhao, R. Ngaloy, A. Md Hoque, B. Karpiak, D. Khokhriakov, and S. P. Dash, Van der Waals magnet based spin-valve devices at room temperature, [arXiv:2107.00310](https://arxiv.org/abs/2107.00310).
- [7] W. Han, K. Pi, K. M. McCreary, Y. Li, J. J. I. Wong, A. G. Swartz, and R. K. Kawakami, Tunneling Spin Injection into Single Layer Graphene, *Phys. Rev. Lett.* **105**, 167202 (2010).
- [8] G. Schmidt, D. Ferrand, L. W. Molenkamp, A. T. Filip, and B. J. van Wees, Fundamental obstacle for electrical spin injection from a ferromagnetic metal into a diffusive semiconductor, *Phys. Rev. B* **62**, R4790 (2000).
- [9] E. I. Rashba, Theory of electrical spin injection: Tunnel contacts as a solution of the conductivity mismatch problem, *Phys. Rev. B* **62**, R16267 (2000).
- [10] W. Han, R. K. Kawakami, M. Gmitra, and J. Fabian, Graphene spintronics, *Nat. Nanotechnol.* **9**, 794 (2014).
- [11] A. Fert and H. Jaffres, Conditions for efficient spin injection from a ferromagnetic metal into a semiconductor, *Phys. Rev. B* **64**, 184420 (2001).
- [12] T. S. Ghiasi, A. A. Kaverzin, A. H. Dismukes, D. K. de Wal, X. Roy, and B. J. van Wees, Electrical and thermal generation of spin currents by magnetic bilayer graphene, *Nat. Nanotechnol.* **16**, 788 (2021).
- [13] A. A. Kaverzin, T. S. Ghiasi, A. H. Dismukes, X. Roy, and B. J. van Wees, Towards fully two-dimensional spintronic devices, [arXiv:2202.09972](https://arxiv.org/abs/2202.09972).
- [14] D. Khokhriakov, S. Sayed, A. Md Hoque, B. Karpiak, B. Zhao, S. Datta, and S. P. Dash, Multifunctional spin logic gates in graphene spin circuits, [arXiv:2108.12259](https://arxiv.org/abs/2108.12259).
- [15] D. Khokhriakov, B. Karpiak, A. Md. Hoque, and S. P. Dash, Two-dimensional spintronic circuit architectures on large scale graphene, *Carbon* **161**, 892 (2020).
- [16] M. Gmitra and J. Fabian, Graphene on transition-metal dichalcogenides: A platform for proximity spin-orbit physics and optospintronics, *Phys. Rev. B* **92**, 155403 (2015).
- [17] M. Gmitra, D. Kochan, P. Högl, and J. Fabian, Trivial and inverted Dirac bands and the emergence of quantum spin Hall states in graphene on transition-metal dichalcogenides, *Phys. Rev. B* **93**, 155104 (2016).
- [18] Y. Li and M. Koshino, Twist-angle dependence of the proximity spin-orbit coupling in graphene on transition-metal dichalcogenides, *Phys. Rev. B* **99**, 075438 (2019).
- [19] A. David, P. Rakyta, A. Kormányos, and G. Burkard, Induced spin-orbit coupling in twisted graphene-transition metal dichalcogenide heterobilayers: Twistronics meets spintronics, *Phys. Rev. B* **100**, 085412 (2019).
- [20] T. Naimer, K. Zollner, M. Gmitra, and J. Fabian, Twist-angle dependent proximity induced spin-orbit coupling in graphene/transition metal dichalcogenide heterostructures, *Phys. Rev. B* **104**, 195156 (2021).
- [21] A. Pezo, Z. Zanolli, N. Wittemeier, P. Ordejón, A. Fazzio, S. Roche, and J. H. Garcia, Manipulation of spin transport in graphene/transition metal dichalcogenide heterobilayers upon twisting, *2D Mater.* **9**, 015008 (2021).

- [22] C. G. Péterfalvi, A. David, P. Rakyta, G. Burkard, and A. Kormányos, Quantum interference tuning of spin-orbit coupling in twisted van der Waals trilayers, *Phys. Rev. Research* **4**, L022049 (2022).
- [23] A. Veneri, D. T. S. Perkins, C. G. Péterfalvi, and A. Ferreira, Twist-angle controlled collinear Edelstein effect in van der Waals heterostructures, [arXiv:2205.08804](https://arxiv.org/abs/2205.08804).
- [24] S. Lee, D. J. P. de Sousa, Y.-K. Kwon, F. de Juan, Z. Chi, F. Casanova, and T. Low, Charge-to-spin conversion in twisted graphene/WSe<sub>2</sub> heterostructures, [arXiv:2206.09478](https://arxiv.org/abs/2206.09478).
- [25] L. A. Benitez, W. S. Torres, J. F. Sierra, M. Timmermans, J. H. Garcia, S. Roche, M. V. Costache, and S. O. Valenzuela, Tunable room-temperature spin galvanic and spin Hall effects in van der Waals heterostructures, *Nat. Mater.* **19**, 170 (2020).
- [26] M. Offidani, M. Milletari, R. Raimondi, and A. Ferreira, Optimal Charge-to-Spin Conversion in Graphene on Transition-Metal Dichalcogenides, *Phys. Rev. Lett.* **119**, 196801 (2017).
- [27] T. S. Ghiasi, A. A. Kaverzin, P. J. Blah, and B. J. van Wees, Charge-to-spin conversion by the Rashba–Edelstein effect in two-dimensional van der Waals heterostructures up to room temperature, *Nano Lett.* **19**, 5959 (2019).
- [28] D. Khokhriakov, A. Md. Hoque, B. Karpiak, and S. P. Dash, Gate-tunable spin-galvanic effect in graphene-topological insulator van der Waals heterostructures at room temperature, *Nat. Commun.* **11**, 3657 (2020).
- [29] F. Herling, C. K. Safeer, J. Ingla-Aynés, N. Ontoso, L. E. Hueso, and F. Casanova, Gate tunability of highly efficient spin-to-charge conversion by spin Hall effect in graphene proximitized with WSe<sub>2</sub>, *APL Mater.* **8**, 071103 (2020).
- [30] C. K. Safeer, F. Herling, W. Y. Choi, N. Ontoso, J. Ingla-Aynés, L. E. Hueso, and F. Casanova, Reliability of spin-to-charge conversion measurements in graphene-based lateral spin valves, *2D Mater.* **9**, 015024 (2022).
- [31] C. Monaco, A. Ferreira, and R. Raimondi, Spin Hall and inverse spin galvanic effects in graphene with strong interfacial spin-orbit coupling: A quasi-classical Green’s function approach, *Phys. Rev. Research* **3**, 033137 (2021).
- [32] A. Ferreira, Theory of spin-charge-coupled transport in proximitized graphene: An SO(5) algebraic approach, *J. Phys. Mater.* **4**, 045006 (2021).
- [33] M. Milletari, M. Offidani, A. Ferreira, and R. Raimondi, Covariant Conservation Laws and the Spin Hall Effect in Dirac-Rashba Systems, *Phys. Rev. Lett.* **119**, 246801 (2017).
- [34] A. Dyrdał, J. Barnaś, and V. K. Dugaev, Current-induced spin polarization in graphene due to Rashba spin-orbit interaction, *Phys. Rev. B* **89**, 075422 (2014).
- [35] J. H. Garcia, A. W. Cummings, and S. Roche, Spin Hall effect and weak antilocalization in graphene/transition metal dichalcogenide heterostructures, *Nano Lett.* **17**, 5078 (2017).
- [36] A. Md. Hoque, D. Khokhriakov, K. Zollner, B. Zhao, B. Karpiak, J. Fabian, and S. P. Dash, All-electrical creation and control of spin-galvanic signal in graphene and molybdenum ditelluride heterostructures at room temperature, *Commun. Phys.* **4**, 124 (2021).
- [37] R. Galceran, B. Tian, J. Li, F. Bonell, M. Jamet, C. Vergnaud, A. Marty, J. H. García, J. F. Sierra, M. V. Costache, S. Roche, S. O. Valenzuela, A. Manchon, X. Zhang, and U. Schwingenschlögl, Control of spin-charge conversion in van der Waals heterostructures, *APL Mater.* **9**, 100901 (2021).
- [38] A. W. Cummings, J. H. Garcia, J. Fabian, and S. Roche, Giant Spin Lifetime Anisotropy in Graphene Induced by Proximity Effects, *Phys. Rev. Lett.* **119**, 206601 (2017).
- [39] T. S. Ghiasi, J. Ingla-Aynés, A. A. Kaverzin, and B. J. Van Wees, Large proximity-induced spin lifetime anisotropy in transition-metal dichalcogenide/graphene heterostructures, *Nano Lett.* **17**, 7528 (2017).
- [40] S. Zihlmann, A. W. Cummings, J. H. Garcia, M. Kedves, K. Watanabe, T. Taniguchi, C. Schönberger, and P. Makk, Large spin relaxation anisotropy and valley-Zeeman spin-orbit coupling in WSe<sub>2</sub>/graphene/h-BN heterostructures, *Phys. Rev. B* **97**, 075434 (2018).
- [41] J. C. Leutenantsmeyer, J. Ingla-Aynés, J. Fabian, and B. J. van Wees, Observation of Spin-Valley-Coupling-Induced Large Spin-Lifetime Anisotropy in Bilayer Graphene, *Phys. Rev. Lett.* **121**, 127702 (2018).
- [42] S. Omar, B. N. Madhushankar, and B. J. van Wees, Large spin-relaxation anisotropy in bilayer-graphene/WS<sub>2</sub> heterostructures, *Phys. Rev. B* **100**, 155415 (2019).
- [43] M. Offidani and A. Ferreira, Microscopic theory of spin relaxation anisotropy in graphene with proximity-induced spin-orbit coupling, *Phys. Rev. B* **98**, 245408 (2018).
- [44] J. Zhang, B. Zhao, Y. Yao, and Z. Yang, Robust quantum anomalous Hall effect in graphene-based van der Waals heterostructures, *Phys. Rev. B* **92**, 165418 (2015).
- [45] B. Karpiak, A. W. Cummings, K. Zollner, M. Vila, D. Khokhriakov, A. Md. Hoque, A. Dankert, P. Svedlindh, J. Fabian, S. Roche, and S. P. Dash, Magnetic proximity in a van der Waals heterostructure of magnetic insulator and graphene, *2D Mater.* **7**, 015026 (2020).
- [46] J. Zhang, B. Zhao, T. Zhou, Y. Xue, C. Ma, and Z. Yang, Strong magnetization and Chern insulators in compressed graphene/CrI<sub>3</sub> van der Waals heterostructures, *Phys. Rev. B* **97**, 085401 (2018).
- [47] M. U. Farooq and J. Hong, Switchable valley splitting by external electric field effect in graphene/CrI<sub>3</sub> heterostructures, *npj 2D Mater. Appl.* **3**, 3 (2019).
- [48] C. Cardoso, D. Soriano, N. A. García-Martínez, and J. Fernández-Rossier, Van der Waals Spin Valves, *Phys. Rev. Lett.* **121**, 067701 (2018).
- [49] K. L. Seyler, D. Zhong, B. Huang, X. Linpeng, N. P. Wilson, T. Taniguchi, K. Watanabe, W. Yao, D. Xiao, M. A. McGuire, K.-M. C. Fu, and X. Xu, Valley manipulation by optically tuning the magnetic proximity effect in WSe<sub>2</sub>/CrI<sub>3</sub> heterostructures, *Nano Lett.* **18**, 3823 (2018).
- [50] K. Zollner and J. Fabian, Engineering Proximity Exchange by Twisting: Reversal of Ferromagnetic and Emergence of Antiferromagnetic Dirac Bands in Graphene/Cr<sub>2</sub>Ge<sub>2</sub>Te<sub>6</sub>, *Phys. Rev. Lett.* **128**, 106401 (2022).
- [51] S. Yan, S. Qi, D. Wang, and W. Mi, Novel electronic structures and magnetic properties in twisted two-dimensional graphene/Janus 2H-VSeTe heterostructures, *Phys. E* **134**, 114854 (2021).
- [52] P. Högl, T. Frank, K. Zollner, D. Kochan, M. Gmitra, and J. Fabian, Quantum Anomalous Hall Effects in Graphene from Proximity-Induced Uniform and Staggered Spin-Orbit and Exchange Coupling, *Phys. Rev. Lett.* **124**, 136403 (2020).

- [53] M. Vila, J. H. Garcia, and S. Roche, Valley-polarized quantum anomalous Hall phase in bilayer graphene with layer-dependent proximity effects, *Phys. Rev. B* **104**, L161113 (2021).
- [54] A. Wiedenmann, J. Rossat-Mignod, A. Louisy, R. Brec, and J. Rouxel, Neutron diffraction study of the layered compounds  $\text{MnPS}_3$  and  $\text{FePS}_3$ , *Solid State Commun.* **40**, 1067 (1981).
- [55] M. Ramos, F. Carrascoso, R. Frisenda, P. Gant, S. Mañas-Valero, D. L. Esteras, J. J. Baldoví, E. Coronado, A. Castellanos-Gomez, and M. R. Calvo, Ultra-broad spectral photo-response in  $\text{FePS}_3$  air-stable devices, *npj 2D Mater. Appl.* **5**, 19 (2021).
- [56] D. Lançon, R. A. Ewings, T. Guidi, F. Formisano, and A. R. Wildes, Magnetic exchange parameters and anisotropy of the quasi-two-dimensional antiferromagnet  $\text{NiPS}_3$ , *Phys. Rev. B* **98**, 134414 (2018).
- [57] H. Lu, W. Wang, Y. Liu, L. Chen, Q. Xie, H. Yin, G. Cheng, and L. He, Exfoliation, lattice vibration and air stability characterization of antiferromagnetic van der Waals  $\text{NiPS}_3$  nanosheets, *Appl. Surf. Sci.* **504**, 144405 (2020).
- [58] N. Sivasdas, M. W. Daniels, R. H. Swendsen, S. Okamoto, and D. Xiao, Magnetic ground state of semiconducting transition-metal trichalcogenide monolayers, *Phys. Rev. B* **91**, 235425 (2015).
- [59] G. L. Flem, R. Brec, G. Ouvar, A. Louisy, and P. Segransan, Magnetic interactions in the layer compounds  $\text{MPX}_3$  ( $M = \text{Mn, Fe, Ni}$ ;  $X = \text{S, Se}$ ), *J. Phys. Chem. Solids* **43**, 455 (1982).
- [60] J.-U. Lee, S. Lee, J. H. Ryoo, S. Kang, T. Y. Kim, P. Kim, C.-H. Park, J.-G. Park, and H. Cheong, Ising-type magnetic ordering in atomically thin  $\text{FePS}_3$ , *Nano Lett.* **16**, 7433 (2016).
- [61] B. L. Chittari, D. Lee, N. Banerjee, A. H. MacDonald, E. Hwang, and J. Jung, Carrier- and strain-tunable intrinsic magnetism in two-dimensional  $\text{MAX}_3$  transition metal chalcogenides, *Phys. Rev. B* **101**, 085415 (2020).
- [62] B. L. Chittari, Y. Park, D. Lee, M. Han, A. H. MacDonald, E. Hwang, and J. Jung, Electronic and magnetic properties of single-layer  $\text{MPX}_3$  metal phosphorous trichalcogenides, *Phys. Rev. B* **94**, 184428 (2016).
- [63] P. A. Joy and S. Vasudevan, Magnetism in the layered transition-metal thiophosphates  $\text{MPS}_3$  ( $M = \text{Mn, Fe, and Ni}$ ), *Phys. Rev. B* **46**, 5425 (1992).
- [64] Y. Li, X. Wu, Y. Gu, C. Le, S. Qin, R. Thomale, and J. Hu, Topological superconductivity in Ni-based transition metal trichalcogenides, *Phys. Rev. B* **100**, 214513 (2019).
- [65] W. Klingen, G. Eulenberger, and H. Hahn, Über hexathio- und hexaselenohypodiphosphate vom Typ  $M_2^{\text{II}} \text{P}_2\text{X}_6$ , *Naturwissenschaften* **55**, 229 (1968).
- [66] Q. Pei, X. Wang, J. Zou, and W. Mi, Tunable electronic structure and magnetic coupling in strained two-dimensional semiconductor  $\text{MnPS}_3$ , *Front. Phys.* **13**, 137105 (2018).
- [67] X. Li, T. Cao, Q. Niu, J. Shi, and J. Feng, Coupling the valley degree of freedom to antiferromagnetic order, *Proc. Natl. Acad. Sci.* **110**, 3738 (2013).
- [68] J. Yang, Y. Zhou, Q. Guo, Y. Dedkov, and E. Voloshina, Electronic, magnetic and optical properties of  $\text{MnPX}_3$  ( $X = \text{S, Se}$ ) monolayers with and without chalcogen defects: A first-principles study, *RSC Adv.* **10**, 851 (2020).
- [69] M. Nauman, D. H. Kiem, S. Lee, S. Son, J.-G. Park, W. Kang, M. J. Han, and Y. Jo, Complete mapping of magnetic anisotropy for prototype Ising van der Waals  $\text{FePS}_3$ , *2D Mater.* **8**, 035011 (2021).
- [70] C. Autieri, G. Cuono, C. Noce, M. Rybak, K. M. Kotur, C. E. Agrapidis, K. Wohlfeld, and M. Birowska, Limited ferromagnetic interactions in monolayers of  $\text{MPS}_3$  ( $M = \text{Mn and Ni}$ ), *J. Phys. Chem. C* **126**, 6791 (2022).
- [71] A. K. Budniak, S. J. Zelewski, M. Birowska, T. Woźniak, T. Bendikov, Y. Kauffmann, Y. Amouyal, R. Kudrawiec, and E. Lifshitz, Spectroscopy and structural investigation of iron phosphorus trisulfide- $\text{FePS}_3$ , *Adv. Opt. Mater.* **10**, 2102489 (2022).
- [72] R. Basnet, K. Kotur, M. Rybak, C. Stephenson, S. Bishop, C. Autieri, M. Birowska, and J. Hu, Controlling magnetic exchange and anisotropy by nonmagnetic ligand substitution in layered  $\text{MPX}_3$  ( $M = \text{Ni, Mn}$ ;  $X = \text{S, Se}$ ), *Phys. Rev. Research* **4**, 023256 (2022).
- [73] R. Samal, G. Sanyal, B. Chakraborty, and C. S. Rout, Two-dimensional transition metal phosphorous trichalcogenides ( $\text{MPX}_3$ ): A review on emerging trends, current state and future perspectives, *J. Mater. Chem. A* **9**, 2560 (2021).
- [74] S. Calder, A. V. Haglund, A. I. Kolesnikov, and D. Mandrus, Magnetic exchange interactions in the van der Waals layered antiferromagnet  $\text{MNPS}_3$ , *Phys. Rev. B* **103**, 024414 (2021).
- [75] T. T. Mai, K. F. Garrity, A. McCreary, J. Argo, J. R. Simpson, V. Doan-Nguyen, R. V. Aguilar, and A. R. H. Walker, Magnon-phonon hybridization in 2D antiferromagnet  $\text{MnPS}_3$ , *Sci. Adv.* **7**, eabj3106 (2021).
- [76] M. Birowska, P. E. Faria Junior, J. Fabian, and J. Kunstmann, Large exciton binding energies in  $\text{MNPS}_3$  as a case study of a van der Waals layered magnet, *Phys. Rev. B* **103**, L121108 (2021).
- [77] F. Dimberger, R. Bushati, B. Datta, A. Kumar, A. H. MacDonald, E. Baldini, and V. M. Menon, Observation of spin-correlated exciton-polaritons in a van der Waals magnet, *arXiv:2203.06129*.
- [78] Q. Pei, Y. Song, X. Wang, J. Zou, and W. Mi, Superior electronic structure in two-dimensional  $\text{MnPS}_3/\text{MoS}_2$  van der Waals heterostructures, *Sci. Rep.* **7**, 9504 (2017).
- [79] J. R. Schaibley, H. Yu, G. Clark, P. Rivera, J. S. Ross, K. L. Seyler, W. Yao, and X. Xu, Valleytronics in 2D materials, *Nat. Rev. Mater.* **1**, 16055 (2016).
- [80] S. A. Vitale, D. Nezhich, J. O. Varghese, P. Kim, N. Gedik, P. Jarillo-Herrero, D. Xiao, and M. Rothschild, Valleytronics: Opportunities, challenges, and paths forward, *Small* **14**, 1801483 (2018).
- [81] L. Zhang, X. Huang, H. Dai, M. Wang, H. Cheng, L. Tong, Z. Li, X. Han, X. Wang, L. Ye, and J. Han, Proximity-coupling-induced significant enhancement of coercive field and curie temperature in 2D van der Waals heterostructures, *Adv. Mater.* **32**, 2002032 (2020).
- [82] C. F. Schippers, H. J. M. Swagten, and M. H. D. Guimarães, Large interfacial spin-orbit torques in layered antiferromagnetic insulator  $\text{NiPS}_3$ /ferromagnet bilayers, *Phys. Rev. Materials* **4**, 084007 (2020).
- [83] P. Hohenberg and W. Kohn, Inhomogeneous electron gas, *Phys. Rev.* **136**, B864 (1964).
- [84] P. Giannozzi *et al.*, Quantum Espresso: A modular and open-source software project for quantum simulations of materials, *J. Phys.: Condens. Matter* **21**, 395502 (2009).

- [85] Q. Pei, X. Wang, J. Zou, and W. Mi, Efficient band structure modulations in two-dimensional  $\text{MnPSe}_3/\text{CrSiTe}_3$  van der Waals heterostructures, *Nanotechnology* **29**, 214001 (2018).
- [86] G. Kresse and D. Joubert, From ultrasoft pseudopotentials to the projector augmented-wave method, *Phys. Rev. B* **59**, 1758 (1999).
- [87] J. P. Perdew, K. Burke, and M. Ernzerhof, Generalized Gradient Approximation Made Simple, *Phys. Rev. Lett.* **77**, 3865 (1996).
- [88] S. Grimme, Semiempirical GGA-type density functional constructed with a long-range dispersion correction, *J. Comput. Chem.* **27**, 1787 (2006).
- [89] S. Grimme, J. Antony, S. Ehrlich, and H. Krieg, A consistent and accurate *ab initio* parametrization of density functional dispersion correction (DFT-D) for the 94 elements H-Pu, *J. Chem. Phys.* **132**, 154104 (2010).
- [90] V. Barone, M. Casarin, D. Forrer, M. Pavone, M. Sambri, and A. Vittadini, Role and effective treatment of dispersive forces in materials: Polyethylene and graphite crystals as test cases, *J. Comput. Chem.* **30**, 934 (2009).
- [91] P. Blaha, K. Schwarz, G. K. H. Madsen, D. Kvasnicka, and J. Luitz, *WIEN2K, An Augmented Plane Wave + Local Orbitals Program for Calculating Crystal Properties* (Vienna University of Technology, Institute of Materials Chemistry, 2001).
- [92] V. I. Anisimov, I. V. Solovyev, M. A. Korotin, M. T. Czyżyk, and G. A. Sawatzky, Density-functional theory and NiO photoemission spectra, *Phys. Rev. B* **48**, 16929 (1993).
- [93] V. Grasso and L. Silipigni, Optical absorption and reflectivity study of the layered  $\text{MnPSe}_3$  seleniophosphate, *J. Opt. Soc. Am. B* **16**, 132 (1999).
- [94] B. Fülöp, A. Márfy, S. Zihlmann, M. Gmitra, E. Tóvári, B. Szentpéteri, M. Kedves, K. Watanabe, T. Taniguchi, J. Fabian *et al.*, Boosting proximity spin-orbit coupling in graphene/ $\text{WSe}_2$  heterostructures via hydrostatic pressure, *npj 2D Mater. Appl.* **5**, 82 (2021).
- [95] T. Frank, P. Högl, M. Gmitra, D. Kochan, and J. Fabian, Protected Pseudo-helical Edge States in  $\mathbb{Z}_2$ -Trivial Proximitized Graphene, *Phys. Rev. Lett.* **120**, 156402 (2018).
- [96] K. Zollner, A. W. Cummings, S. Roche, and J. Fabian, Graphene on two-dimensional hexagonal BN, AlN, and GaN: Electronic, spin-orbit, and spin relaxation properties, *Phys. Rev. B* **103**, 075129 (2021).
- [97] K. Zollner, M. Gmitra, and J. Fabian, Heterostructures of graphene and hBN: Electronic, spin-orbit, and spin relaxation properties from first principles, *Phys. Rev. B* **99**, 125151 (2019).
- [98] J.-X. Lin, Y.-H. Zhang, E. Morissette, Z. Wang, S. Liu, D. Rhodes, K. Watanabe, T. Taniguchi, J. Hone, and J. I. A. Li, Spin-orbit driven ferromagnetism at half moire filling in magic-angle twisted bilayer graphene, *Science* **375**, 437 (2022).
- [99] K. Zollner, M. Gmitra, and J. Fabian, Swapping Exchange and Spin-Orbit Coupling in 2D van der Waals Heterostructures, *Phys. Rev. Lett.* **125**, 196402 (2020).
- [100] K. Zollner and J. Fabian, Bilayer graphene encapsulated within monolayers of  $\text{WS}_2$  or  $\text{Cr}_2\text{Ge}_2\text{Te}_6$ : Tunable proximity spin-orbit or exchange coupling, *Phys. Rev. B* **104**, 075126 (2021).
- [101] K. Zollner, M. Gmitra, and J. Fabian, Proximity spin-orbit and exchange coupling in ABA and ABC trilayer graphene van der Waals heterostructures, *Phys. Rev. B* **105**, 115126 (2022).
- [102] D. Kochan, S. Imer, and J. Fabian, Model spin-orbit coupling Hamiltonians for graphene systems, *Phys. Rev. B* **95**, 165415 (2017).
- [103] V. T. Phong, N. R. Walet, and F. Guinea, Effective interactions in a graphene layer induced by the proximity to a ferromagnet, *2D Mater.* **5**, 014004 (2017).
- [104] K. Zollner, M. Gmitra, T. Frank, and J. Fabian, Theory of proximity-induced exchange coupling in graphene on  $\text{hBN}/(\text{Co}, \text{Ni})$ , *Phys. Rev. B* **94**, 155441 (2016).
- [105] Y. Baskin and L. Meyer, Lattice constants of graphite at low temperatures, *Phys. Rev.* **100**, 544 (1955).
- [106] Y. Gu, Q. Zhang, C. Le, Y. Li, T. Xiang, and J. Hu, Ni-based transition metal trichalcogenide monolayer: A strongly correlated quadruple-layer graphene, *Phys. Rev. B* **100**, 165405 (2019).
- [107] A. R. Wildes, B. Roessli, B. Lebech, and K. W. Godfrey, Spin waves and the critical behaviour of the magnetization in  $\text{MnPS}_3$ , *J. Phys.: Condens. Matter* **10**, 6417 (1998).
- [108] K. Kurosawa, S. Saito, and Y. Yamaguchi, Neutron diffraction study on  $\text{MnPS}_3$  and  $\text{FePS}_3$ , *J. Phys. Soc. Jpn.* **52**, 3919 (1983).
- [109] D. Lançon, H. C. Walker, E. Ressouche, B. Ouladdiaf, K. C. Rule, G. J. McIntyre, T. J. Hicks, H. M. Rønnow, and A. R. Wildes, Magnetic structure and magnon dynamics of the quasi-two-dimensional antiferromagnet  $\text{FePS}_3$ , *Phys. Rev. B* **94**, 214407 (2016).
- [110] M. A. Susner, M. Chyasnachyus, M. A. McGuire, P. Ganesh, and P. Maksymovych, Metal thio- and selenophosphates as multifunctional van der Waals layered materials, *Adv. Mater.* **29**, 1602852 (2017).
- [111] F. Wang, T. A. Shifa, P. Yu, P. He, Y. Liu, F. Wang, Z. Wang, X. Zhan, X. Lou, F. Xia, and J. He, New frontiers on van der Waals layered metal phosphorous trichalcogenides, *Adv. Funct. Mater.* **28**, 1802151 (2018).
- [112] R. Brec, Review on structural and chemical properties of transition metal phosphorous trisulfides  $\text{MPS}_3$ , *Solid State Ionics* **22**, 3 (1986).
- [113] G. Ouvrard, R. Brec, and J. Rouxel, Structural determination of some  $\text{MPS}_3$  layered phases ( $\text{M} = \text{Mn}, \text{Fe}, \text{Co}, \text{Ni}$  and  $\text{Cd}$ ), *Mater. Res. Bull.* **20**, 1181 (1985).
- [114] R. R. Rao and A. K. Raychaudhuri, Magnetic studies of a mixed antiferromagnetic system  $\text{Fe}_{1-x}\text{Ni}_x\text{P}_3\text{S}_{13}$ , *J. Phys. Chem. Solids* **53**, 577 (1992).
- [115] A. R. Wildes, V. Simonet, E. Ressouche, R. Ballou, and G. J. McIntyre, The magnetic properties and structure of the quasi-two-dimensional antiferromagnet  $\text{CoPS}_3$ , *J. Phys.: Condens. Matter* **29**, 455801 (2017).
- [116] Q. Zhang, K. Hwangbo, C. Wang, Q. Jiang, J.-H. Chu, H. Wen, D. Xiao, and X. Xu, Observation of giant optical linear dichroism in a zigzag antiferromagnet  $\text{FePS}_3$ , *Nano Lett.* **21**, 6938 (2021).
- [117] T. Olsen, Magnetic anisotropy and exchange interactions of two-dimensional  $\text{FePS}_3$ ,  $\text{NiPS}_3$  and  $\text{MnPS}_3$  from first principles calculations, *J. Phys. D* **54**, 314001 (2021).
- [118] M. Newville, T. Stensitzki, D. B. Allen, and A. Ingarciola, LMFIT: Non-Linear Least-Square Minimization and Curve-

- Fitting for Python (0.8.0). Zenodo (2014), <https://doi.org/10.5281/zenodo.11813>.
- [119] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/PhysRevB.106.035137>, where we show band structures, density of states, and fit results for the remaining graphene/ $MPX_3$  heterostructures. For the  $MnPS_3$  case we also show the calculated spin polarizations on graphene.
- [120] V. M. Pereira, A. H. Castro Neto, and N. M. R. Peres, Tight-binding approach to uniaxial strain in graphene, *Phys. Rev. B* **80**, 045401 (2009).
- [121] B. Wunsch, F. Guinea, and F. Sols, Dirac-point engineering and topological phase transitions in honeycomb optical lattices, *New J. Phys.* **10**, 103027 (2008).
- [122] B. Fülöp, A. Márfy, E. Tóvári, M. Kedves, S. Zihlmann, D. Indolese, Z. Kovács-Krausz, K. Watanabe, T. Taniguchi, C. Schönberger *et al.*, New method of transport measurements on van der Waals heterostructures under pressure, *J. Appl. Phys.* **130**, 064303 (2021).
- [123] G. Graziano, J. Klimeš, F. Fernandez-Alonso, and A. Michaelides, Improved description of soft layered materials with van der Waals density functional theory, *J. Phys.: Condens. Matter* **24**, 424216 (2012).
- [124] M. Gmitra, S. Konschuh, C. Ertler, C. Ambrosch-Draxl, and J. Fabian, Band-structure topologies of graphene: Spin-orbit coupling effects from first principles, *Phys. Rev. B* **80**, 235431 (2009).
- [125] S. Konschuh, M. Gmitra, and J. Fabian, Tight-binding theory of the spin-orbit coupling in graphene, *Phys. Rev. B* **82**, 245412 (2010).
- [126] K. Zollner and J. Fabian, Single and bilayer graphene on the topological insulator  $Bi_2Se_3$ : Electronic and spin-orbit properties from first principles, *Phys. Rev. B* **100**, 165141 (2019).